

Pileup mitigation at the LHC

A theorist's view

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CEA Saclay, SPP (CMS) — March 16 2018

What is pileup and why is it there?
Why is it bad?

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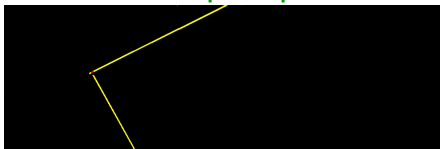
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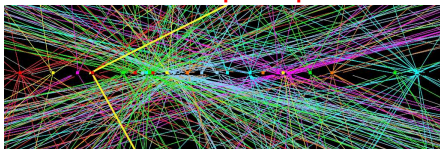
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No pileup



Clear picture

With pileup [ATLAS event]

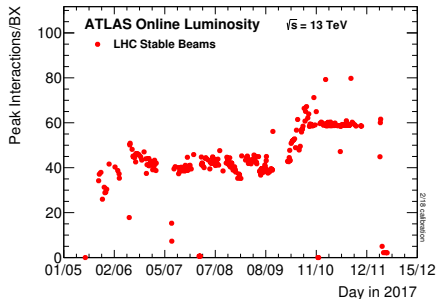


Not so clear!

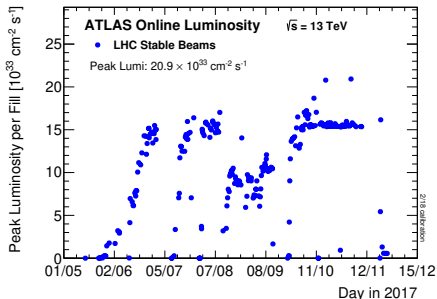
Soft (low-energy) background blurring your resolution \Rightarrow to be mitigated

Typical numbers

(peak) Pileup multiplicity



(peak) collision rate (luminosity)



- $\mu = \langle N_{PU} \rangle$: increased from ~ 20 (Run I) to ~ 40 (early Run II) and now ~ 60 (late 2017)
- Will keep increasing in the future with 140 – 200 planned for HL-LHC
- Collisions rate (luminosity) increases in parallel

Idea/Plan for the talk

- Useful simple characterisation of pileup
- Review of the area–median pileup subtraction technique (currently in use at the LHC)
- Comparison with other basic approaches
- Go over ideas for new pileup mitigation techniques
- Highlight that some level of (analytic) understanding can be achieved

A few (purposeful) over-simplifications

- no detector response/simulation
- purely “in-time” pileup
- often neglect UE for simplicity
- will concentrate on jet quantities (MET and lepton/photon isolation have extra dependence (tuning) on detector details)
- will mostly focus on the jet p_t

Early clarifications/disclaimers

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- no detector response/simulation
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But...

- detector and out-of-time PU: minor impact expected (at least qualitatively and for the physics message)
- I'll briefly discuss other quantities than the jet p_t when relevant
- I can come back to these points if necessary (closer to the end)

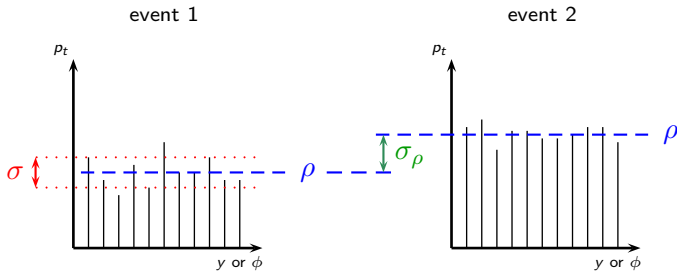
Simple characterisation of pileup

Simple (and very helpful!) characterisation

Pileup is roughly uniform (in $y - \phi$)

Pileup mostly characterised by 3 numbers

- ρ : the average activity in an event (per unit area)
- σ : the intra-event fluctuations (per unit area)
- σ_ρ : the event-to-event fluctuations of ρ



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Jet of momentum p_t and area A (more below):

$$\text{one event: } p_t \xrightarrow{+\text{pileup}} p_t + \rho A \pm \sigma \sqrt{A}$$

$$\text{event average: } p_t \xrightarrow{+\text{pileup}} p_t + \langle \rho \rangle A \pm \sigma_\rho A \pm \sigma \sqrt{A}$$

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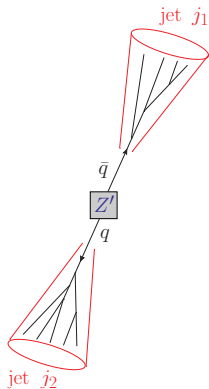
p_t shift

p_t smearing
resolution degradation

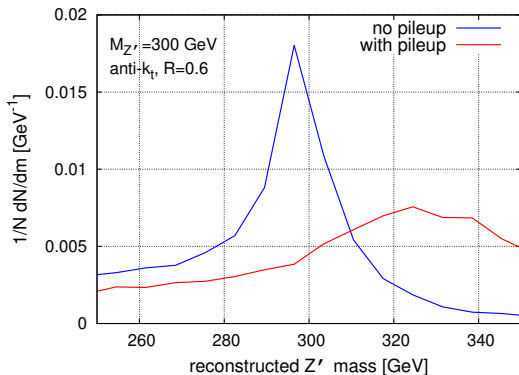
Pileup effects: explicit example

Example: (fictitious new) Z' boson with $M_{Z'} = 300$ GeV

$$Z' \rightarrow q\bar{q} \rightarrow jj$$



$$Z' \approx j_1 + j_2$$



Pileup mitigation

1. generic strategy

$$p_t^{(\text{truth})} \xrightarrow{+\text{pileup}} p_t^{(\text{full})} \xrightarrow{\text{subtract}} p_t^{(\text{sub})}$$

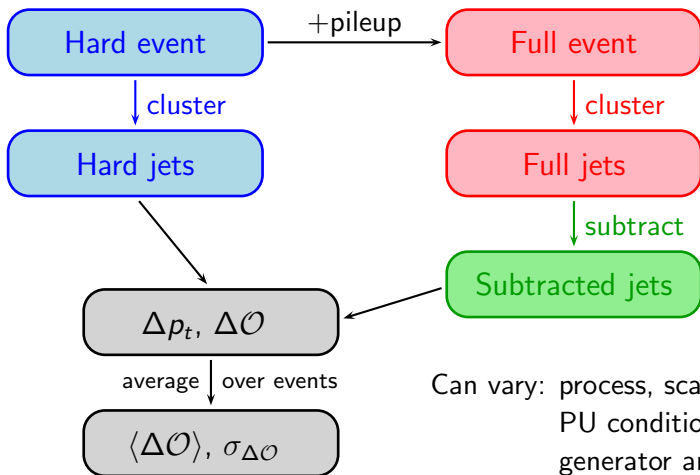
Goal: $p_t^{(\text{sub})} \approx p_t^{(\text{truth})}$, i.e. $\Delta p_t = p_t^{(\text{sub})} - p_t^{(\text{truth})} \approx 0$.

More precisely, the subtraction should be:

- 1 **Unbiased:** $\langle \Delta p_t \rangle_{\text{events}} \approx 0$
- 2 **Sharp (good resolution):** $\sigma_{\Delta p_t}$ as small as possible
Alternative width measurements possible (but avoid correlation coefficients)
- 3 **Robust:** independent of the jet p_t , rapidity, N_{PU} , the process, ...

