

# The quest for precision across scales

Gregory Soyez

arXiv:2002:11114 with M.Dasgupta, F.Dreyer, K.Hamilton, P.Monni and G.Salam

IPhT, CNRS, CEA Saclay

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- Motivate the importance of event generators
- Parton showers
  - ▶ What physics goes in?
  - ▶ How is it built?
  - ▶ Some recent progress
- Assessing parton shower accuracy
- the PanScales showers
  - ▶ Solving current issues
  - ▶ NLL accuracy

# Importance of Event Generators

## Simulate events using Monte-Carlo techniques

- All-purpose generators simulating a “full event”  
3 main tools: Pythia, Herwig, Sherpa
- more specific tools (e.g. fixed-order, parton shower)  
long list of tools: e.g. aMC@NLO, POWHEG, Vincia, Dire, ...

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### Main advantage: versatility

- “realistic” and very generic aspects of all-purpose generators  
(including combination with detector simulation)
- broad range of analyses (any phase-space cut, observable, ...)

# What do Event Generators provide?

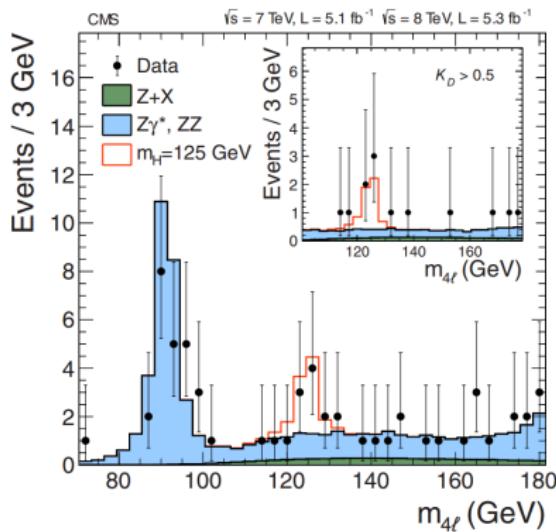
Broad range of applications



Searches

Background (and signal) estimate

Example:  
 $H \rightarrow ZZ \rightarrow 4\ell$   
[CMS, arXiv:1207.7235]



# What do Event Generators provide?

Broad range of applications

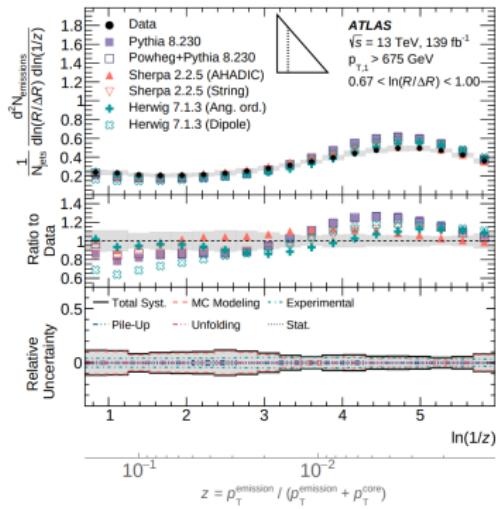


Searches

Measurements

Idea: data v. MC

- allows the use of MC as modelling tool
- helps developing better MC



[ATLAS, arXiv:2004.03540]

# What do Event Generators provide?

Broad range of applications



Searches

Measurements  
& modelling

Tool to estimate uncertainties

Example:  
top mass measurement  
[ATLAS-CONF-2019-046]

Source	Unc. on $m_t$ [GeV]	Stat. precision [GeV]
Data statistics	0.40	
Signal and background model statistics	0.16	
Monte Carlo generator	0.04	$\pm 0.07$
Parton shower and hadronisation	0.07	$\pm 0.07$
Initial-state QCD radiation	0.17	$\pm 0.07$
Parton shower $\alpha_S^{FSR}$	0.09	$\pm 0.04$
$b$ -quark fragmentation	0.19	$\pm 0.02$
HF-hadron production fractions	0.11	$\pm 0.01$
HF-hadron decay modelling	0.39	$\pm 0.01$
Underlying event	$< 0.01$	$\pm 0.02$
Colour reconnection	$< 0.01$	$\pm 0.02$
Choice of PDFs	0.06	$\pm 0.01$
$W/Z+jets$ modelling	0.17	$\pm 0.01$
Single top modelling	0.01	$\pm 0.01$
Fake lepton modelling ( $t \rightarrow W \rightarrow \ell$ )	0.06	$\pm 0.02$
Soft muon fake modelling	0.15	$\pm 0.03$
Jet energy scale	0.12	$\pm 0.02$
Soft muon jet $p_T$ calibration	$< 0.01$	$\pm 0.01$
Jet energy resolution	0.07	$\pm 0.05$
Jet vertex tagger	$< 0.01$	$\pm 0.01$
$b$ -tagging	0.10	$\pm 0.01$
Leptons	0.12	$\pm 0.00$
Missing transverse momentum modelling	0.15	$\pm 0.01$
Pile-up	0.20	$\pm 0.05$
Luminosity	$< 0.01$	$\pm 0.01$
Total systematic uncertainty	0.67	$\pm 0.04$



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Broad range of applications



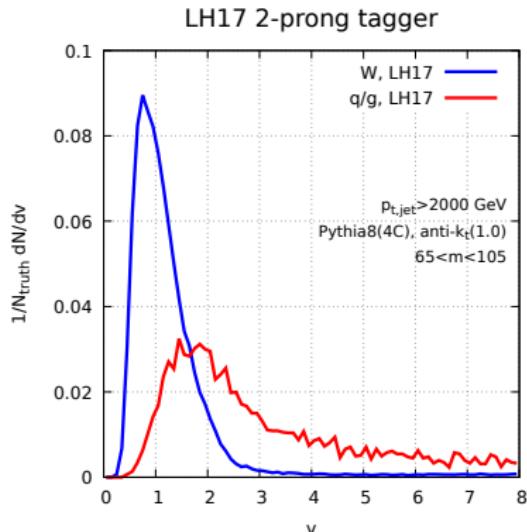
Searches



Measurements  
& modelling



Pheno  
studies



Long list of applications:

- New tools & observables (incl. substructure)
- Comparison to analytics
- Comparison to data
- BSM models

# What do Event Generators provide?

Broad range of applications



Searches



Measurements  
& modelling



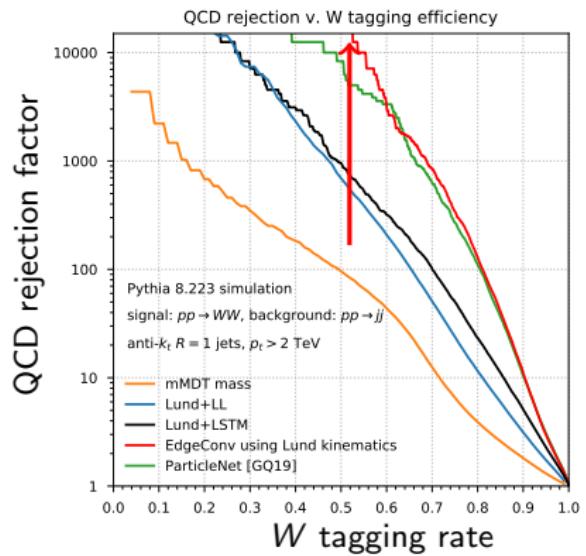
Pheno  
studies



Machine  
learning

- Deep Learning increasingly used at the LHC
- Shows interesting performance
- Example: boosted  $W \rightarrow q\bar{q}$  v. QCD jet
- Training often done on MCs.

[plot from Frederic Dreyer]

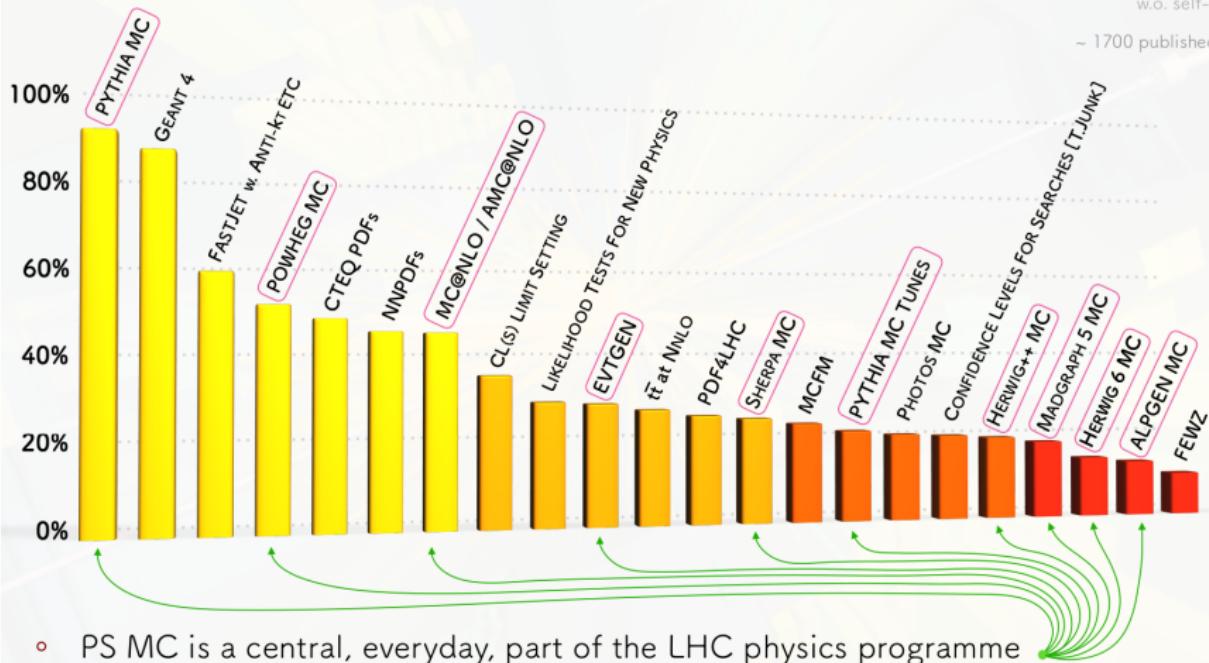


# Event Generators are among us!

- % of ATLAS+CMS+LHCb papers citing some article/group in Jan '14 → May '20

w.o. self-citations

~ 1700 published articles



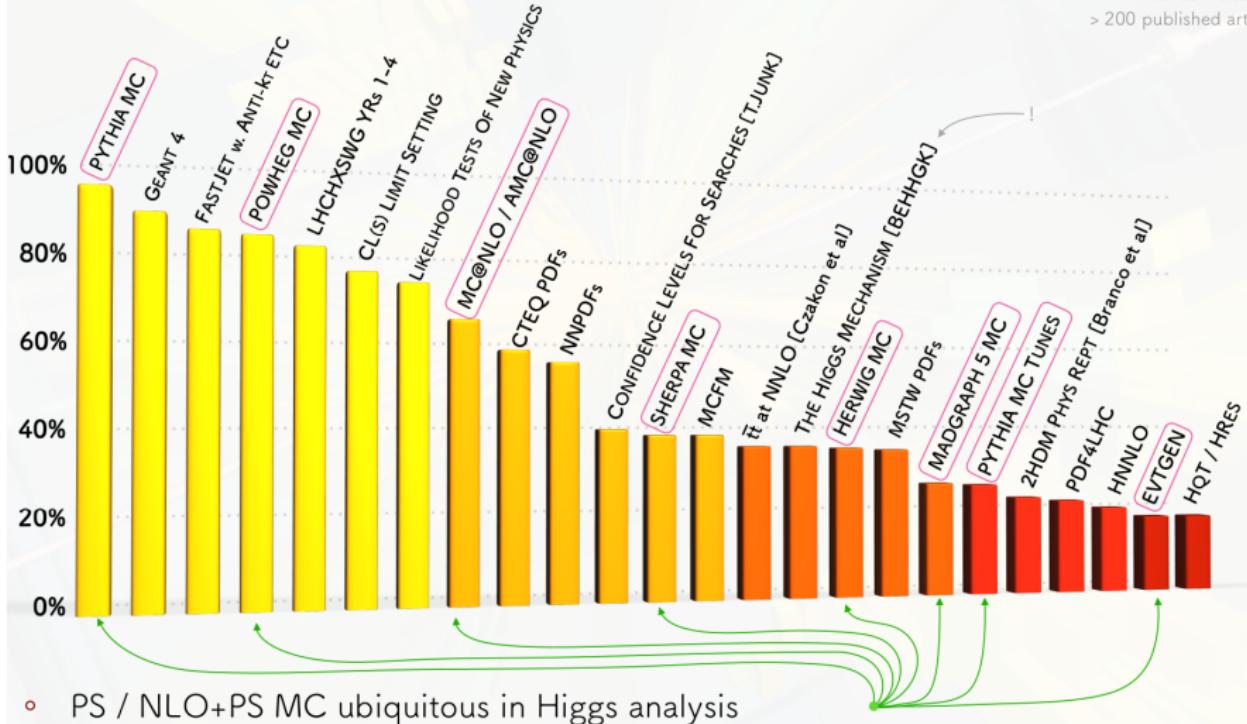
- PS MC is a central, everyday, part of the LHC physics programme

Both “fixed-order” and “parton-shower/all-purpose” generators

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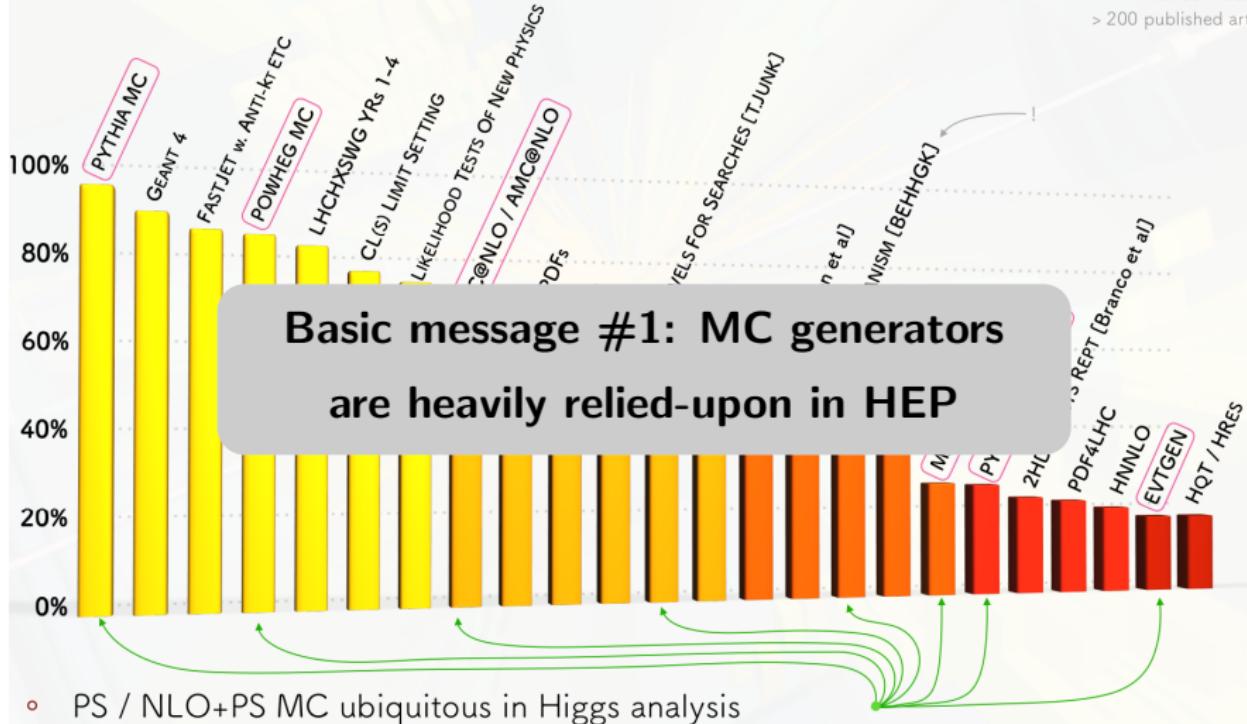
- PS / NLO+PS MC ubiquitous in Higgs analysis