Testing framework

Tests based on Monte-Carlo event generators:



Can vary: process, scales,
PU conditions
generator and tune

Pileup mitigation

2. the area–median technique

[M.Cacciari, G.P. Salam, GS, 2008]

Remember:

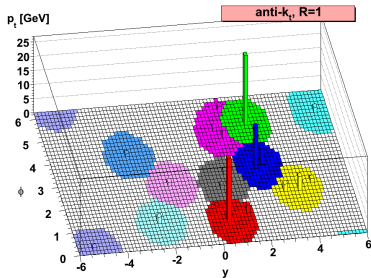
$$p_t \xrightarrow{+\text{pileup}} p_t + \rho A \pm \sigma \sqrt{A}$$

Remember:

$$p_t \xrightarrow{+\text{pileup}} p_t + \rho A \pm \sigma \sqrt{A}$$

Introduce an “Active” area definition:

- Add “ghosts” to the event:
 - particles with infinitesimal p_t
 - on a grid (+fluct.) of cell area a_0
- Include the ghosts in the clustering
- If a jet contains N_g ghosts, its area is $N_g a_0$

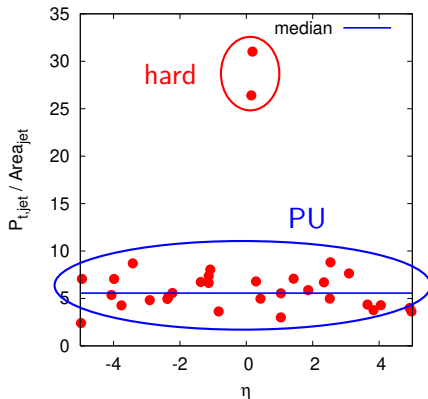


Area–median pileup subtraction method

[M.Cacciari, G.P. Salam, 08]

$$\text{Estimation: } \rho_{\text{est}} = \text{median}_{j \in \text{patches}} \left\{ \frac{p_{t,j}}{A_j} \right\}$$

$$\text{Subtraction: } p_{t,\text{jet}}^{(\text{sub})} = p_{t,\text{jet}} - \rho_{\text{est}} A_{\text{jet}}$$

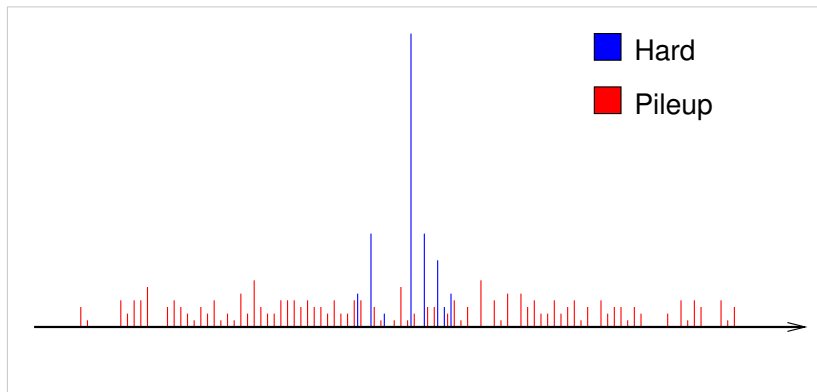


per jet
per event
(typically)

break the event in
patches of similar size
e.g. cluster with k_t
or break into grid cells

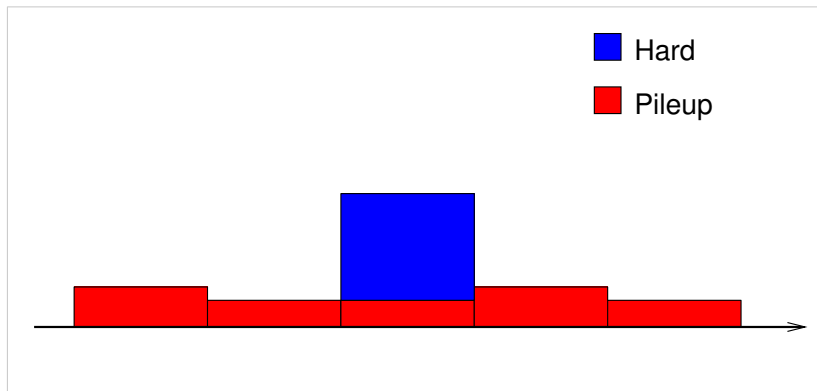
Simple discussion of pileup subtraction (take 1)

To illustrate the physics, use a simple (1-D) event with 1 jet + PU



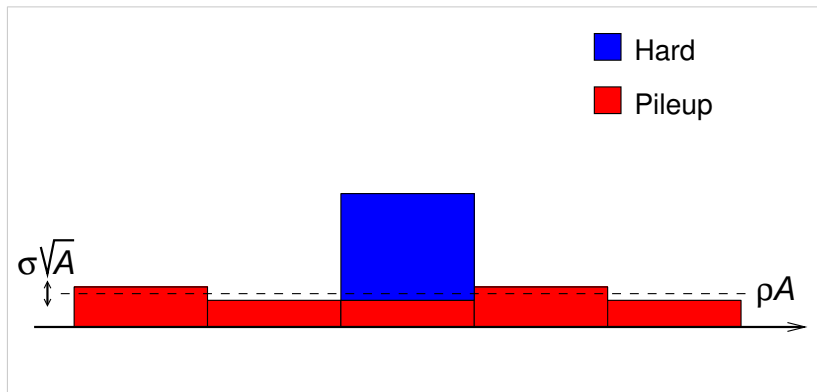
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Subtract pileup from the **hard jets**



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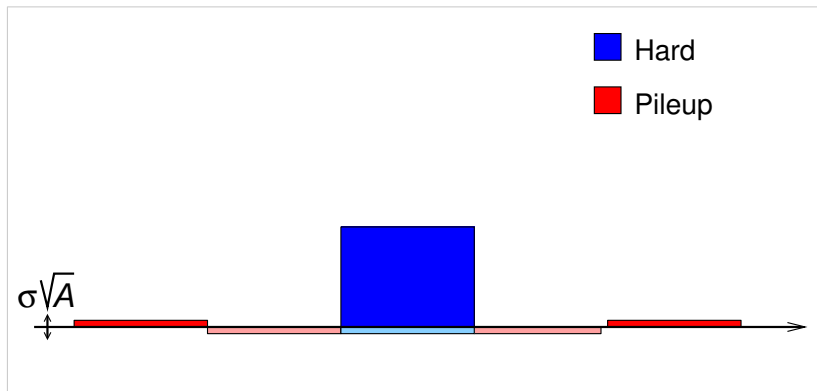
Subtract pileup from the **hard jets**



Area-median subtraction would subtract ρA

Simple discussion of pileup subtraction (take 1)

Subtract pileup from the **hard jets**

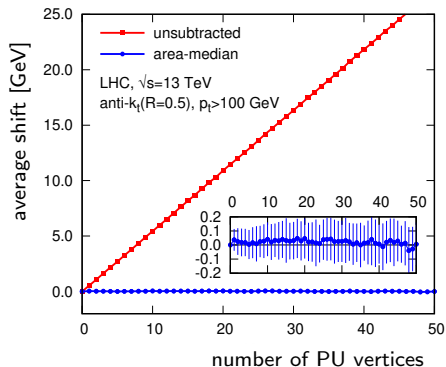


For the **hard jets**: **unbiased** (average ≈ 0) and **robust**
smearing $\approx \sigma\sqrt{A}$ (smaller than $\pm\sigma_{\rho}A \pm \sigma\sqrt{A}$)

Subtraction benchmarks

[revamped Les-Houches 2011 study]

average p_t shift



No subtraction

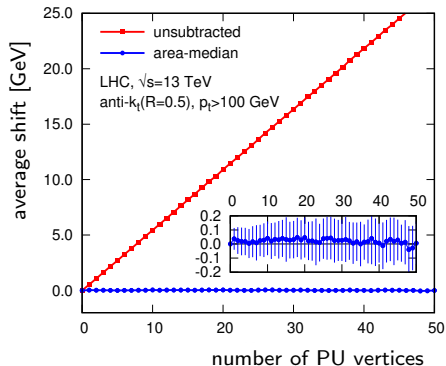
area-median
subtraction

corrected for shift

Subtraction benchmarks

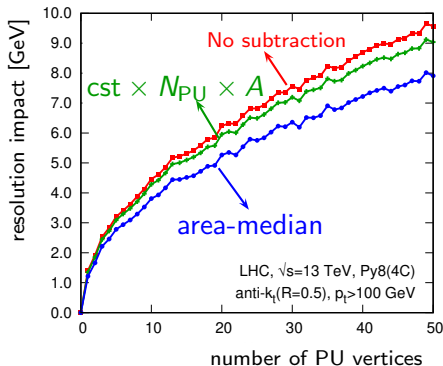
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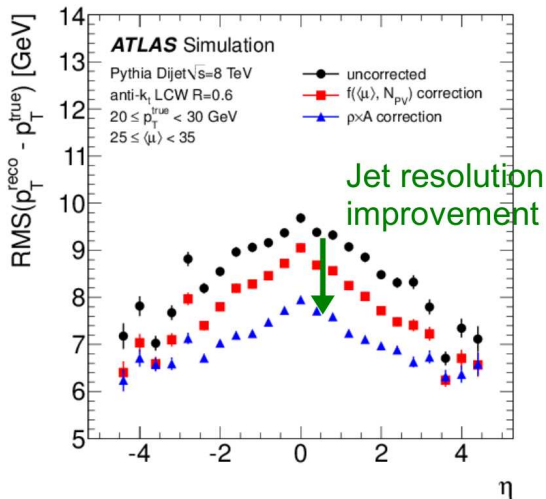
impact on resolution



resolution improved
event-by-event ρ is key

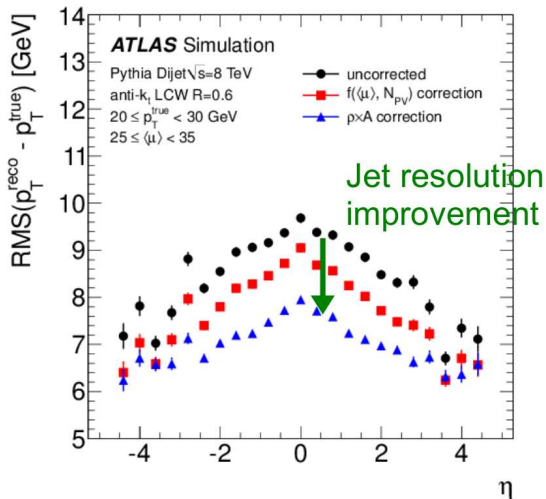
PU subtraction as seen in ATLAS

[B. Petersen, ATLAS Status report for the LHCC, 2013]



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Gain compared to a
 $f(\mu, N_{PV})$ correction:

even-by-event determination
of ρ captures the fluctuations
better than an (averaged)
fixed function

(one partial exception where $f(\mu, N_{PV})$ info helps
the area-median is for the rapidity profile in
the forward calorimeter; ask details later)

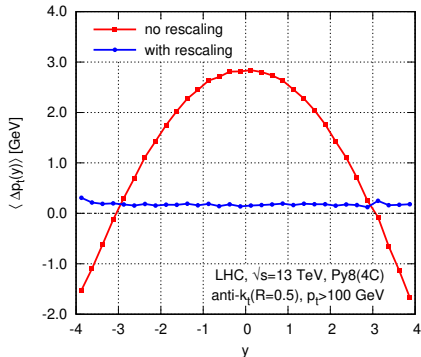
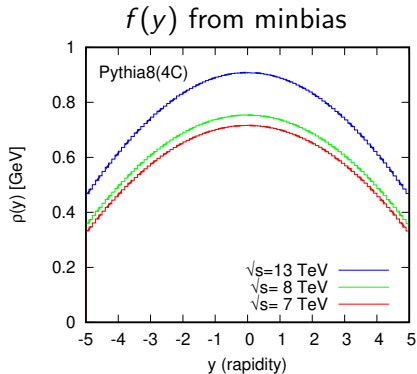
Further developments

Improvements/extensions of the basic method

- Methods to handle **positional dependence of ρ**
Directly relevant for the LHC (e.g. rapidity dependence)
[M.Cacciari,G.Salam,GS,2010-2011]
- Subtraction for **jet mass and jet shapes**
Important for jet tagging ("q v. g jet", b jet, top jet, $H \rightarrow b\bar{b}$)
[GS,G.Salam,J.Kim,S.Dutta,M.Cacciari,2013]
[P.Berta,M.Spousta,D.Miller,R.Leitner,2014]
- Applications to CHS events
[M.Cacciari,G.Salam,GS,2013]
- Applications to heavy-ion collisions (not discussed here)
[M.Cacciari,J.Rojo,G.Salam,GS,2011]
- Subtraction of **fragmentation function (moments)** (not discussed here)
Useful for quenching in $PbPb$ collisions
[M.Cacciari,P.Quiroga,G.Salam,GS,2012]

Rapidity dependence

$$\rho = \text{median}_{j \in \text{patches}} \left\{ \frac{p_{t,j}}{A_j} \right\} \quad \longrightarrow \quad \rho(y) = f(y) \text{median}_{j \in \text{patches}} \left\{ \frac{p_{t,j}}{A_j f(y_j)} \right\}$$



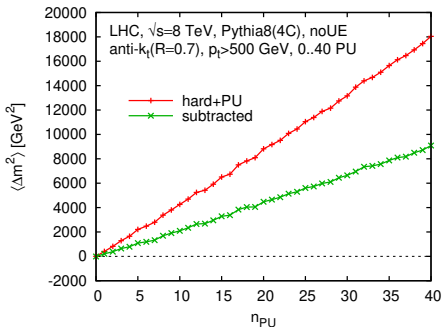
4-vector and jet mass subtraction

$$p_{\text{jet}}^{\mu,(\text{sub})} = p_{\text{jet}}^{\mu} - \rho_{\text{est}} A_{\text{jet}}^{\mu}$$

4-vector and jet mass subtraction

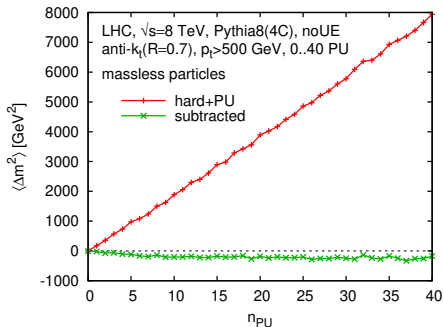
$$p_{\text{jet}}^{\mu,(\text{sub})} = p_{\text{jet}}^{\mu} - \rho_{\text{est}} A_{\text{jet}}^{\mu}$$

How do we do for the jet mass?



$$\Delta m^2 = (m_{\text{full}}^{(\text{sub})})^2 - m_{\text{hard}}^2$$

poor subtraction



OK for massless particles

4-vector and jet mass subtraction

Generic 4-vector: $(m_t = \sqrt{p_t^2 + m^2})$

$$p^\mu \equiv (p_t \cos(\phi), p_t \sin(\phi), m_t \sinh(\phi), m_t \cosh(\phi))$$

Background uniform in y and ϕ

\Rightarrow 2 degrees of freedom: p_t and m_t

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For pile-up contamination in a jet:

$$\begin{aligned} \sum_i p_i^\mu &= \sum_i (p_{t,i} \cos(\phi_i), p_{t,i} \sin(\phi_i), m_{t,i} \sinh(\phi_i), m_{t,i} \cosh(\phi_i)) \\ &= \sum_i p_{t,i} (\cos(\phi_i), \sin(\phi_i), \sinh(\phi_i), \cosh(\phi_i)) \\ &\quad + (m_{t,i} - p_{t,i}) (0, 0, \sinh(\phi_i), \cosh(\phi_i)) \end{aligned}$$

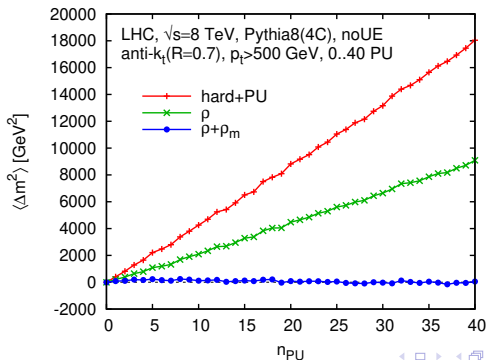
1st line is $\propto \rho \times$ ghost coverage; 2nd line is a new correction