[thanks to Keith Hamilton]

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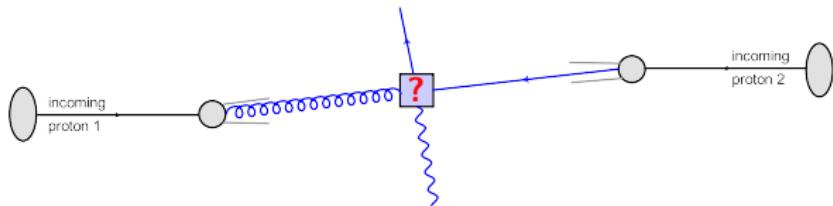
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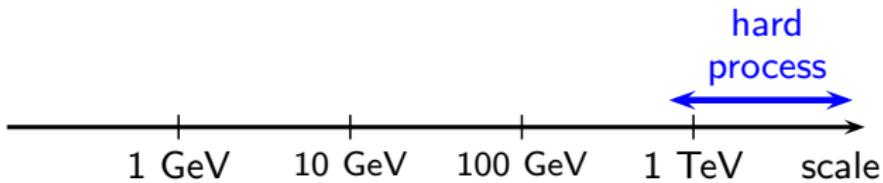
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# Anatomy of a high-energy collision

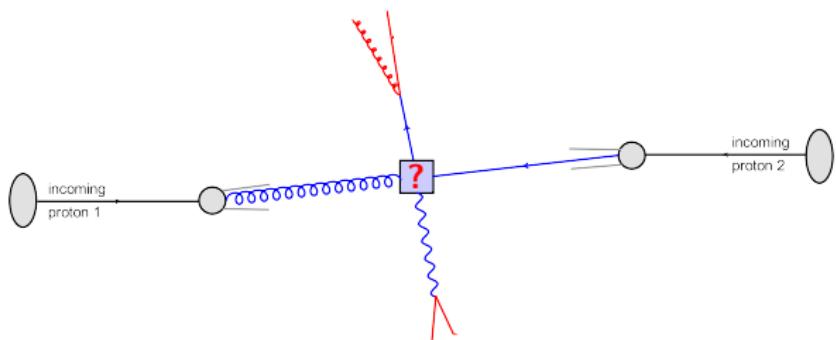


Simulating a high-energy collision requires several ingredients

- A hard process

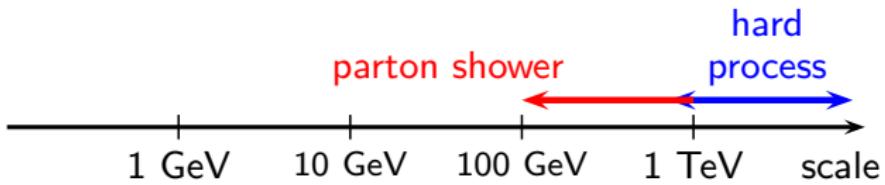


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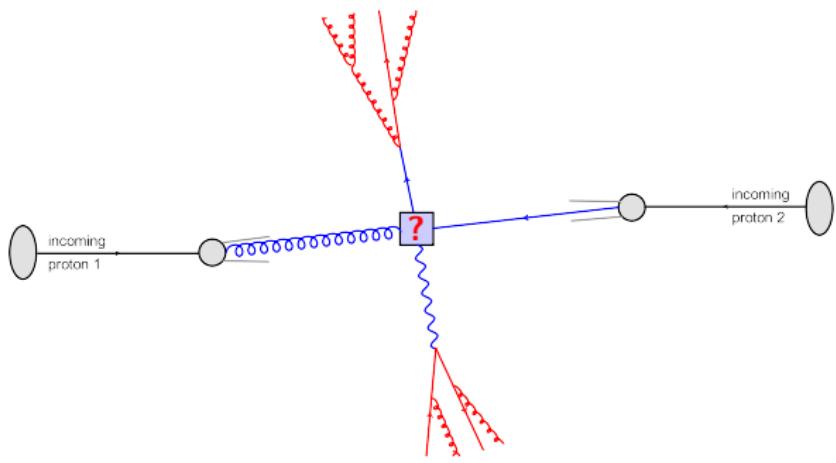


Simulating a high-energy collision requires several ingredients

- A hard process
- Parton shower (initial and final-state)

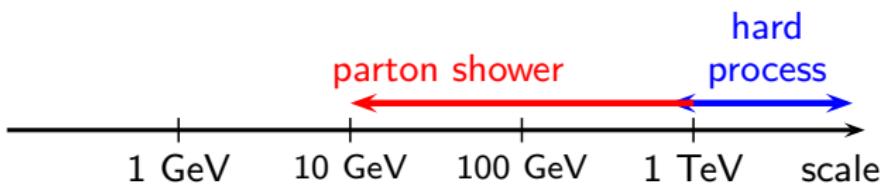


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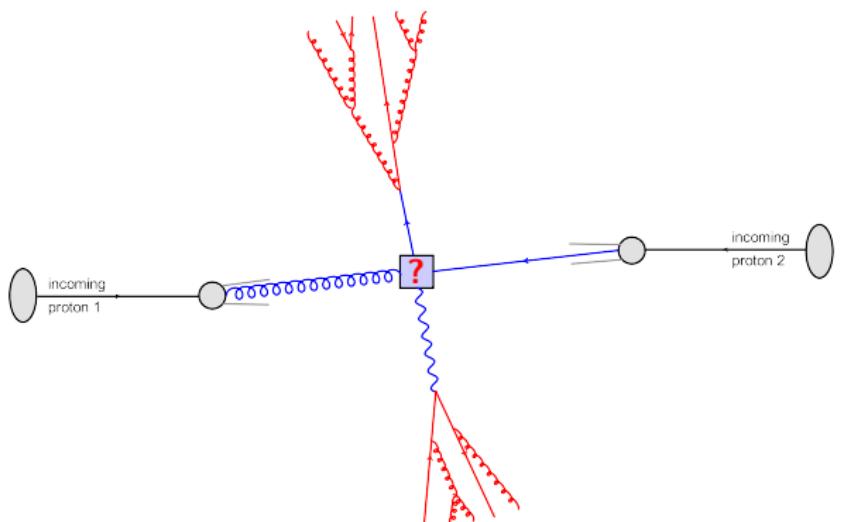


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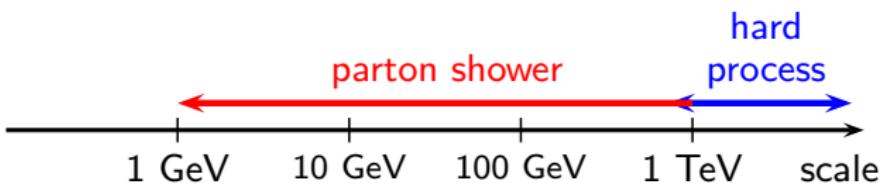


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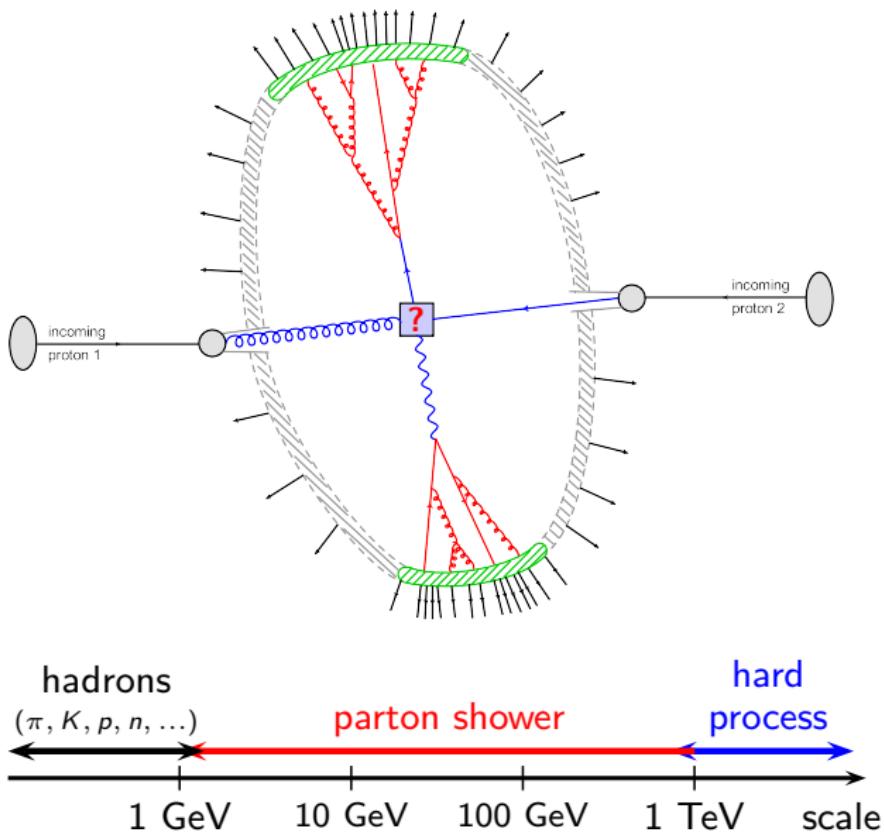


Simulating a high-energy collision requires several ingredients

- A hard process
- Parton shower (initial and final-state)
- Hadronisation



# Anatomy of a high-energy collision

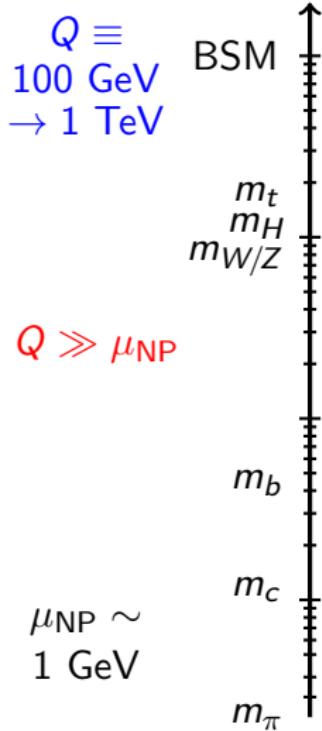


Simulating a high-energy collision requires several ingredients

- A hard process
- Parton shower (initial and final-state)
- Hadronisation
- Multi-parton interactions
- ...

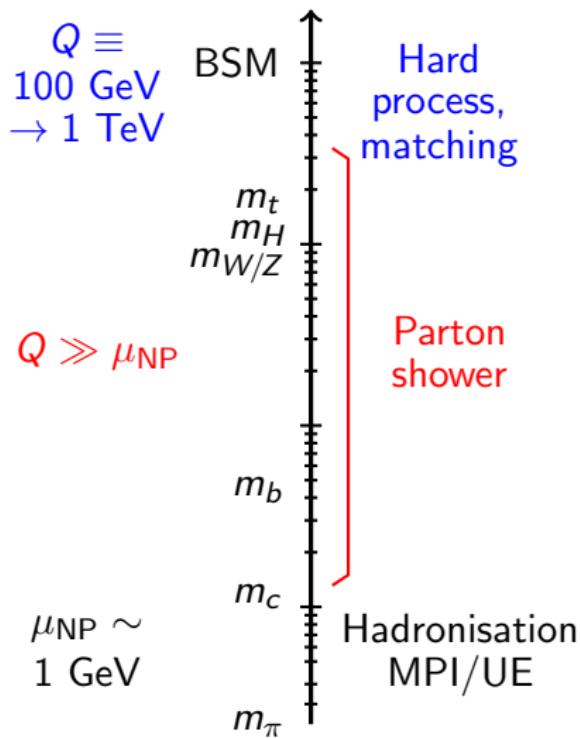
# Basic message #2: physics at all scales

LHC probes physics across many scales



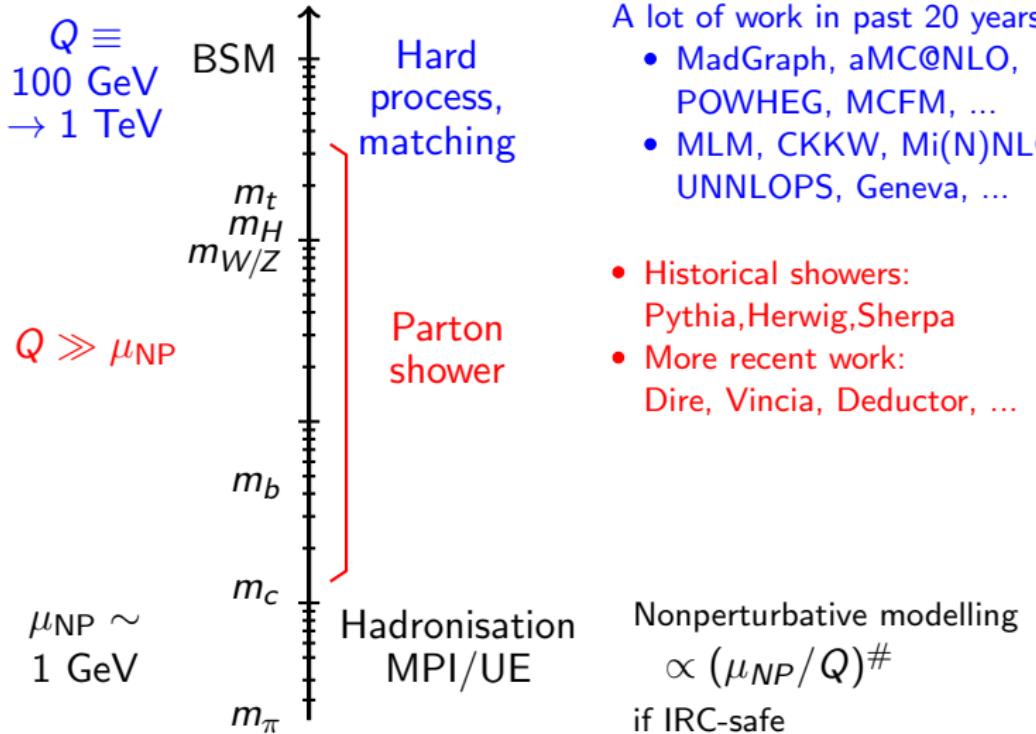
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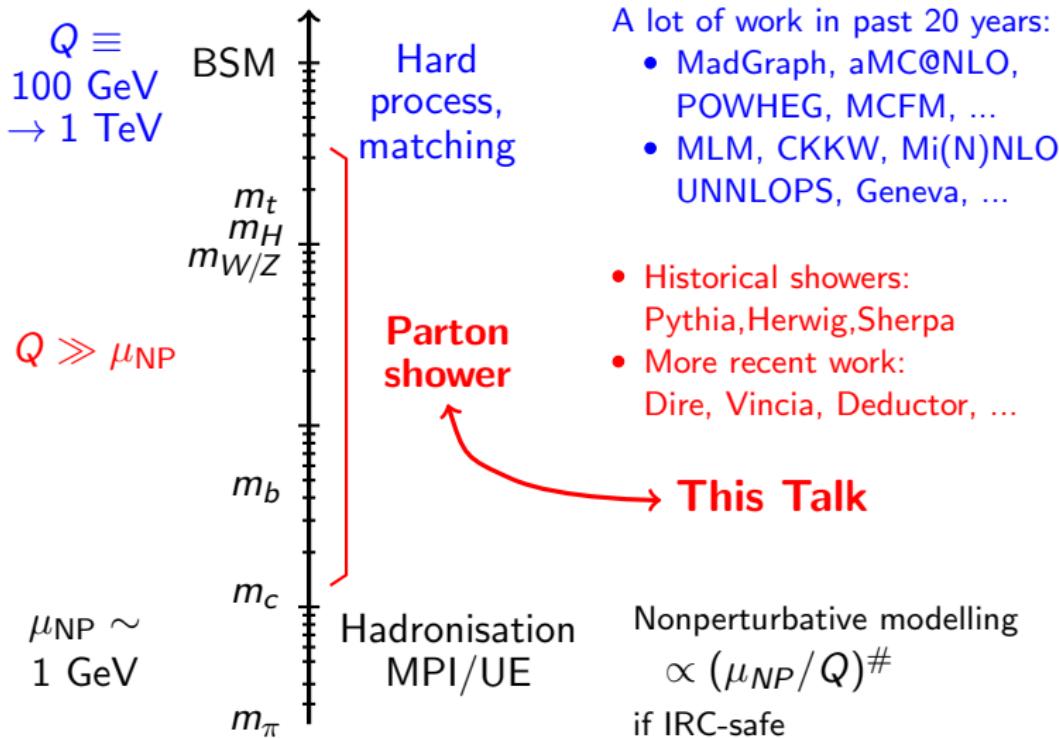
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# Need for precision

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LHC increasingly goes into precision  
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precise  
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Amplitudes  
NNLO, ...  
(+resummations)



deep learning  
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A key question in this talk: accuracy of parton showers?

Beware!

each part/component of the "simulation" has  
its own capabilities/limitations and its own accuracy

# How do parton showers work?

# Dipole/Antenna showers: ingredients

Many showers (Pythia, Sherpa, Vincia, Dire, ...) are  
**dipole/antenna** showers (main exception: Herwig)

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Idea #1:

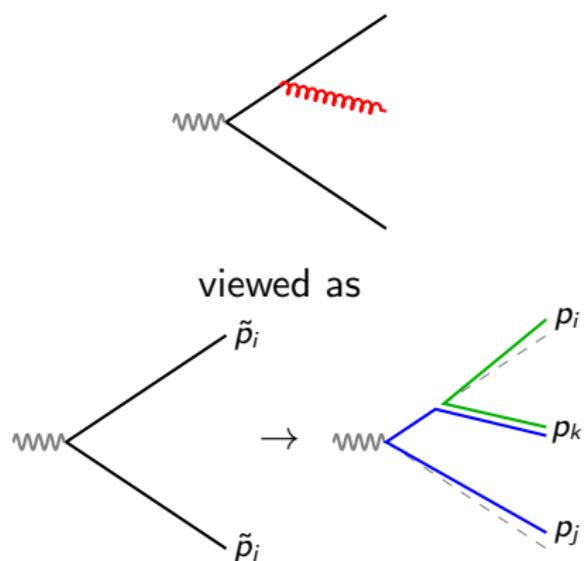
gluon emission  $\equiv$  dipole splitting

$$(ij) \rightarrow (ik)(kj)$$

- captures the soft/collinear limits
- key ingredient: mapping

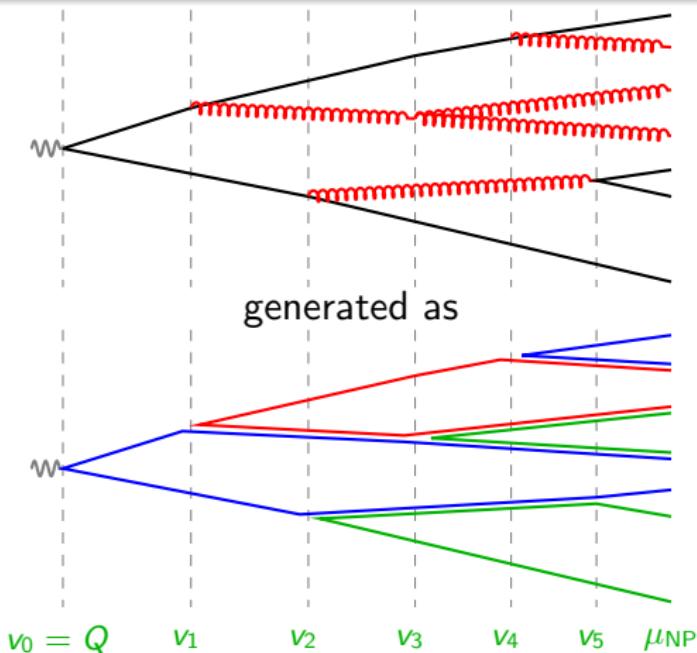
$$\underbrace{\tilde{p}_i, \tilde{p}_j}_{\text{before split}} \rightarrow \underbrace{p_i, p_j, p_k}_{\text{after split}}$$

includes recoil  
& energy-mom conservation



# Dipole/Antenna showers: ingredients

Many showers (Pythia, Sherpa, Vincia, Dire, ...) are **dipole/antenna** showers (main exception: Herwig)



Idea #2:

iterate dipole splittings  
(populate the full phase space with multiple emissions)

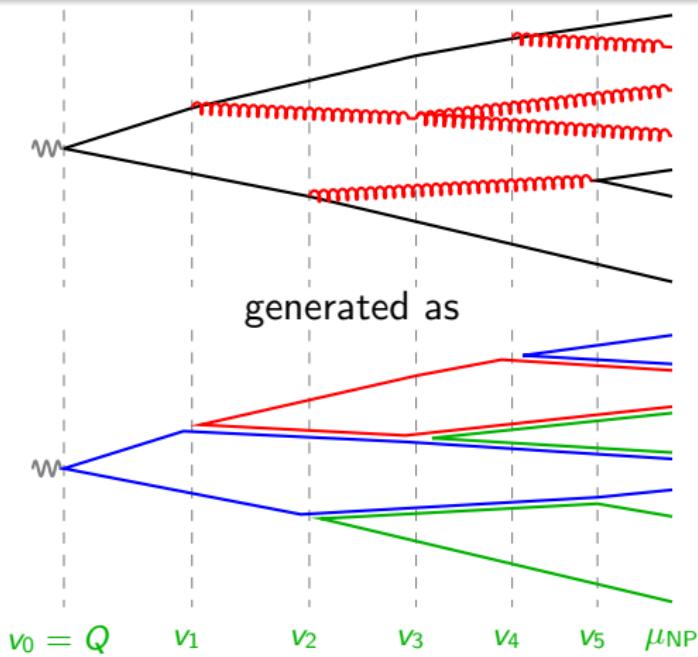
Rooted in QCD factorisation

$$P_{n+1}(v_{n+1})$$

$$= e^{-\Delta_n(v_0, v)} |M^2|(v) P_n(v_n)$$

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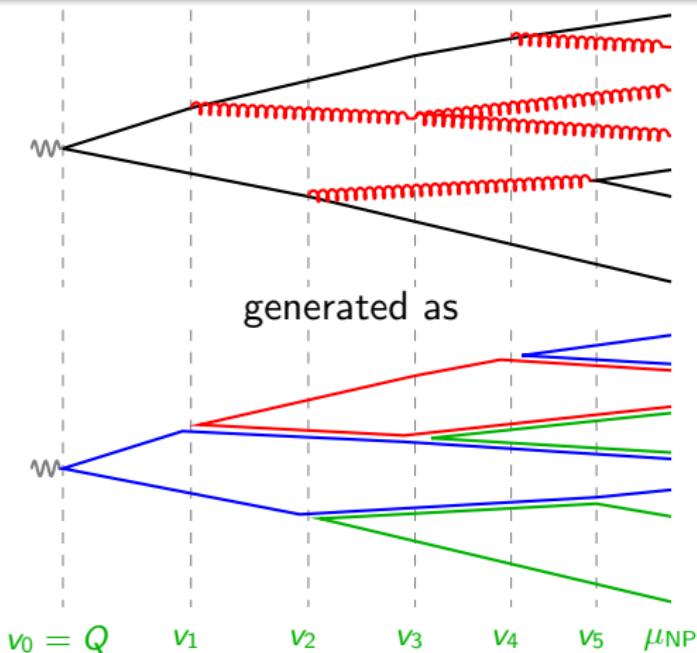
Rooted in QCD factorisation

$$P_{n+1}(v_{n+1}) = e^{-\Delta_n(v_0, v)} |M^2|(v) P_n(v_n)$$

↗ *n, n + 1 particles probabilities*  
 ↘ *Sudakov*  
 ↘ *"no emissions"*  
 ↘ *(virtuals)*  
 ↗ *real emission*

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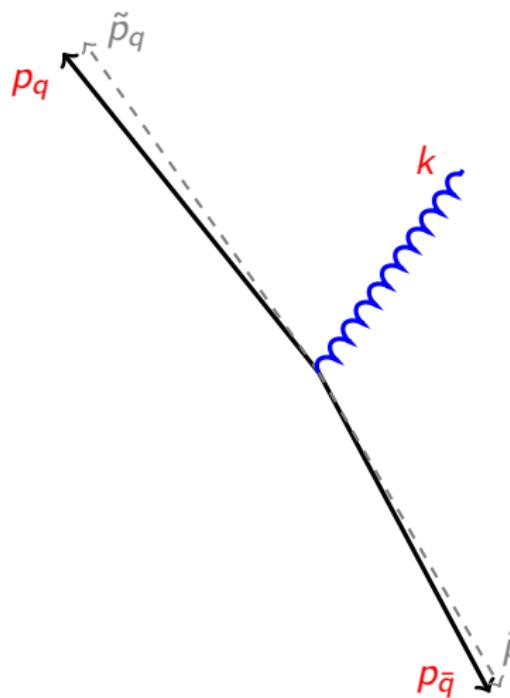
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Several challenges:

- ordering variable
- beyond large/leading- $N_c$
- treat recoil properly
- assess/improve accuracy

# Basic features of QCD radiations

Take a gluon emission from a ( $q\bar{q}$ ) dipole



Emission  $(\tilde{p}_q \tilde{p}_{\bar{q}}) \rightarrow (p_q k)(k p_{\bar{q}})$ :

$$k^\mu \equiv z_q \tilde{p}_q^\mu + z_{\bar{q}} \tilde{p}_{\bar{q}}^\mu + k_\perp^\mu$$

3 degrees of freedom:

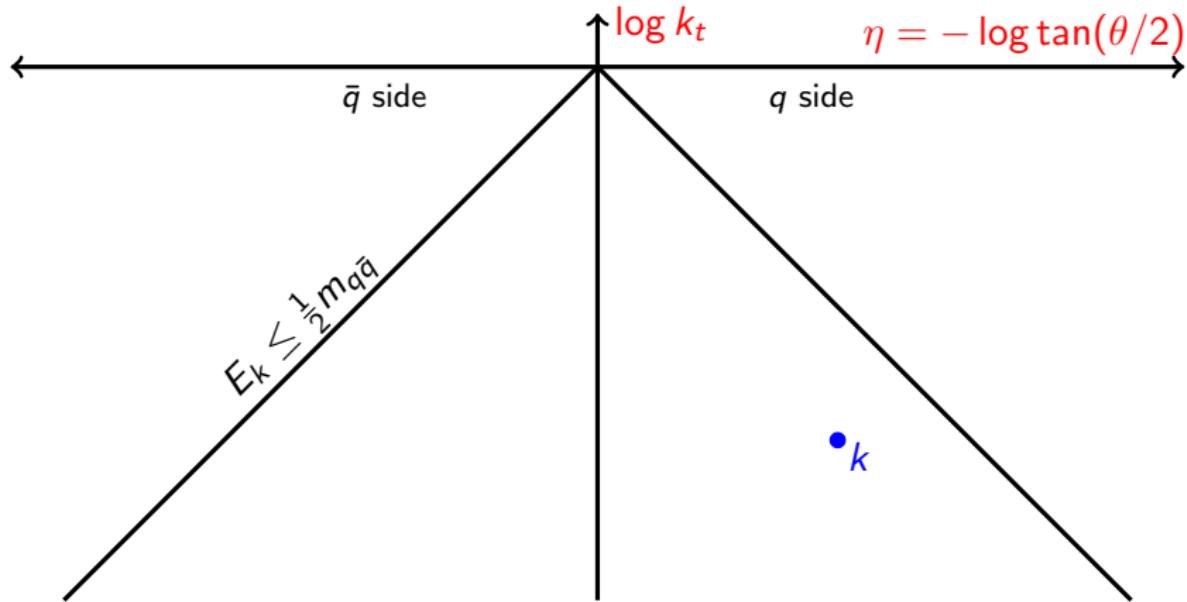
- Rapidity:  $\eta = \frac{1}{2} \log \frac{z_q}{z_{\bar{q}}}$
- Transverse momentum:  $k_\perp$
- Azimuth:  $\phi$

In the soft-collinear approximation

$$d\mathcal{P} = \frac{\alpha_s(k_\perp) C_F}{\pi^2} d\eta \frac{dk_\perp}{k_\perp} d\phi$$

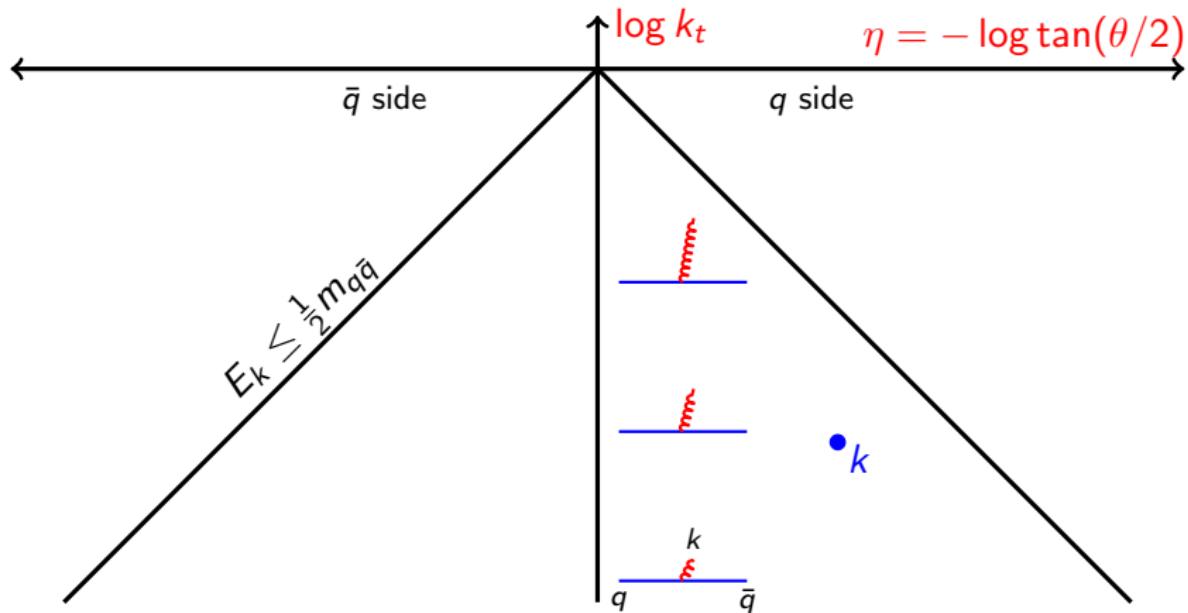
# Basic features of QCD radiations: the Lund plane

Lund plane: natural representation uses the 2 “log” variables  $\eta$  and  $\log k_\perp$