4-vector and jet mass subtraction

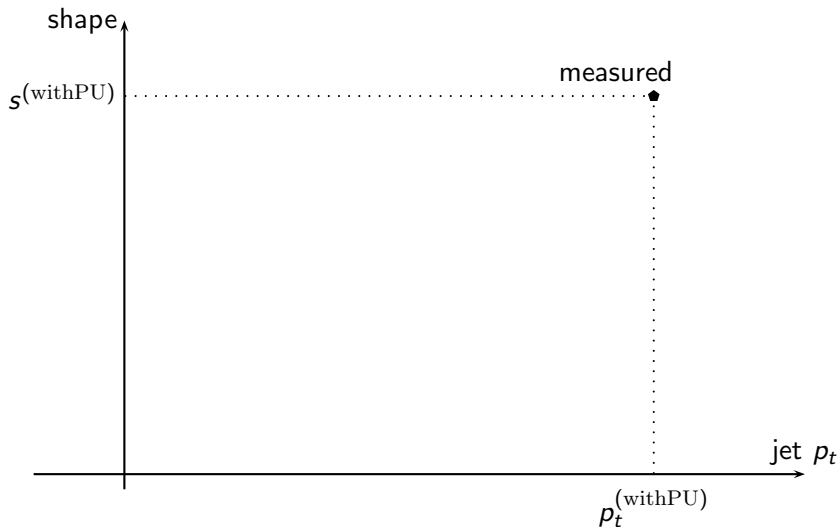
$$p_{\text{sub}}^{\mu} = p^{\mu} - \rho A^{\mu} - \rho_m A_m^{\mu}$$

with

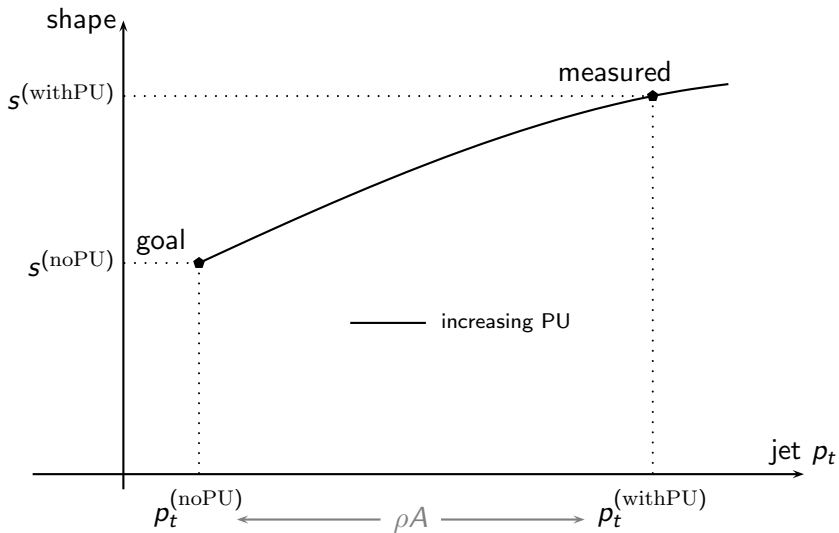
$$\rho_m = \text{median}_{j \in \text{patches}} \left\{ \frac{\sum_{i \in j} m_{t,i} - p_{t,i}}{A} \right\} \quad \text{and} \quad A_m^{\mu} \equiv (0, 0, A_z, A_E)$$



Jet shapes: extrapolation to 0 pileup



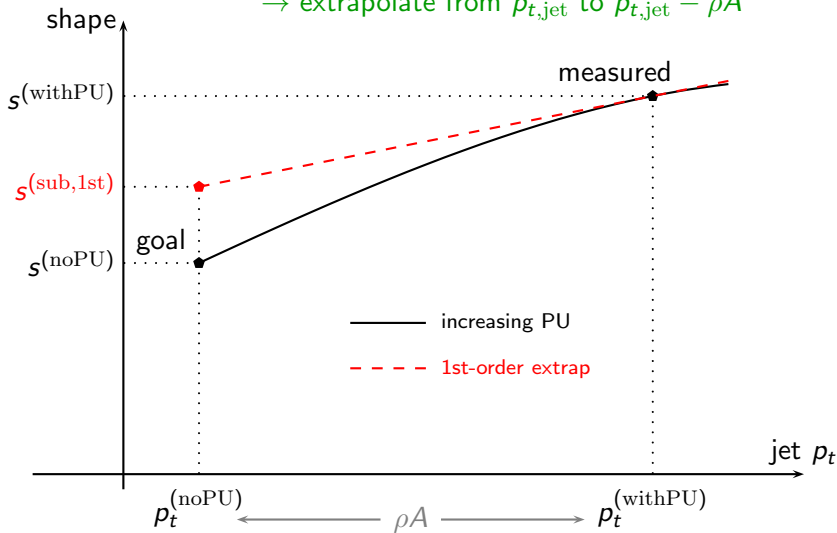
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knowledge of the derivatives wrt uniform shift of PU

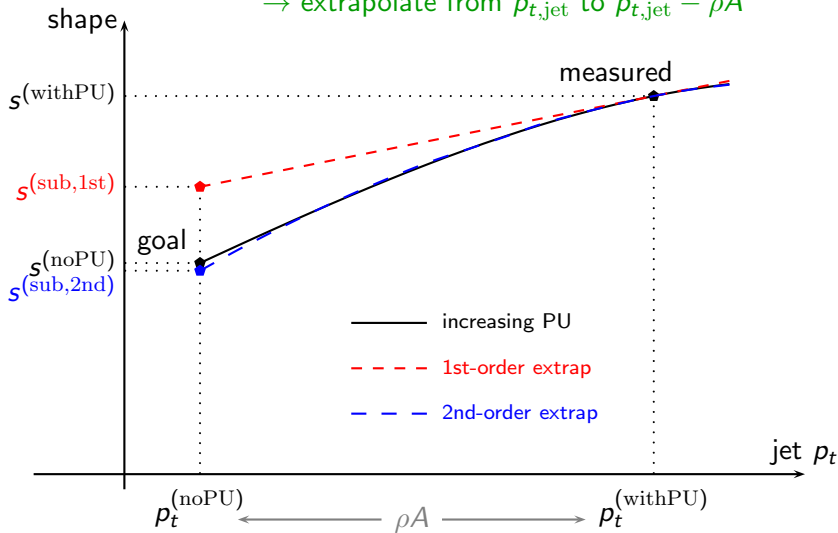
→ extrapolate from $p_{t,\text{jet}}$ to $p_{t,\text{jet}} - \rho A$



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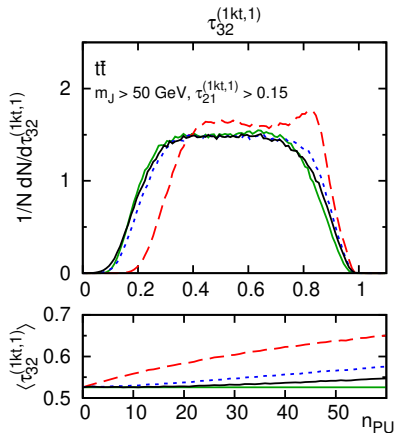
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Jet shapes performance

Example: N -subjettiness for boosted top tagging

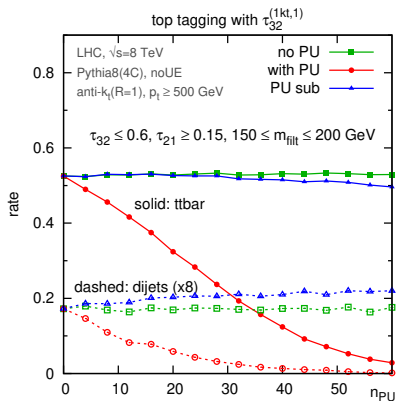


Green: truth

Red: truth+PU (unsub)