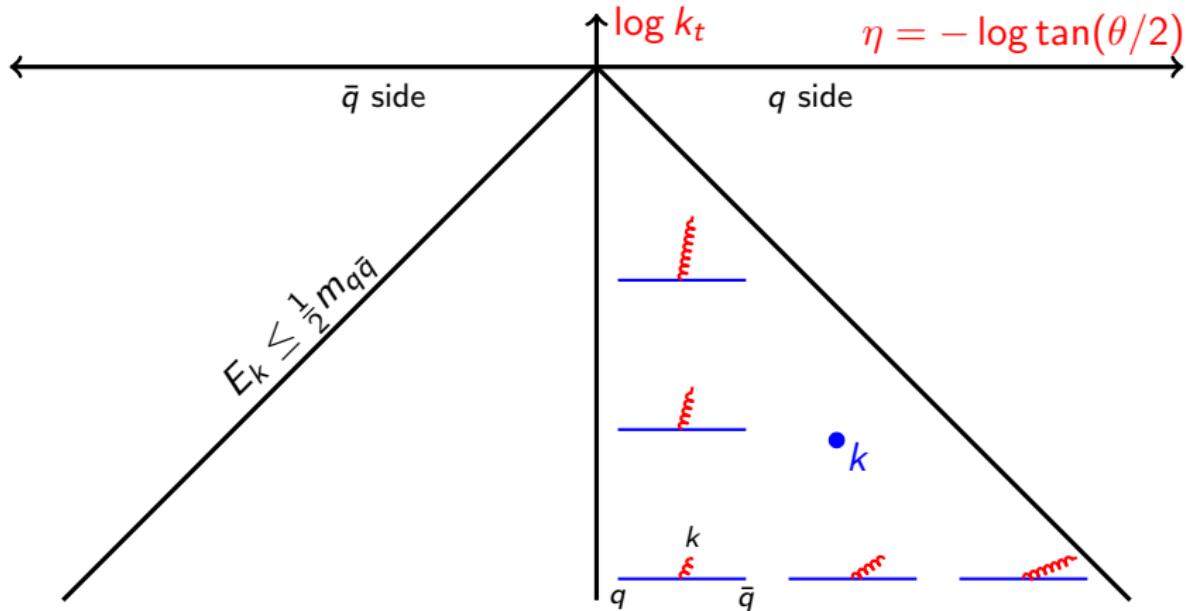
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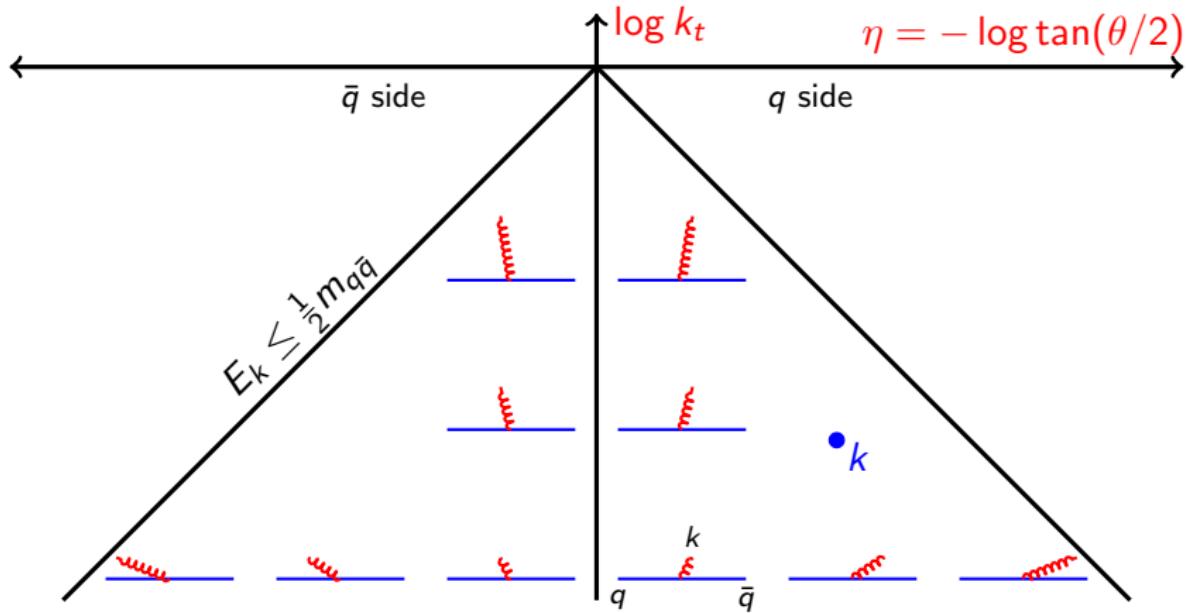
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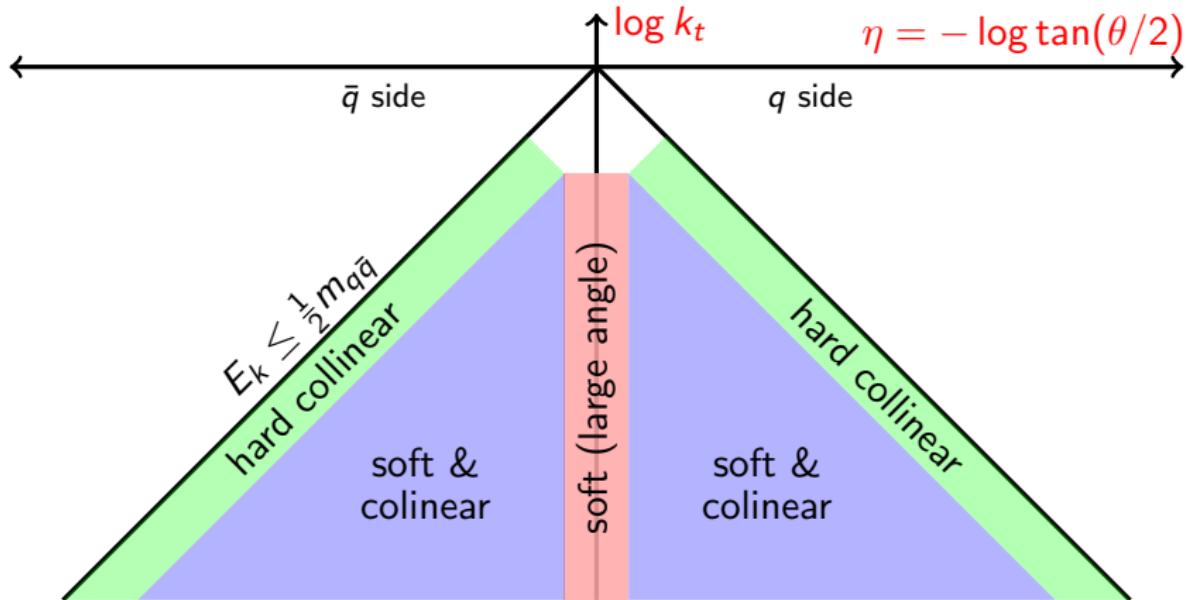
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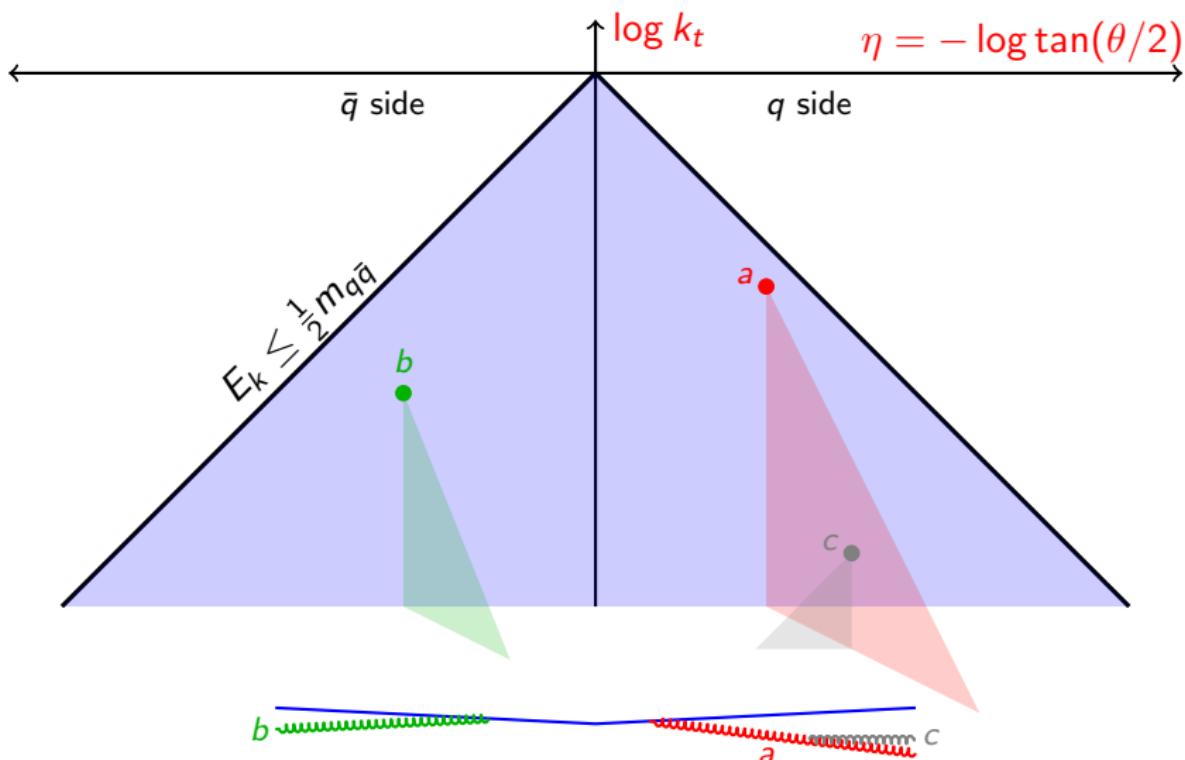


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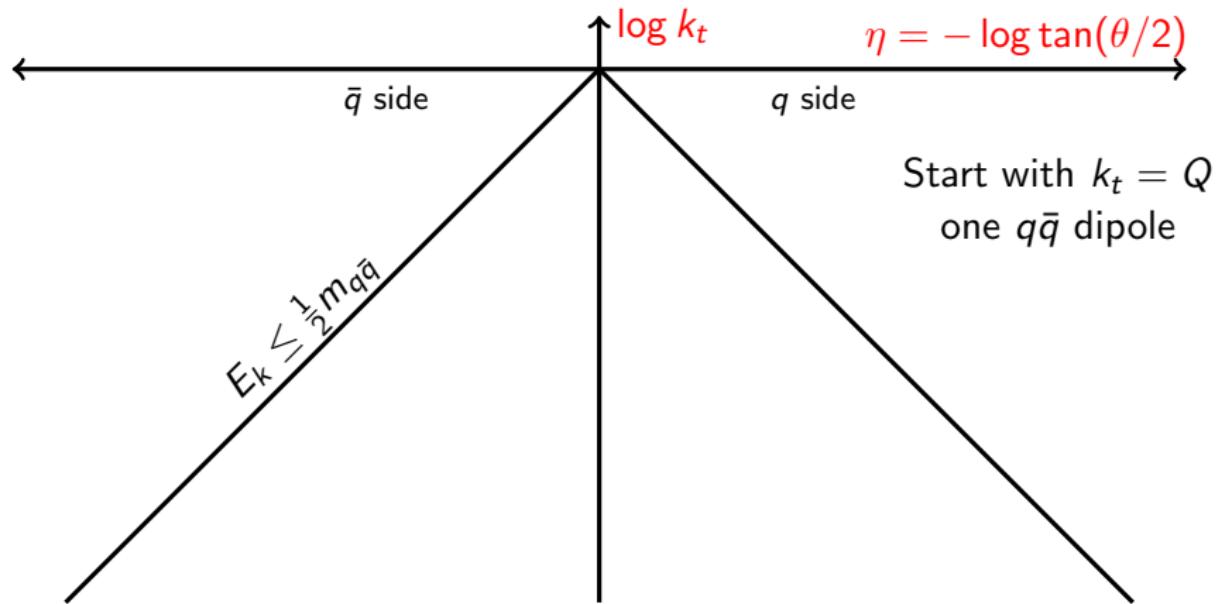


# Multiple emissions in the Lund plane



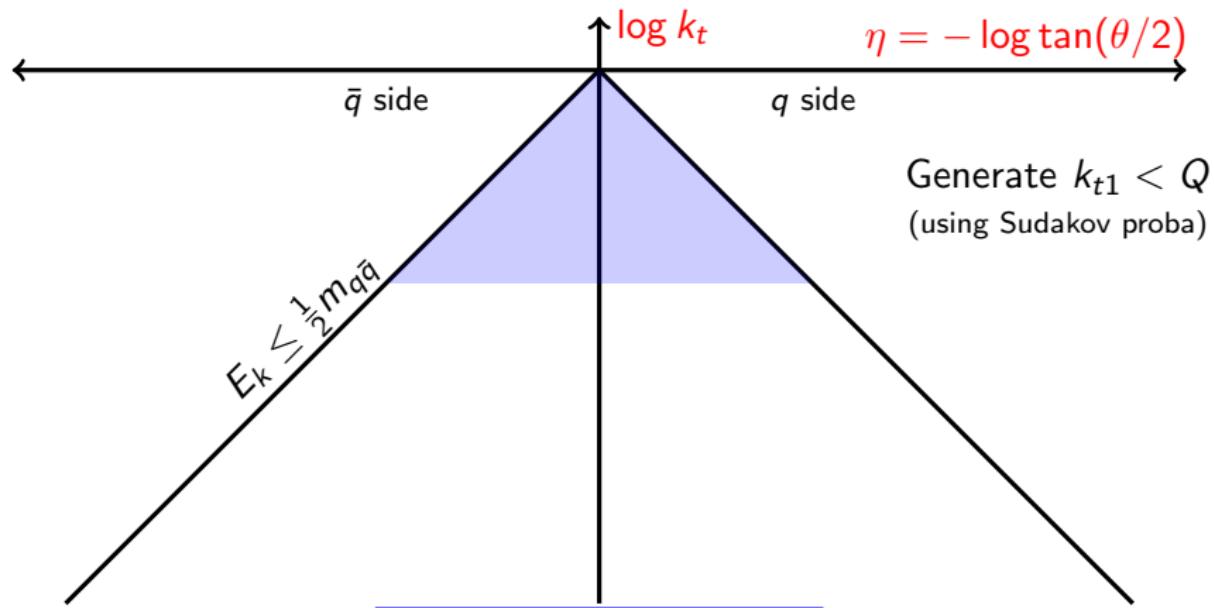
# Parton shower in the Lund plane

Ordering variable: transverse momentum  $k_t$



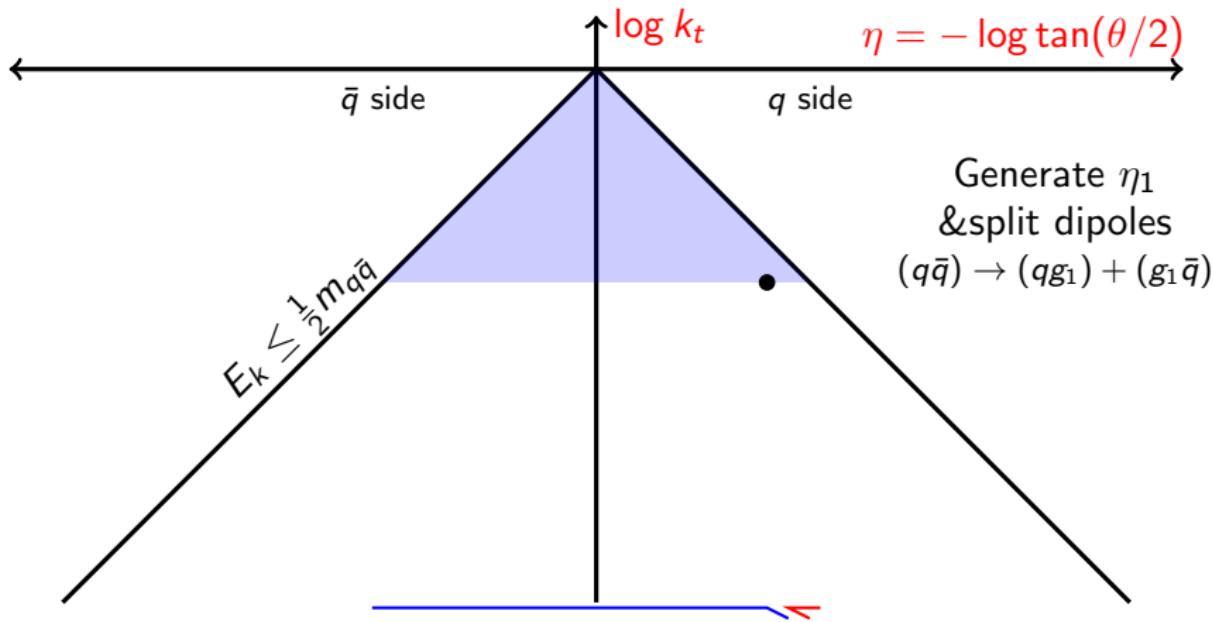
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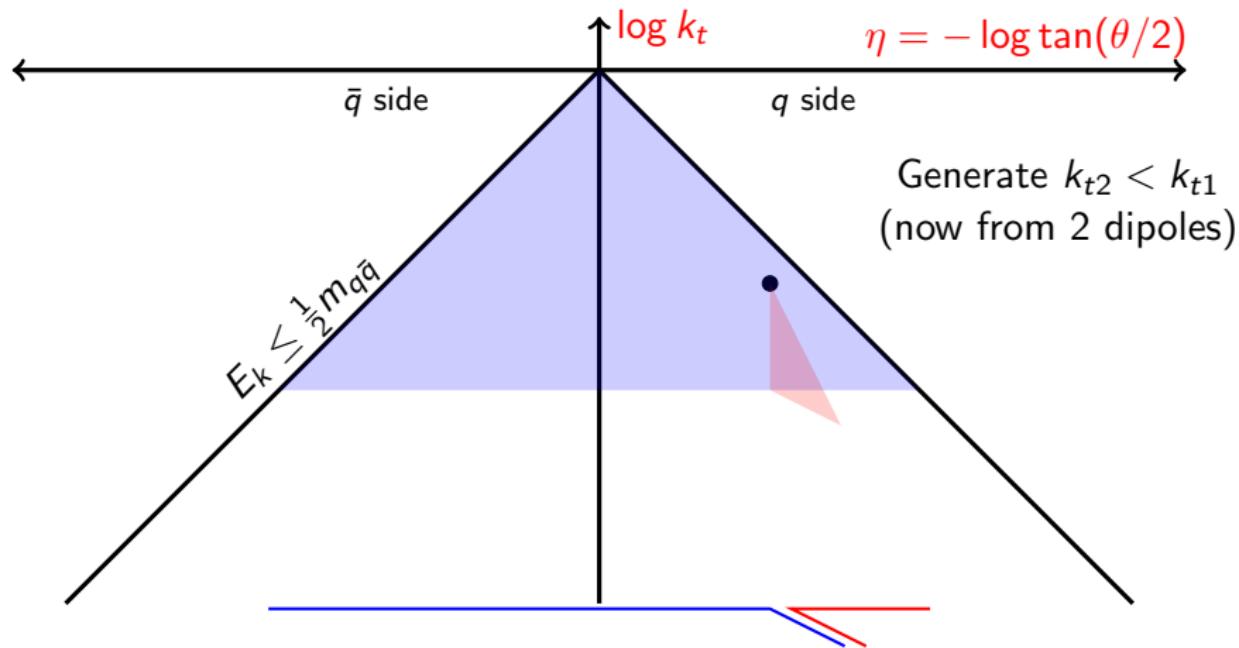
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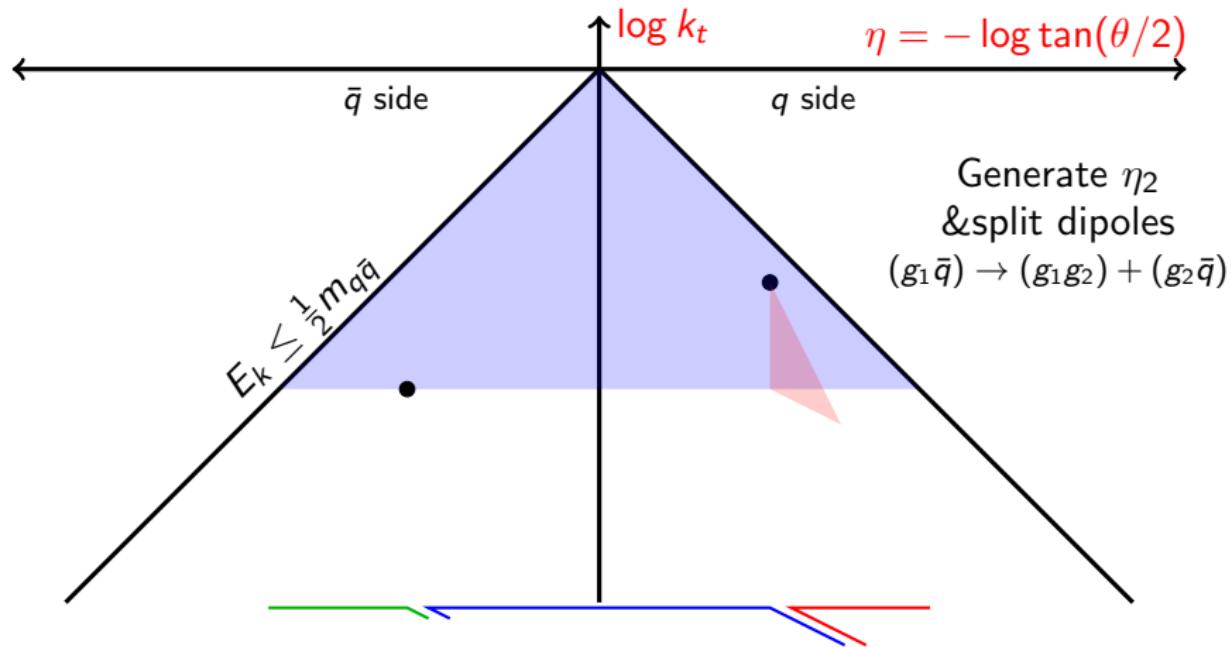
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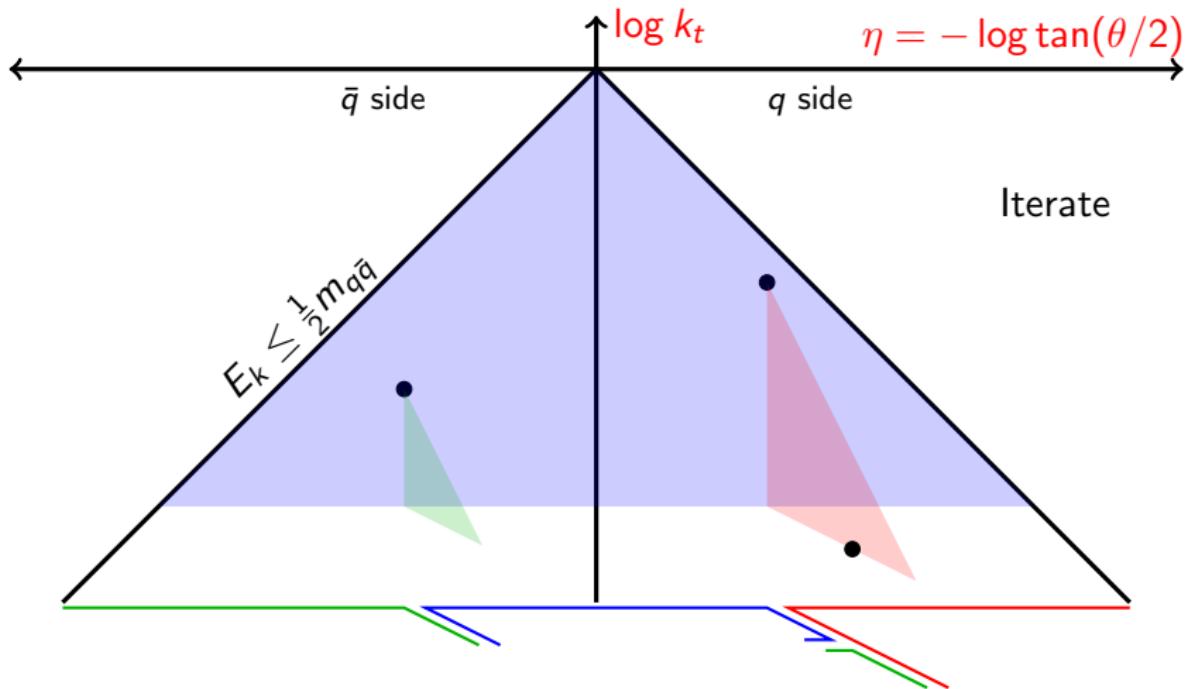
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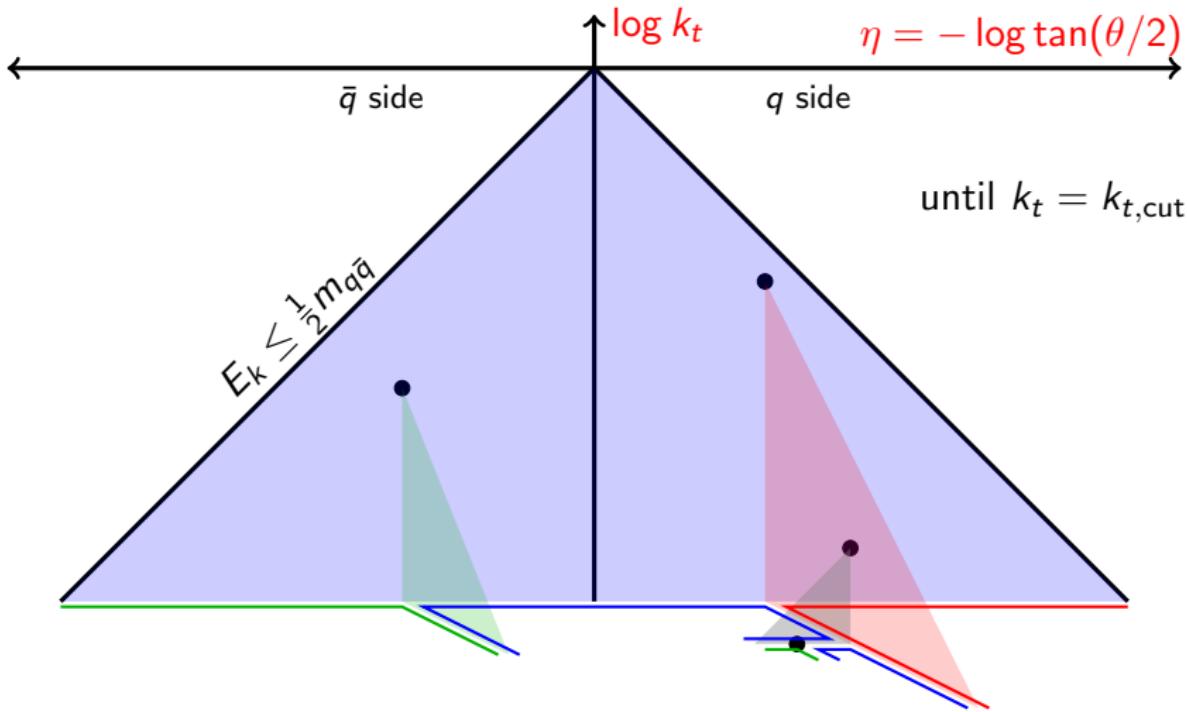
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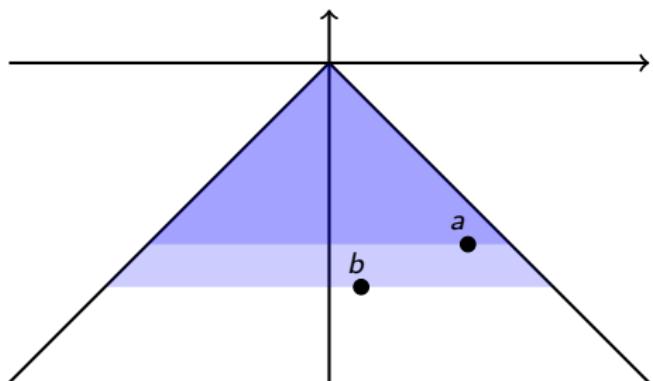
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# Different ordering variables...

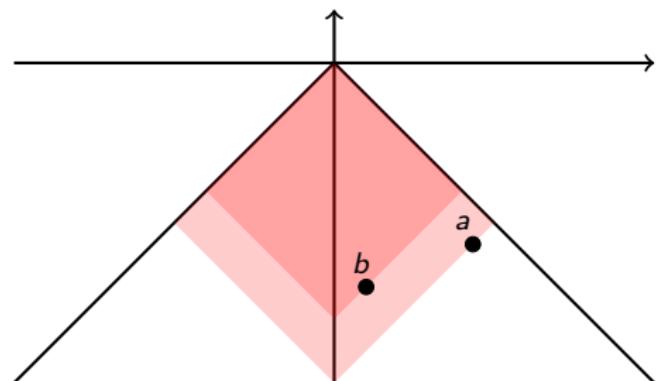
... can lead to different emission orderings

$k_t$  (transv. mom.) ordering



$$k_{ta} > k_{tb}$$
$$\Rightarrow a \text{ emitted before } b$$

$q$  (virtuality) ordering



$$q_b > q_s$$
$$\Rightarrow b \text{ emitted before } a$$

# (a glimpse at) recent progress?

# $1 \rightarrow 3$ splitting functions

Idea

ingredients towards NLO DGLAP

- ▶ Implements  $1 \rightarrow 3$  splittings  
 $2 \rightarrow 4$  in terms of dipoles
- ▶ Example: Dire(v2)

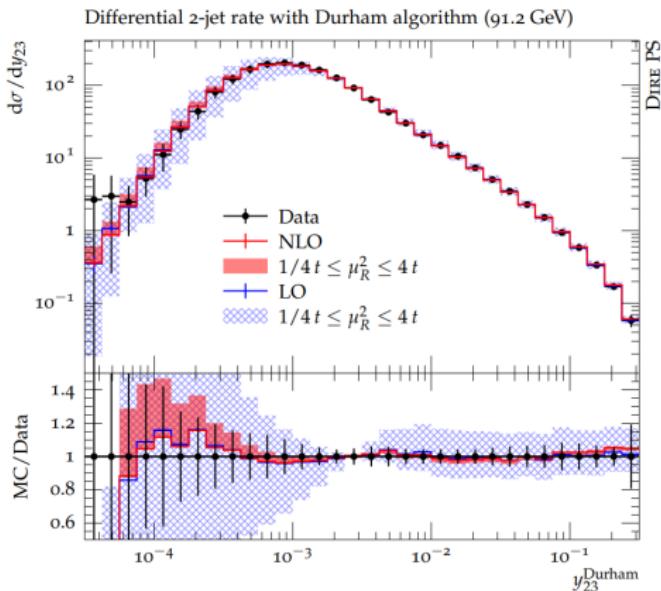
See e.g.