Blue: 1st order sub

Black: 2nd order sub



good performance and stability

Application to CHS events

- Assume idealised CHS (perfect separation between charged and neutral, perfect charged pileup identification)
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- Assume idealised CHS (perfect separation between charged and neutral, perfect charged pileup identification)
- Area–median applies as before with ρ estimated from the neutrals (or CHS)
- Subtleties
 - PU charged tracks can be kept as ghosts (with ∞^{al} momentum)
 - additional +ivity constraints
 - A “neutral-proportional-to-charged” (NpC) approach like

$$p_{t,\text{neutral}}^{(\text{sub})} = p_{t,\text{neutral}}^{(\text{full})} - \gamma p_{t,\text{charged}}^{(\text{PU})}$$

does a slightly worse job than the area–median
(mostly because soft physics loses the collinear correlation between charged and neutrals)

Area–median: final recommendations

Issue: information scattered over several papers

⇒ Goal/Idea: summarise recommendations for the area–median method

Recommendations

- Basic setup:

- use active areas with ghosts up to the particle rapidity acceptance (+ use `n_repeat=1` + try lowering a_0 + keep random seeds)
- estimate ρ using a grid of size 0.55 (0.5-0.7)
- use rapidity rescaling for the positional dependence

- Generic usage:

- use explicit ghosts
- include the extra ρ_m term for observables sensitive to particle masses
- use “safe mass” subtraction (avoids negative m^2)

- Specific usage:

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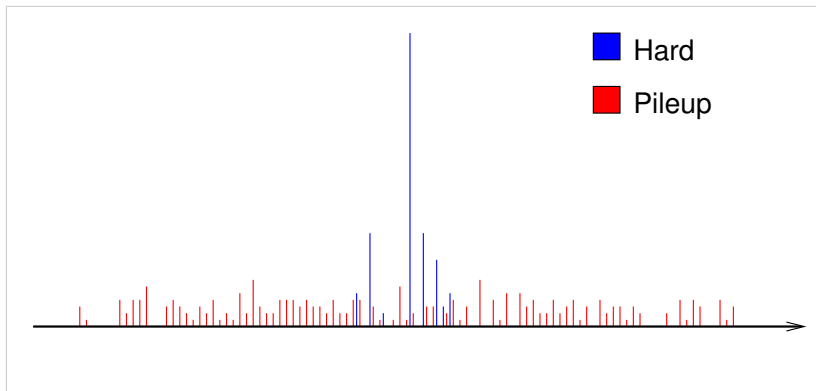
Everything implemented in FastJet

Pileup mitigation

3. towards new strategies

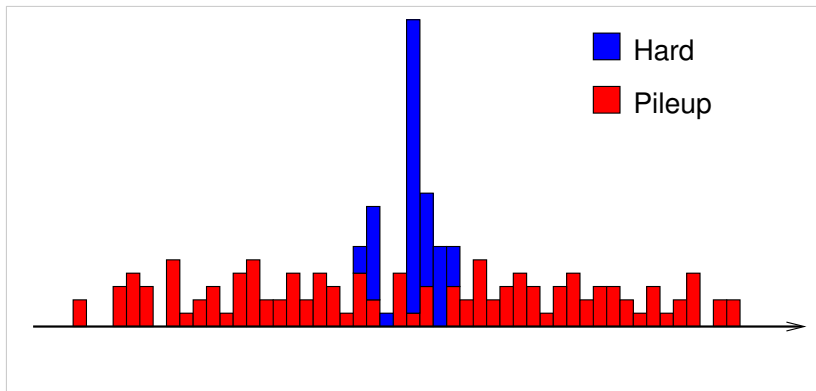
Goal: get a better resolution i.e. reduce effects of σ

Come back to our simple (1-D) event with 1 jet + PU



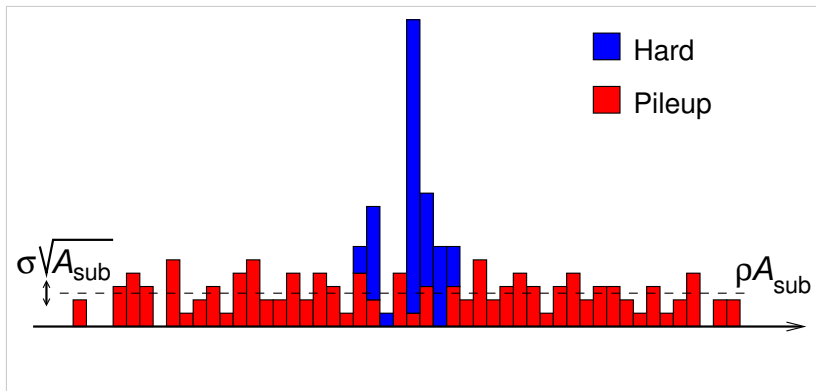
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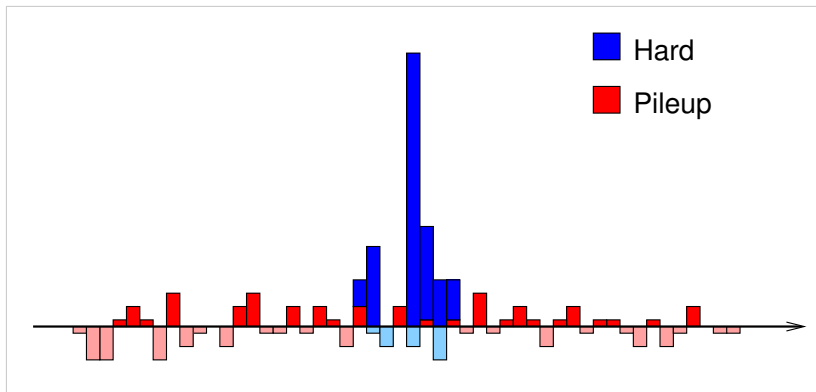
Now, we look at a smaller scale, e.g. subjets (or particles)



Similar to before: $\sum \rho A_{\text{sub}} = \rho A_{\text{jet}}$ and $\sum \sigma^2 A_{\text{sub}} = \sigma^2 A_{\text{jet}}$

Goal: get a better resolution i.e. reduce effects of σ

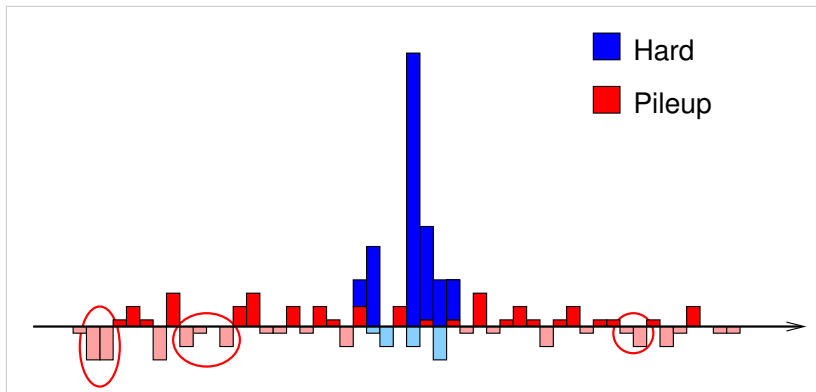
Now, we look at a smaller scale, e.g. subjets (or particles)



subtract ρA_{sub} in each subjet

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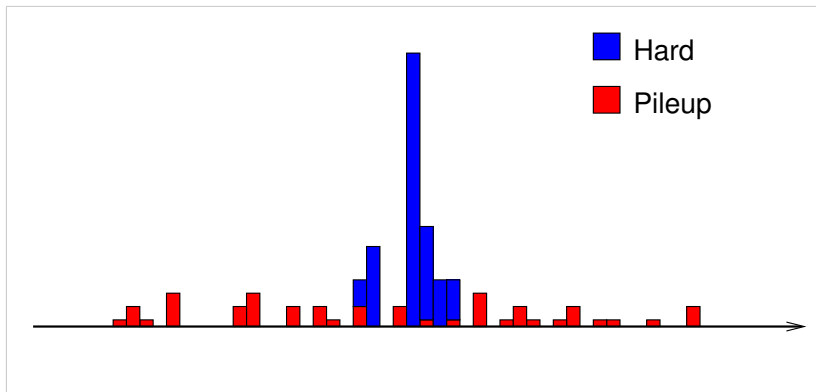
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But one gets (unphysical) negative subjets!!