[Jadach *et al*,16]

[Li,Skands,16]

[Höche,Krauss,Prestel,17]

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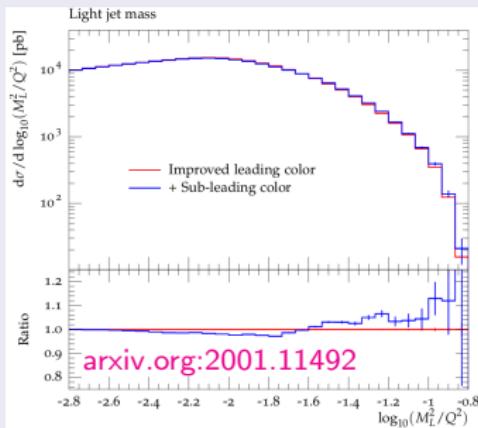
# Beyond leading colour

## Challenges

- most showers (except Herwig) are leading colour (even at leading-log) (see e.g. [Dasgupta,Dreyer,Hamilton,Monni,Salam,18])
- very complex structure for multiple soft-gluon emissions

## Recent progress

- Amplitude-level showers  
in contrast to approached based  
on squared matrix-elements  
see e.g. [Forshaw,Holguin,Plätzer,19]
- Beyond leading- $N_c$ /full colour  
see e.g. [Nagy,Soper,12],[Höche,Reichelt,20],  
[Gieseke,Kirchgaesser,Plätzer,Siodmok,18],  
[Forshaw,Holguin,Plätzer,20]



# Electroweak showers

## Main challenges

- Splitting functions more involved than standard Altarelli-Parisi
- Explicit dependence on chirality/spin<sup>(\*)</sup>

## Recent progress

Implementation in Vincia, based on the spinor-helicity formalism

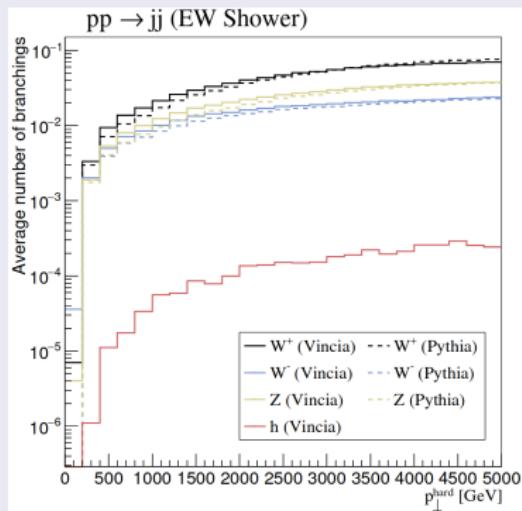
[Kleiss,Verheyen,20]

phenomenological relevance at large  $p_t$

see also:

[Bauer,Ferland,Webber,17-18]

[Bauer,DeJong,Nachman,Provasoli,19]

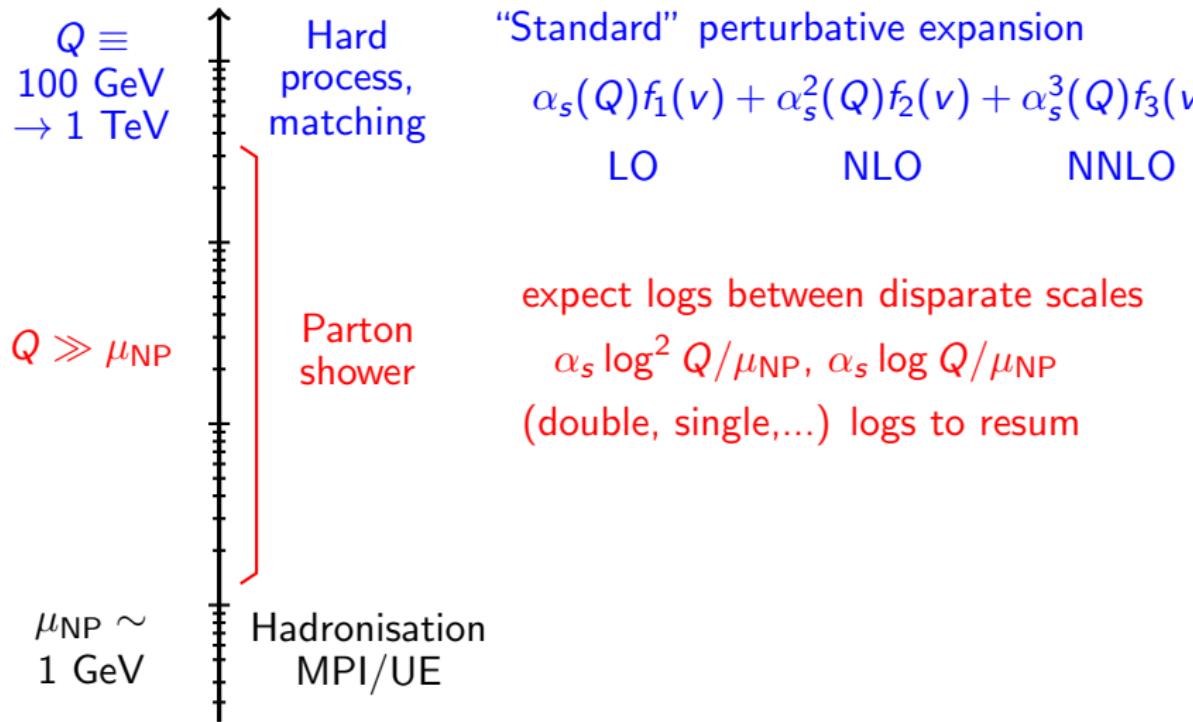


(\*) Technically, this is also the case for QCD showers

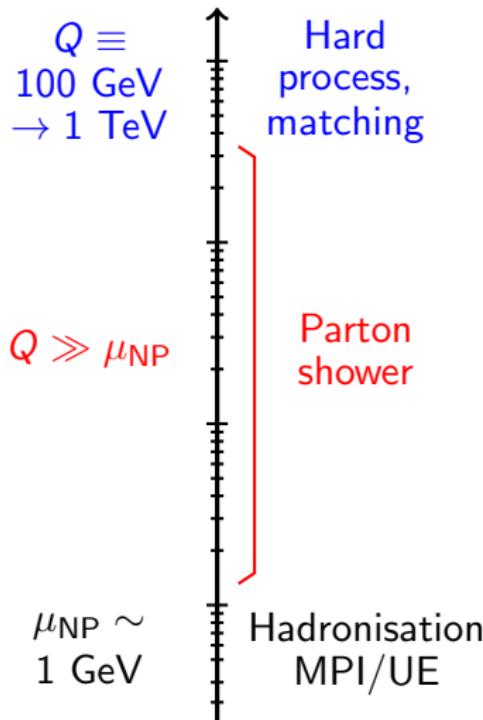
## Parton-shower accuracy?

[M.Dasgupta,F.Dreyer,K.Hamilton,P.Monni,G.Salam,GS,arXiv:2002:11114]

# What does shower accuracy mean?



# What does shower accuracy mean?



"Standard" perturbative expansion

$$\alpha_s(Q)f_1(v) + \alpha_s^2(Q)f_2(v) + \alpha_s^3(Q)f_3(v) + \dots$$

LO

NLO

NNLO

expect logs between disparate scales

$$\alpha_s \log^2 Q/\mu_{\text{NP}}, \alpha_s \log Q/\mu_{\text{NP}}$$

(double, single,...) logs to resum

**accuracy means logarithmic  
accuracy: LL, NLL,  $N^2\text{LL}$ , ...**

**well-defined  
+ systematically improvable**

# Testing shower accuracy

(Cumulative) distributions can (often) be written as

$$P(v < e^{-L}) = \exp \left[ \underbrace{g_1(\alpha_s L)L}_{\text{leading log}(LL)} + \underbrace{g_2(\alpha_s L)}_{\text{next-to-leading log}(NLL)} + \underbrace{g_3(\alpha_s L)\alpha_s}_{\text{NNLL}} + \dots \right]$$

Examples:

- Thrust  $T = \max_{|\vec{u}|=1} \frac{\sum_i |\vec{p}_i \cdot \vec{u}|}{\sum_i |\vec{p}_i|}$
- Cambridge  $y_{23}$  ( $\approx$  largest  $k_t$  in an angular-ordered clustering)
- angularities
- ...

# Testing shower accuracy

(Cumulative) distributions can (often) be written as

$$P(v < e^{-L}) = \exp \left[ \underbrace{g_1(\alpha_s L)L}_{\text{leading log}(LL)} + \underbrace{g_2(\alpha_s L)}_{\text{next-to-leading log}(NLL)} + \underbrace{g_3(\alpha_s L)\alpha_s}_{\text{NNLL}} + \dots \right]$$
$$\mathcal{O}(1/\alpha_s) \quad \mathcal{O}(1) \quad \mathcal{O}(\alpha_s)$$

in resummation regime:

$$\alpha_s \ll 1, \quad L \gg 1, \quad \lambda \equiv \alpha_s L \sim 1$$

We should control at least  $\mathcal{O}(1)$  contributions

# Our targeted accuracy

## NLL accuracy for a range of observables

- global event shapes

- ▶ thrust
- ▶ jet rates
- ▶ angularities
- ▶ broadening
- ▶ ...

- non-global  
observables

e.g. energy in slice

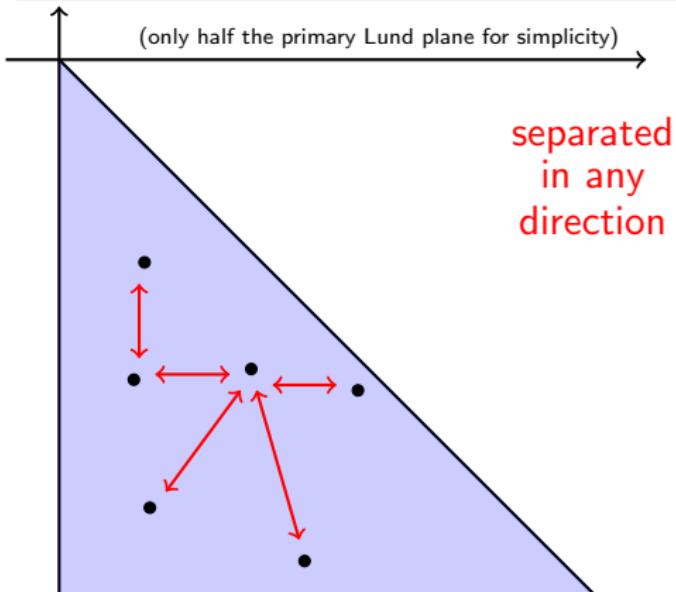
- multiplicity  
(NLL is  $\alpha_s^n L^{2n-1}$ )

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## Correct matrix elements for $N$ well separated emissions in the Lund plane

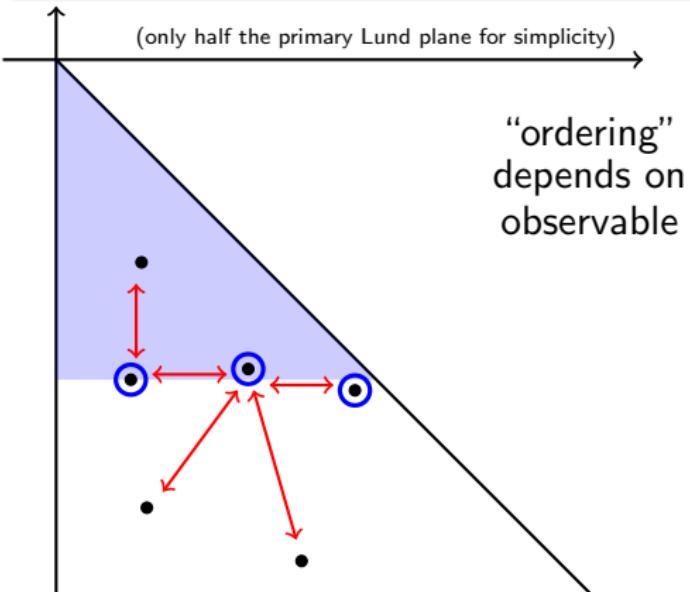


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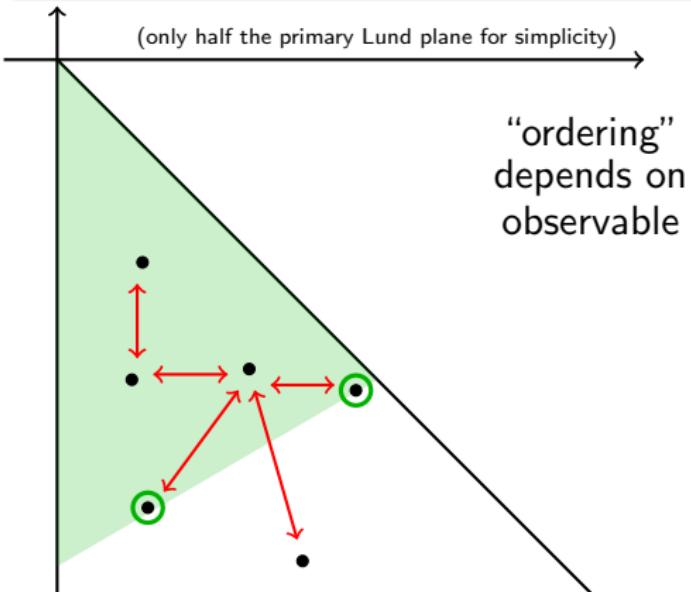


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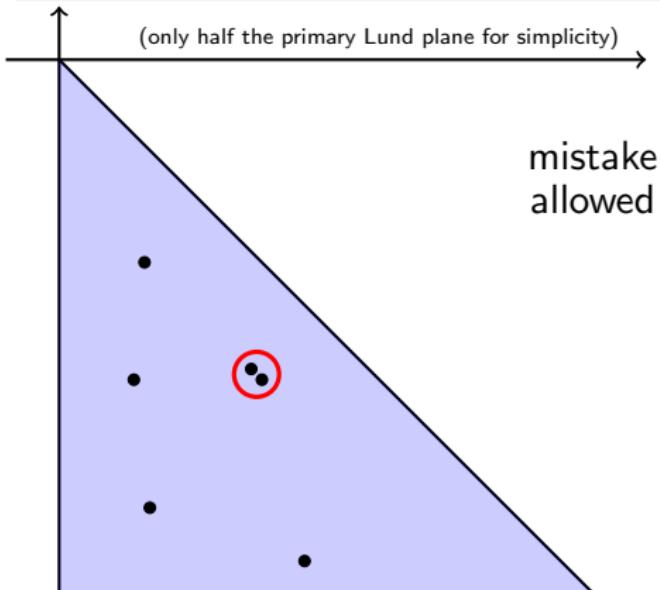


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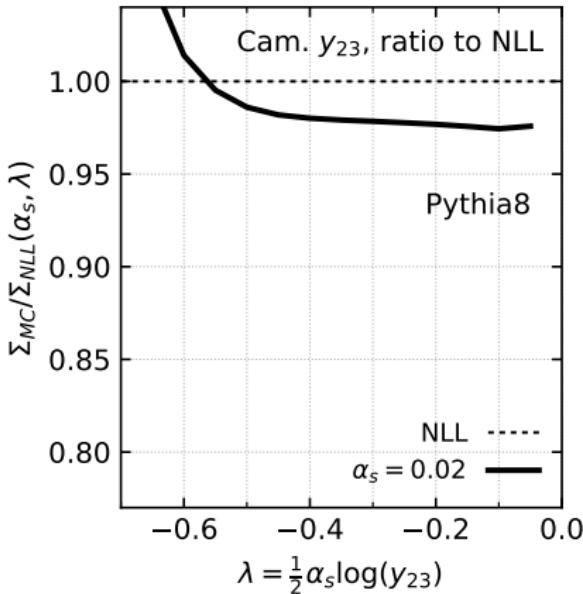
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## Correct matrix elements for $N$ well separated emissions in the Lund plane



# Testing accuracy



Idea for testing:

$$\frac{\sum_{MC}(\lambda=\alpha_s L, \alpha_s)}{\sum_{NLL}(\lambda=\alpha_s L, \alpha_s)} \text{ v. } 1$$

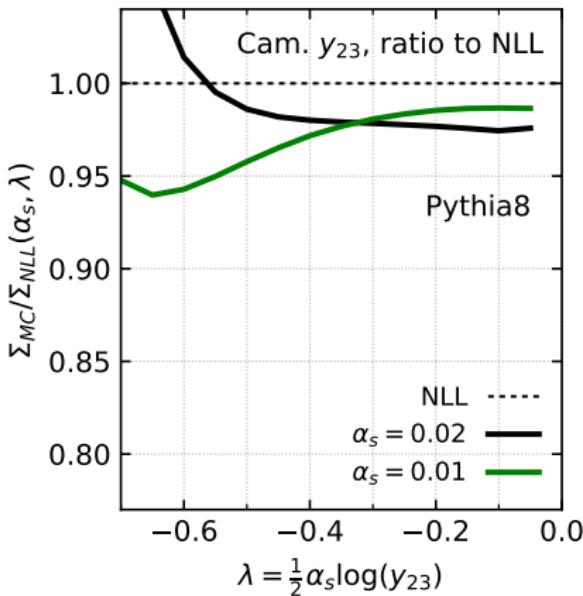
with  $\lambda = \alpha_s L$

NLL deviations

or

subleading effects?

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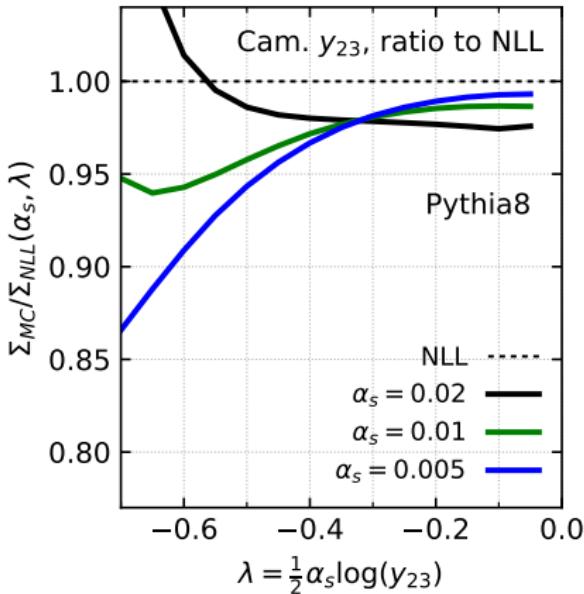
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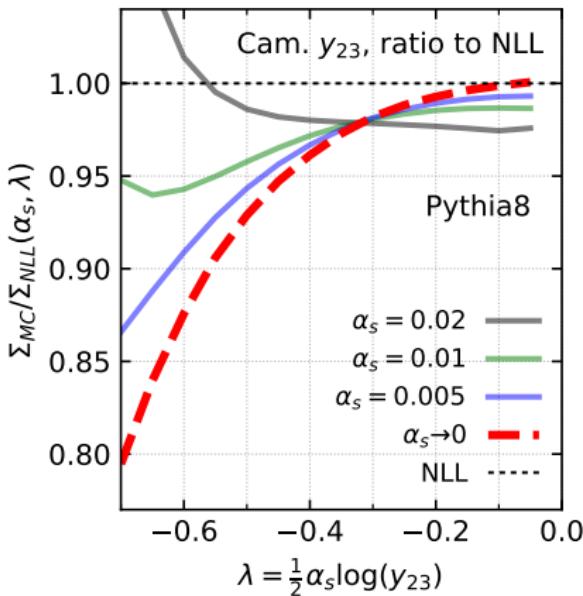
with  $\lambda = \alpha_s L$

NLL deviations

or

subleading effects?

# Testing accuracy



Idea for testing:

$$\frac{\sum_{MC}(\lambda=\alpha_s L, \alpha_s)}{\sum_{NLL}(\lambda=\alpha_s L, \alpha_s)} \xrightarrow{\alpha_s \rightarrow 0} 1$$

at fixed  $\lambda = \alpha_s L$

NLL deviations

or

~~subleading effects?~~

# Towards NLL accuracy with the PanScales showers

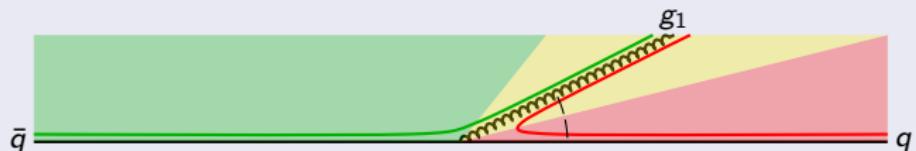
[M.Dasgupta,F.Dreyer,K.Hamilton,P.Monni,G.Salam,arXiv:2002:11114]

# PanScales showers

[M.Dasgupta,F.Dreyer,K.Hamilton,P.Monni,G.Salam,GS,20]

Key element 1: how to associate colour and transverse recoil to dipoles?

Expected rad<sup>n</sup>  
from  $q g_1 \bar{q}$   
 $[(q g_1) + (g_1 \bar{q})]$

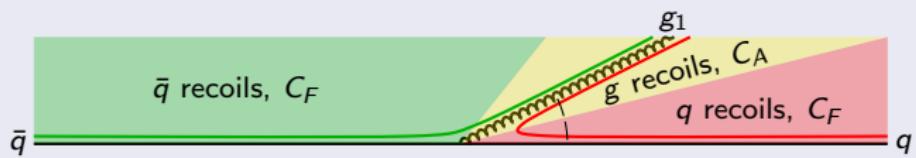


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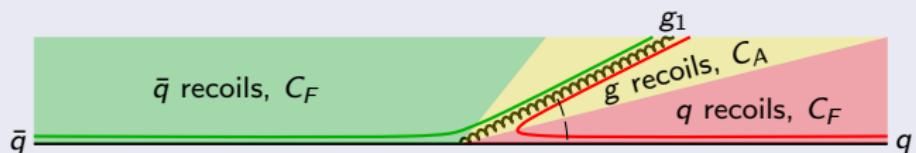


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Pythia:

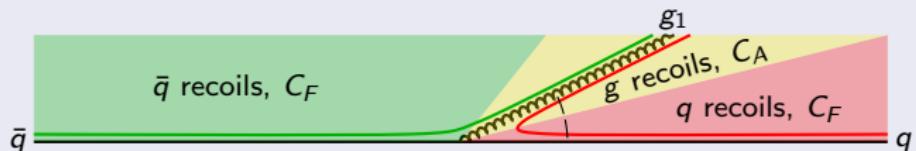


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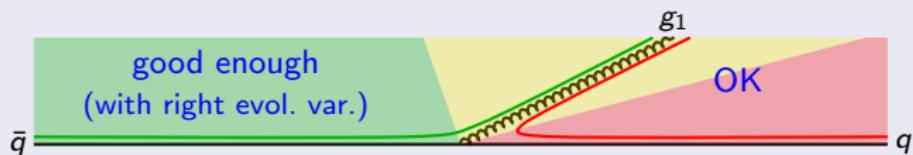
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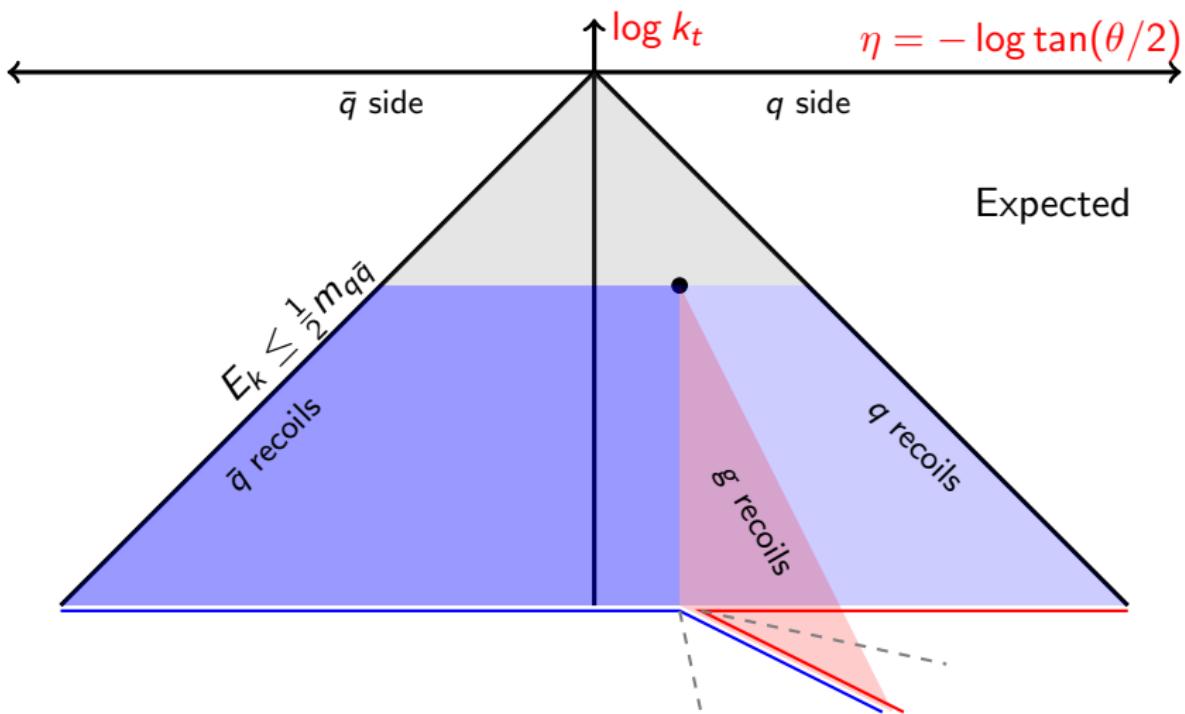


Key element 2: choice of evolution variable

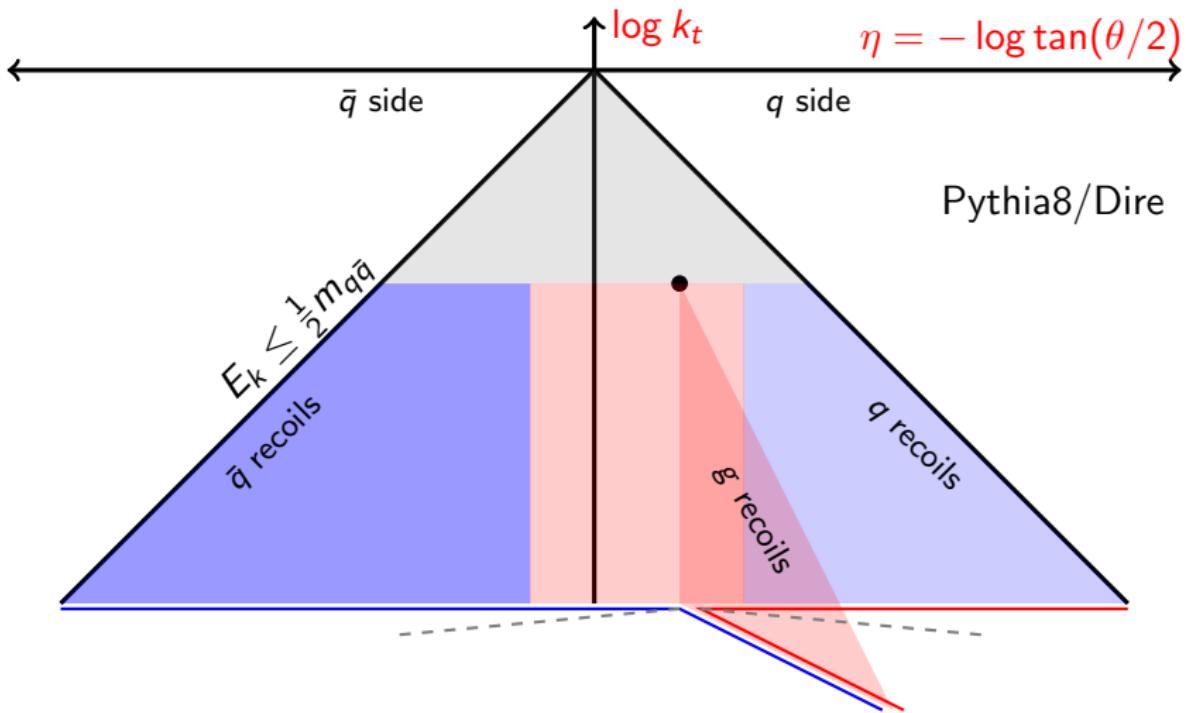
$$v \sim k_{t,ik} \theta_{ik}^\beta \quad (0 < \beta < 1)$$

Idea: emissions with commensurate  $k_t$   
radiated with successively smaller angles

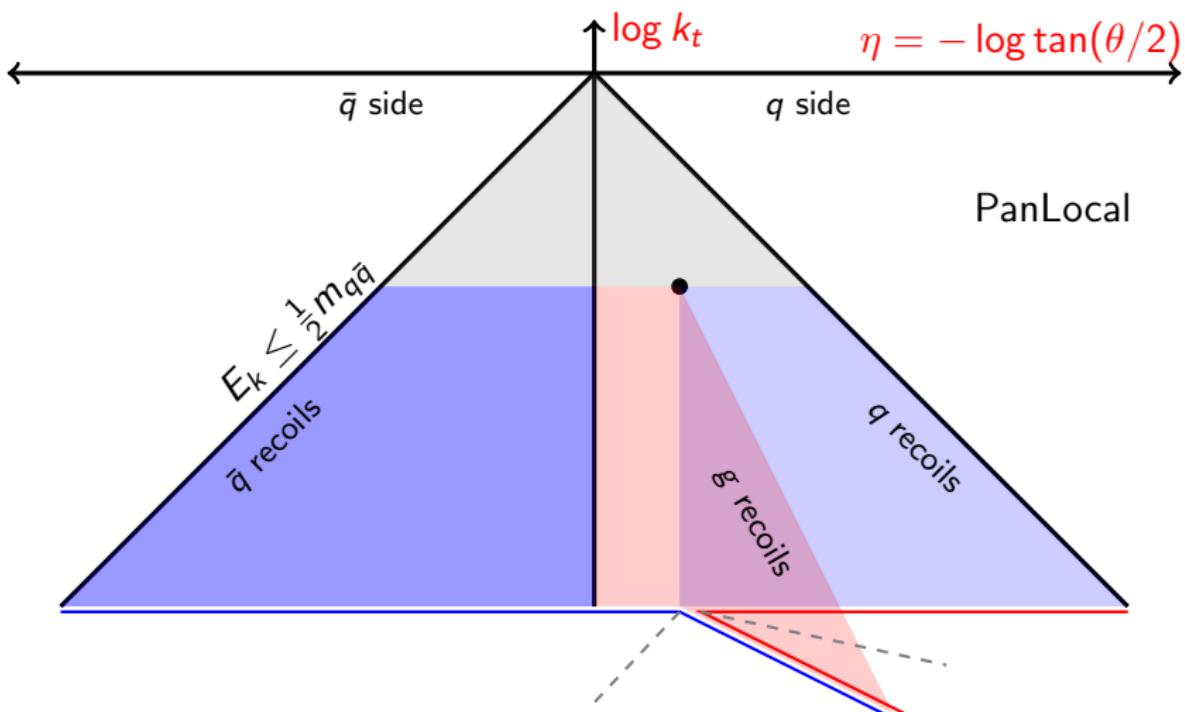
# Lund-plane representation: transverse recoil boundaries