Goal: get a better resolution i.e. reduce effects of σ

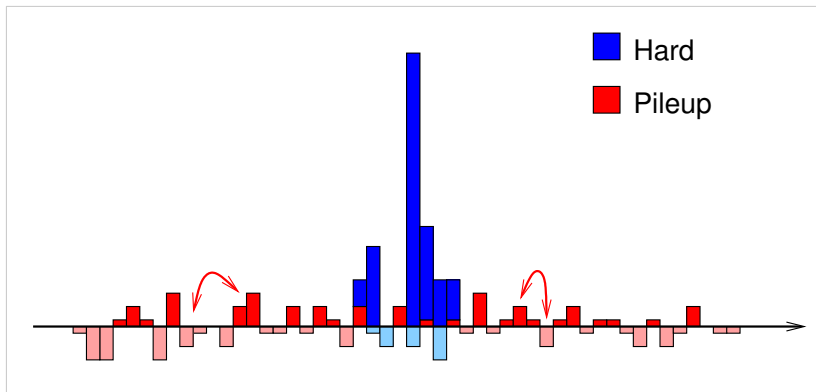
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With a simple cut: **reduced energy smearing**, **but biased** (undersubtraction)

Goal: get a better resolution i.e. reduce effects of σ

Now, we look at a smaller scale, e.g. subjects (or particles)



For an unbiased method, we need to balance negative and positive subjects

Goal: get a better resolution i.e. reduce effects of σ

Now, we look at a smaller scale, e.g. subjects (or particles)

Generic idea

Say we have a method that keeps/throws away particles (or subjects)

- PU particles kept: positive bias
- “hard” particles thrown out: negative bias

The two biases need to balance generically (all p_t , N_{PU}, \dots)

Challenge: fine-tuning to get small biases + robustness at stakes

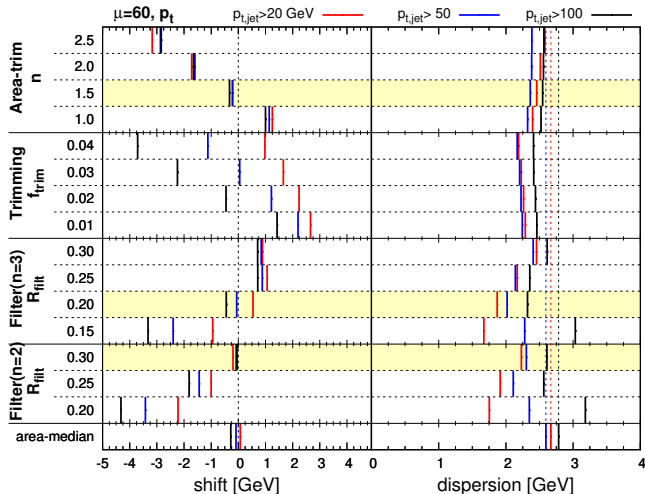
We have explored many options mostly in 2 directions:

- **Subjet-based (grooming) techniques**
 - Idea: use a grooming technique
 - Cluster the jet into smaller subjets, subtract the subjets, keep only some of the hard subjets
 - Example: keep subjets with $p_t \geq n\sigma\sqrt{A_{\text{subjet}}}$ (“above noise”)
- **even-wide particle-level subtraction**
 - Idea: cut or subtract soft particles in the whole event
 - Useful quantities to consider: particle p_t , Voronoi particle area, ...
 - various “stopping conditions” considered (examples later)

Preliminary ideas to explore (1/2)

[GS, unpublished, started in Les-Houches 2013]

Category 1: use subjets (grooming: Filtering, trimming, area-trimming)



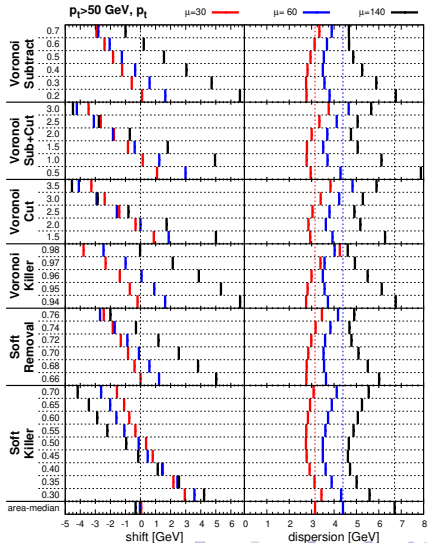
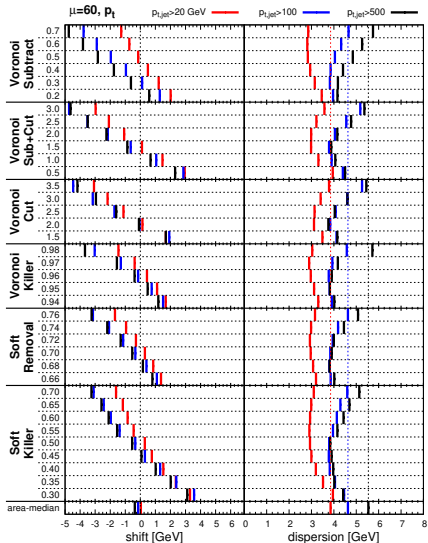
Observations:

- fine-tuning
- not so robust
- sharper

Preliminary ideas to explore (2/2)

[M.Cacciari,G.Salam,GS, unpublished]

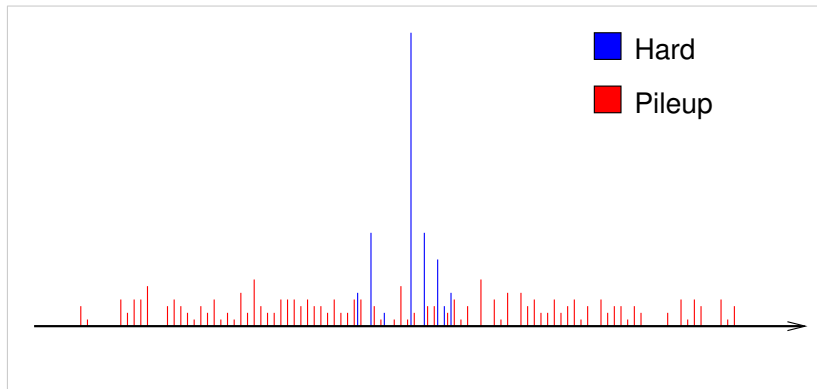
Category 2: particle-level subtraction (before clustering)



The SoftKiller approach to event-wide subtraction

[M.Cacciari, G.Salam, GS, 2014]

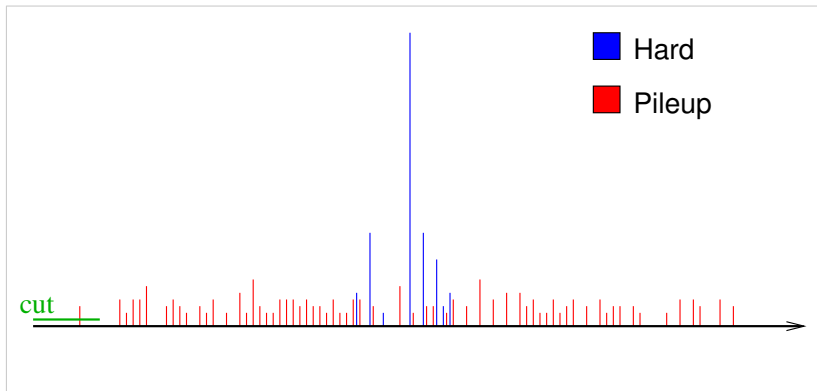
Come back to our toy event...



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[M. Cacciari, G. Salam, GS, 2014]

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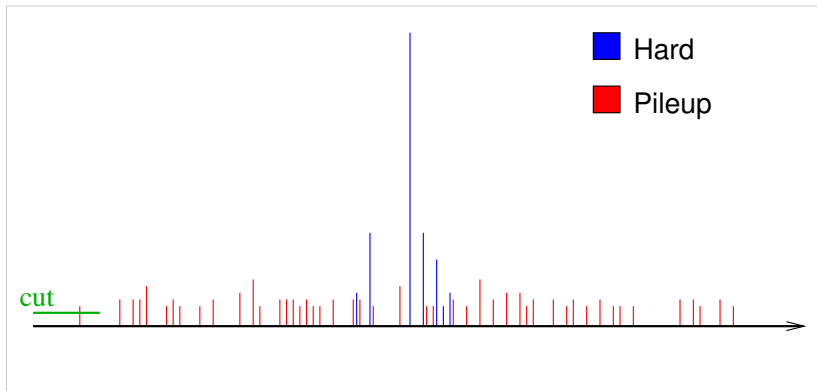


start to remove the softest particles

The SoftKiller approach to event-wide subtraction

[M.Cacciari, G.Salam, GS, 2014]

Come back to our toy event...

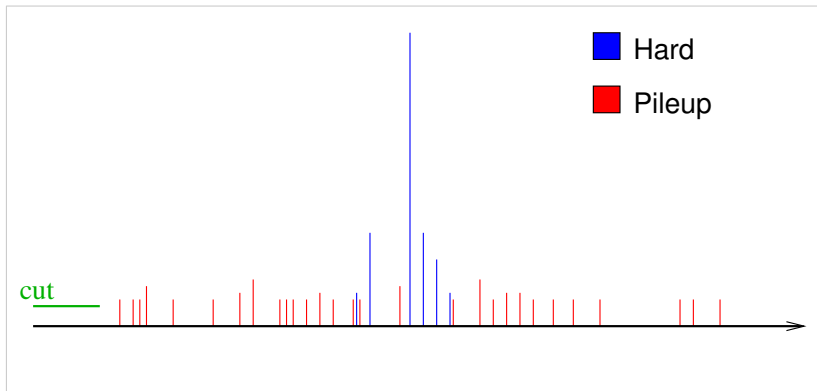


progressively increase the cut on soft particles

The SoftKiller approach to event-wide subtraction

[M.Cacciari, G.Salam, GS, 2014]

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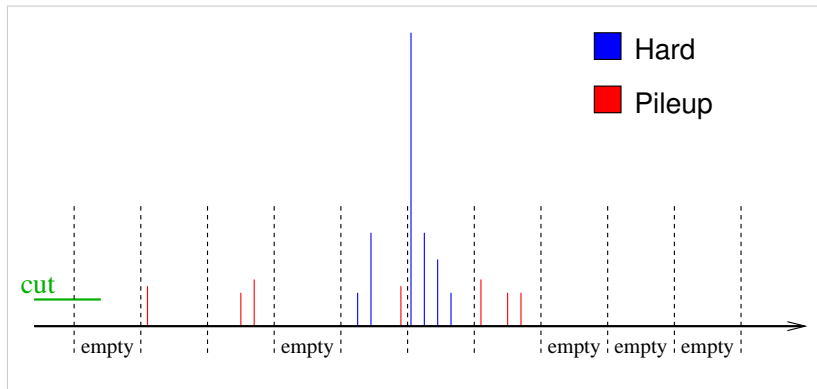


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[M.Cacciari, G.Salam, GS, 2014]

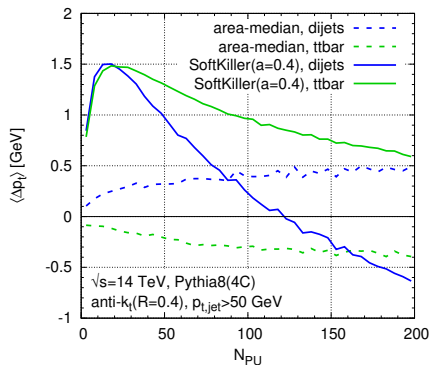
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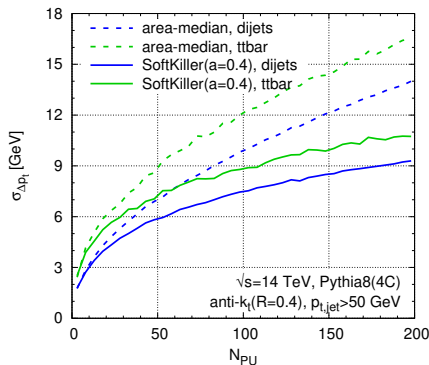
until the estimated ρ is 0 (*i.e.* half the event is empty)

The SoftKiller approach to event-wide subtraction

[M. Cacciari, G. Salam, GS, 2014]



Reasonable bias

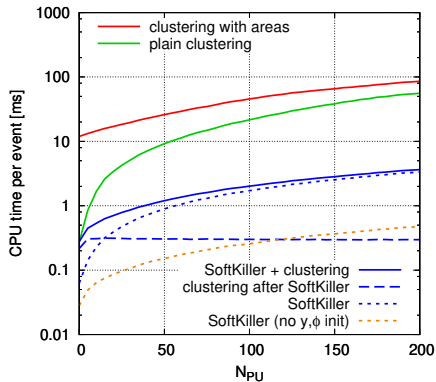


smaller dispersion

The SoftKiller approach to event-wide subtraction

[M.Cacciari,G.Salam,GS,2014]

Remarkable timings

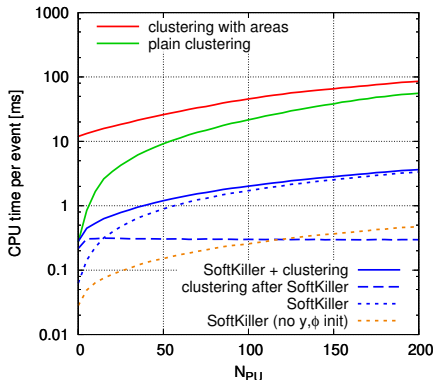


great e.g. for trigger

The SoftKiller approach to event-wide subtraction

[M. Cacciari, G. Salam, GS, 2014]

Remarkable timings



great e.g. for trigger

Preliminary work

- adding zeroing (remove if not close to a chg track from LV) helps a bit further
- Not obvious to improve on angular (R) dependence)

Analytic properties

- Many effects understood e.g. from a Gaussian approximation
- Here: also discussing more specific examples

Simple example PU+steeply-falling spectrum

Gaussian pileup: ($\sigma \ll \rho \ll p_{t,\text{jet}}$)

$$\frac{dP}{d\delta p_{t,\text{PU}}} = \frac{1}{\sqrt{2\pi A}\sigma} \exp\left(-\frac{(p_{t,\text{PU}} - \rho A)^2}{2\sigma^2 A}\right),$$

“hard” spectrum can be approximated by:

$$\frac{d\sigma_{\text{truth}}}{dp_t} = \frac{\sigma_0}{\mu} e^{-p_t/\mu}$$

We find the expected shift and smearing effects:

$$\frac{d\sigma_{\text{reco}}}{dp_t} = \frac{d\sigma_{\text{truth}}}{dp_t} \exp\left(\frac{\rho A}{\mu} + \frac{\sigma^2 A}{2\mu^2}\right)$$

and

$$p_{t,\text{truth}}^{\text{most likely}} = p_{t,\text{reco}} - \rho A - \frac{\sigma^2 A}{\mu}$$

Analytic properties of jet areas

[M.Cacciari, G.Salam, GS, 08]

Jet areas are (almost by definition) infrared unsafe.
But we can say many (analytic) things about them

Passive area (for simplicity)

Add one “ghost” ($\propto^{\text{al}} p_t$): $a_{\text{jet}} = \int dy d\phi \Theta(\text{ghost at } (y, \phi) \in \text{jet})$

Perturbative calculations of area

1 particle:

$$a = \pi R^2$$



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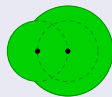
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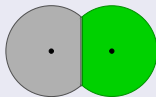
Perturbative calculations of area

1 particle + 1 soft particle:

$$a = a(\Delta) \neq \pi R^2$$



$$R/2 < \Delta_{12} < R$$



$$R < \Delta_{12} < 2R$$

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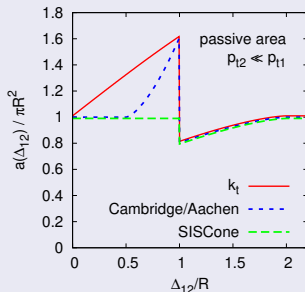
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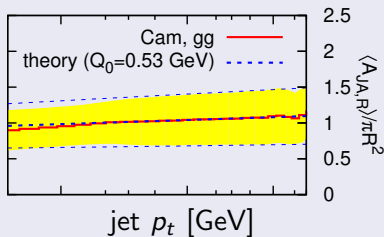
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Perturbative calculations of area

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$$\begin{aligned} \langle a \rangle &= \frac{\alpha_s}{2\pi} \int \frac{dz}{z} \frac{d\Delta}{\Delta} [a(\Delta) - a(0)] \\ &= \frac{\alpha_s}{2\pi} \log \frac{p_t}{Q_0} \mathbf{d} \end{aligned}$$



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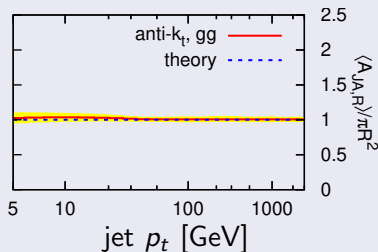
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Perturbative calculations of area

One noticeable exception:

anti- k_t jets are insensitive
to soft particles



Analytic properties of the ρ estimation

[Adapted from [M.Cacciari, G.Salam, S.Sapeta, 10]

How good is our estimation of ρ ? What drives differences?

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Setup

- Toy-model for pileup (indep particles with exp spectrum)
- soft emissions from the hard event (initial-initial state)
- Gives at least parametric estimates ($p_t, \rho, \sigma, R, \text{range}$)

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Median \neq average:

$$\frac{\rho_{\text{est}} - \rho}{\rho} \propto -\frac{\sigma^2}{\rho^2 a_{\text{grid}}^2}$$

Hard contaminates median:

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Many applications (in the thesis and beyond)

sizeable a_{grid} range, range size estimates, jet R optimisation

Usefulness of analytic control

Analytic control of 3 types:

- simple Gaussian description of PU effects
- understanding of how a jet reacts to soft particles (area understanding)
- understanding of biases of the area–median

have greatly helped the understanding of jet algs and PU subtraction

- Cone v. k_t v. anti- k_t around 2008
- understanding of areas–median biases (e.g. number of jets in the median estimate)
- understanding of grooming selection biases
- ...

Future perspectives

Several directions of varying interest and impact

Towards better PU mitigation techniques

Can we get analytic control from $(\text{pQCD})_{\text{hard}} + (\text{toy-model/data})_{\text{PU}}$?

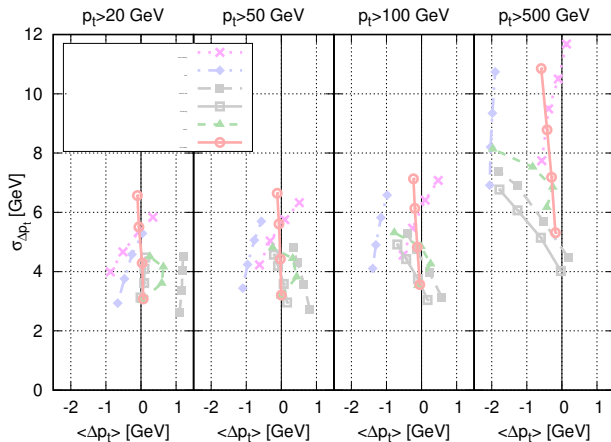
- Analytic control over SoftKiller parameter (N_{PU} , p_t , R dependence)
- Better analytic understanding of grooming techniques
- Deeper exploration of other noise-reduction techniques

Ultimate goal: use that knowledge to design efficient new techniques

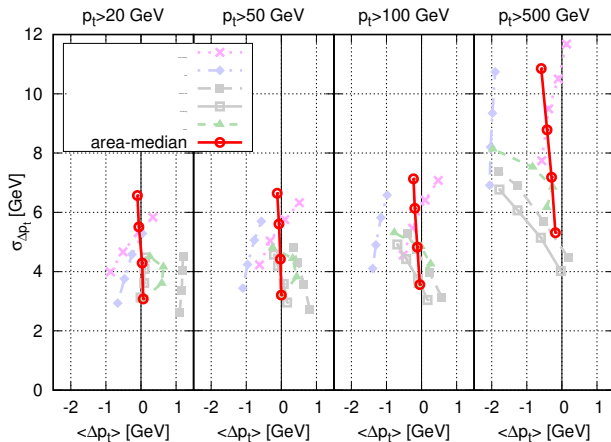
Other curiosities/open questions

- Areas to tune Monte-Carlo?
- Better analytic understanding of active areas (e.g. pure-ghost jets)
- What is the maximal reach of anti- k_t jets?

Conclusions

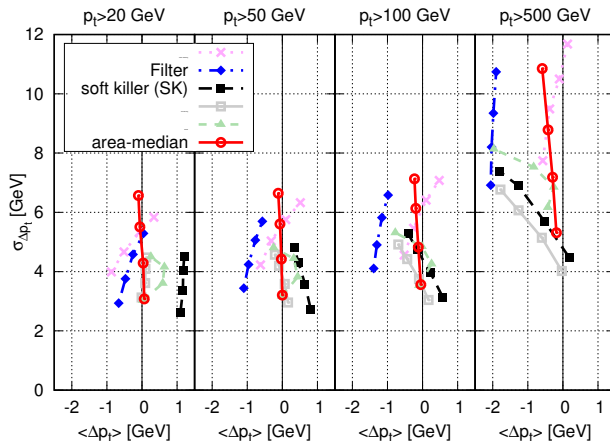


Conclusions



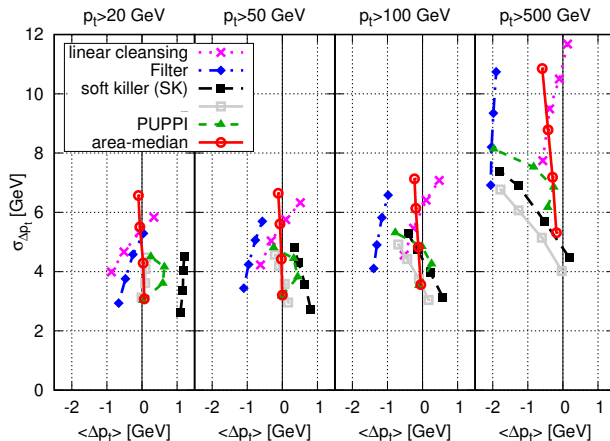
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- unbiased
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Conclusions



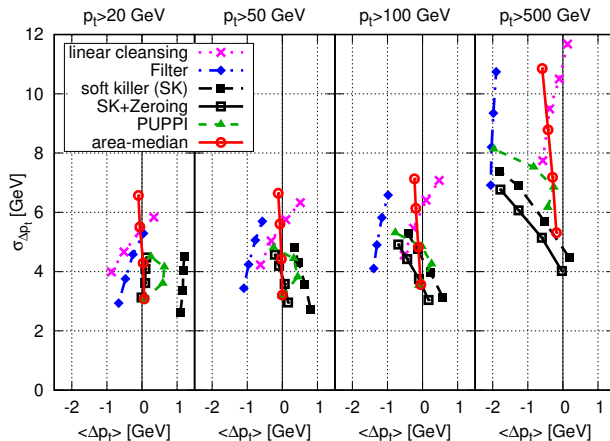
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- New candidates:
 - ▶ better resolution
 - ▶ fine-tuning

Conclusions



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Conclusions



- Area-median
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- “external” not reviewed here
- Stay tuned