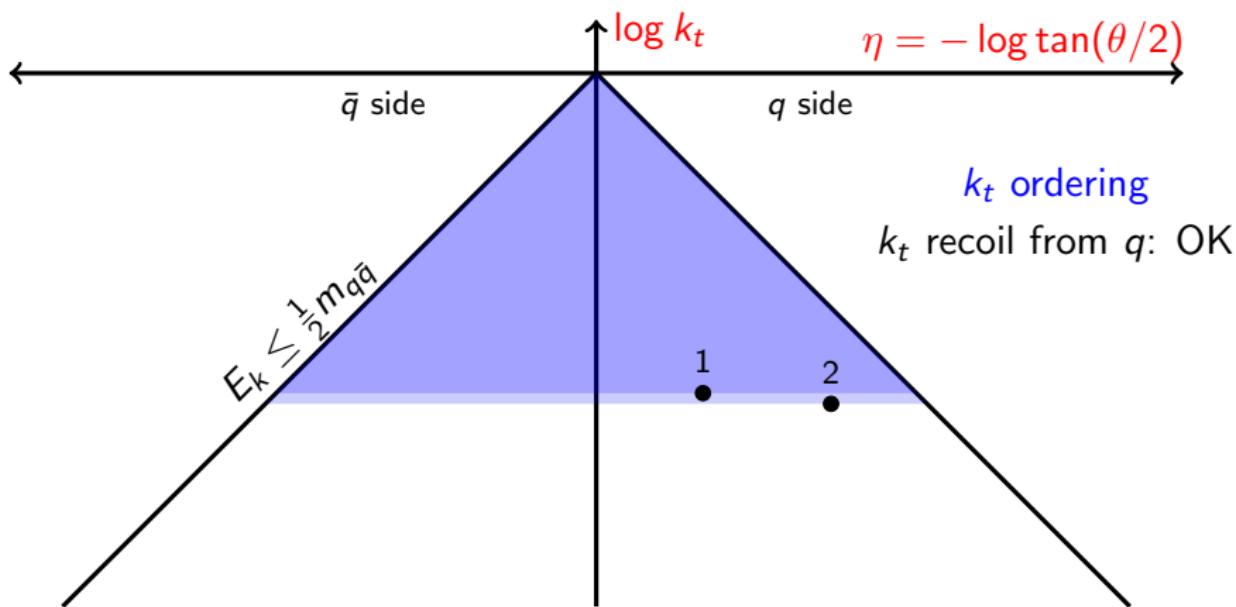
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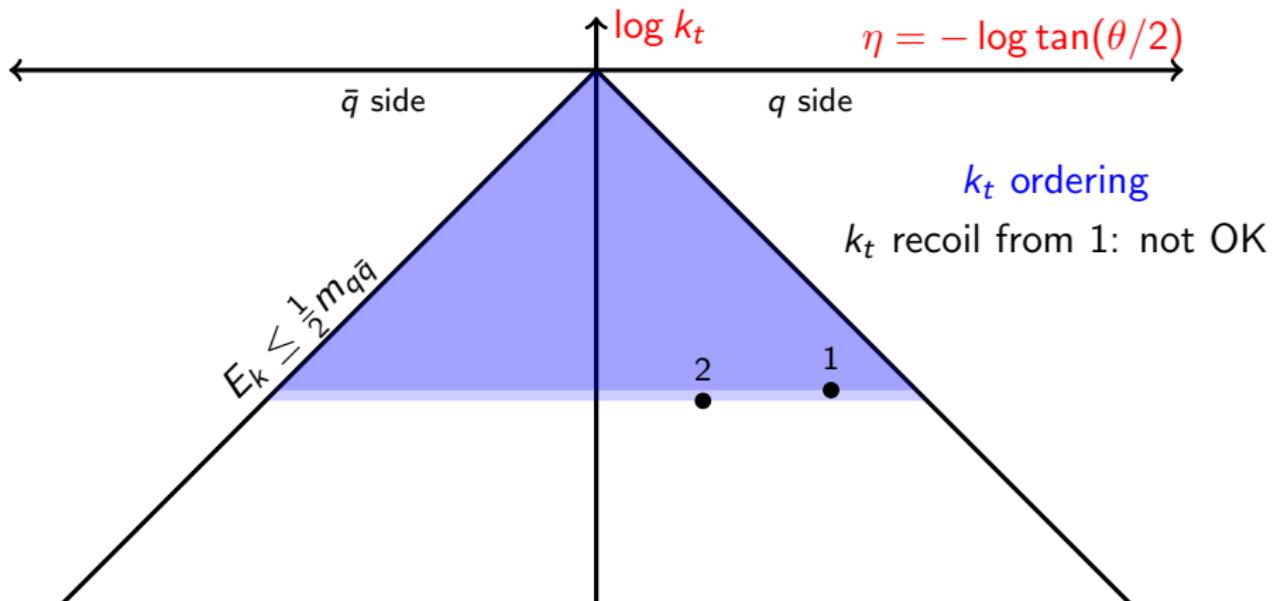
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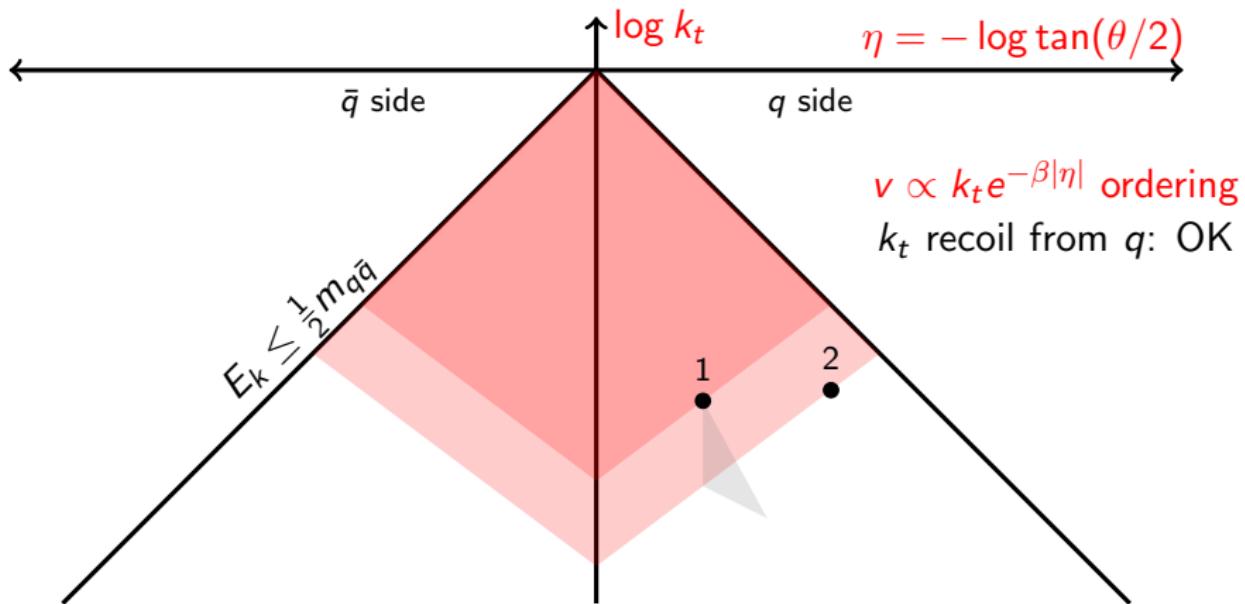
# Lund-plane representation: PanLocal evolution variable



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# Lund-plane representation: PanLocal evolution variable



$v \propto k_t e^{-\beta|\eta|}$  ordering  
 $k_t$  recoil from  $q$ : OK

# Kinematic map

(just to give an idea of what it takes)

$$p_k = a_k \tilde{p}_i + b_k \tilde{p}_j + k_{\perp}$$

$$p_i = a_i \tilde{p}_i + b_i \tilde{p}_j - f k_{\perp}$$

$$p_j = a_j \tilde{p}_i + b_j \tilde{p}_j - (1-f) k_{\perp}$$

*f* decides where to put recoil

- $f \rightarrow 1$  when  $k \rightarrow i$
- $f \rightarrow 0$  when  $k \rightarrow j$

Where to put the transition?

- Pythia8/Dire: equal angles in dipole rest frame
- PanLocal: equal angles in event frame

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with (PanLocal( $\beta$ ), variables  $v$  and  $\tilde{\eta}$ )

$$|k_{\perp}| = \rho v e^{\beta |\tilde{\eta}|} \quad \rho = \left( \frac{2 \tilde{p}_i \cdot Q \tilde{p}_j \cdot Q}{Q^2 \tilde{p}_i \cdot \tilde{p}_j} \right)^{\beta/2}$$

$$a_k = \sqrt{\frac{\tilde{p}_j \cdot Q}{2 \tilde{p}_i \cdot Q \tilde{p}_i \cdot \tilde{p}_j}} |k_{\perp}| e^{+\tilde{\eta}},$$

$$b_k = \sqrt{\frac{\tilde{p}_i \cdot Q}{2 \tilde{p}_j \cdot Q \tilde{p}_i \cdot \tilde{p}_j}} |k_{\perp}| e^{-\tilde{\eta}},$$

$f \approx \Theta(\tilde{\eta})$  and E-mom conservation

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# Assessing accuracy: $y_{23}$

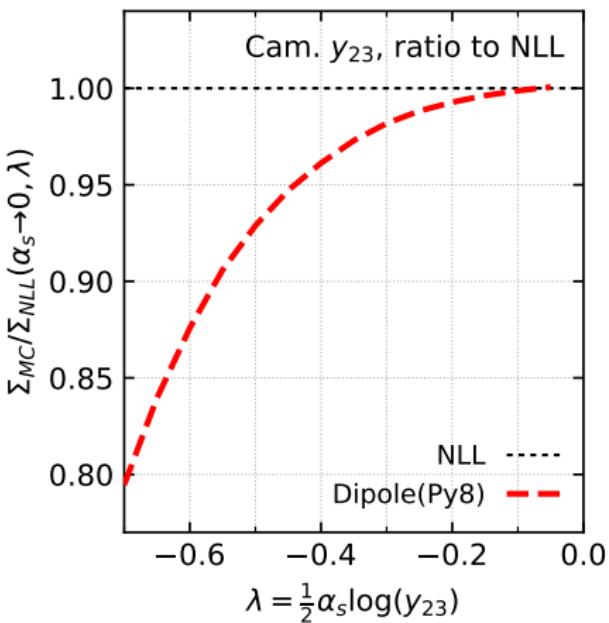
[M.Dasgupta,F.Dreyer,K.Hamilton,P.Monni,G.Salam,GS,20]

Example: C/A  $y_{23} \equiv \max_i k_{ti}$

Study

$$\frac{\sum_{MC}(\lambda = \alpha_s L, \alpha_s)}{\sum_{NLL}(\lambda = \alpha_s L, \alpha_s)} \text{ for } \alpha_s \rightarrow 0.$$

✗ Pythia8 deviates from NLL



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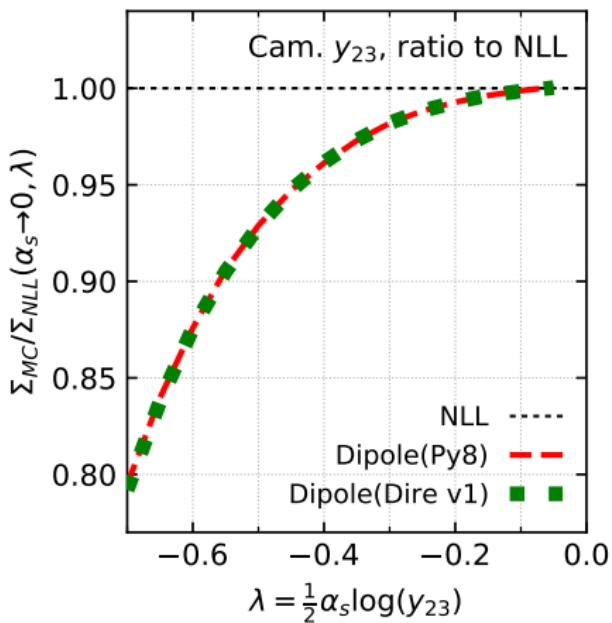
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- ✗ Dire(v1) same as Pythia8



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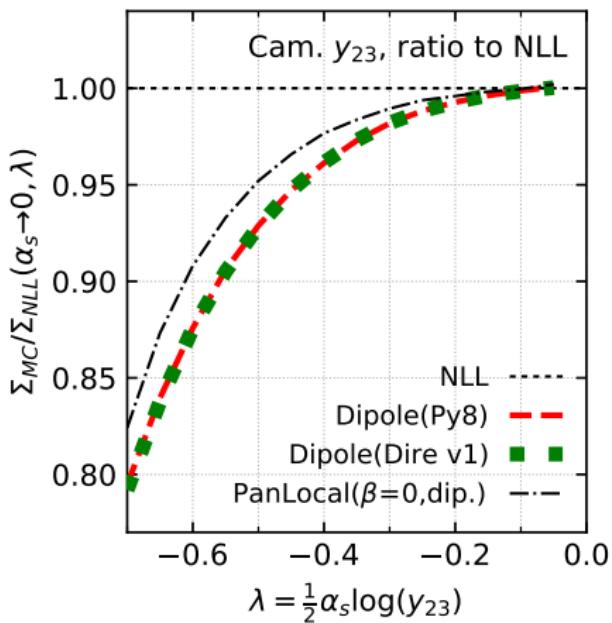
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- ✗ PanLocal( $\beta = 0$ ) still deviates  
(issue of  $k_t$  ordering remains)



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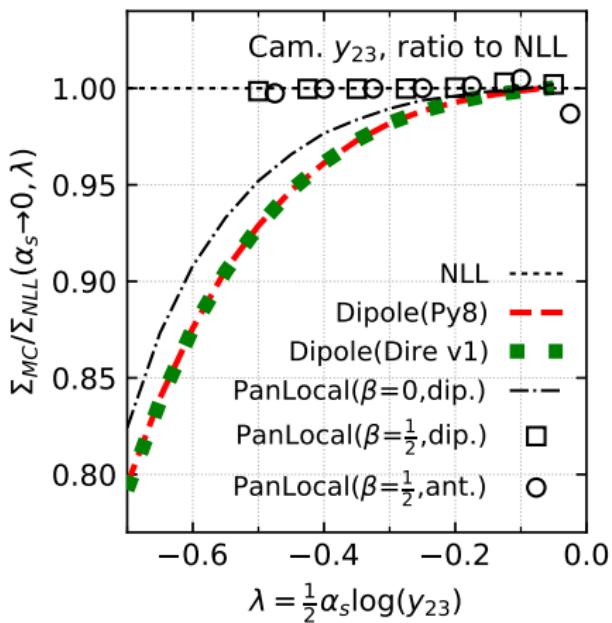
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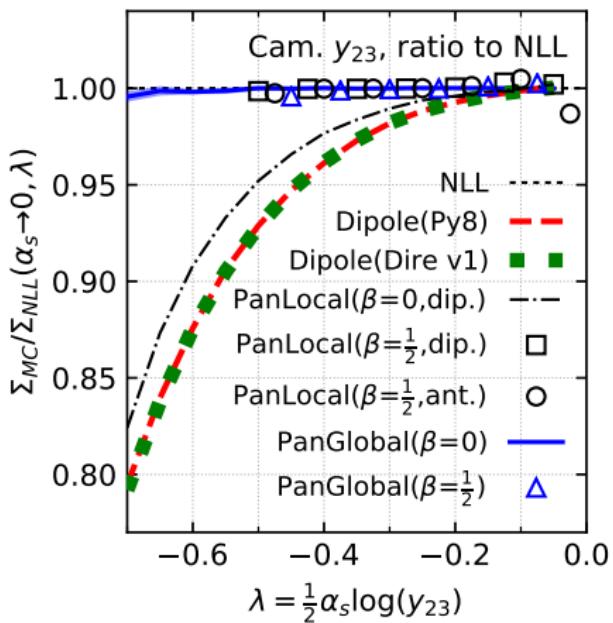
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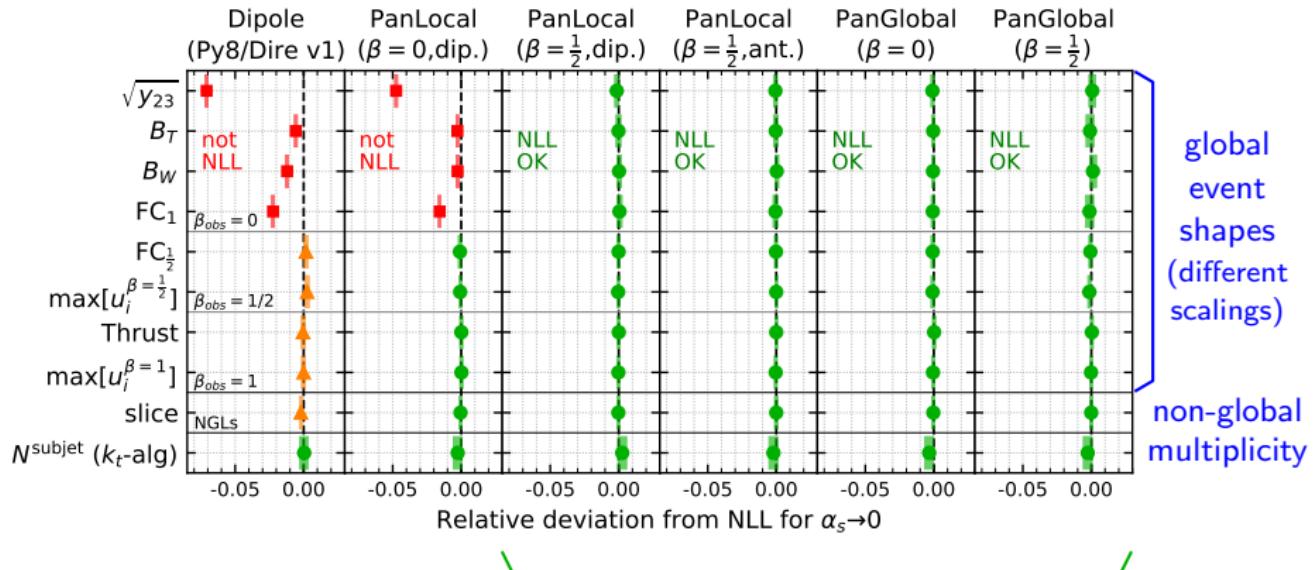
$$\frac{\sum MC(\lambda = \alpha_s L, \alpha_s)}{\sum NLL(\lambda = \alpha_s L, \alpha_s)} \text{ for } \alpha_s \rightarrow 0.$$

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(issue of  $k_t$  ordering remains)
- ✓ PanLocal( $0 < \beta < 1$ ) OK  
(issue of  $k_t$  ordering remains)
- ✓ PanGlobal( $0 \leq \beta < 1$ ) OK  
(global recoil allows also for  $\beta = 0$ )



# Assessing accuracy: extensive observable list

[M.Dasgupta,F.Dreyer,K.Hamilton,P.Monni,G.Salam,GS,20]

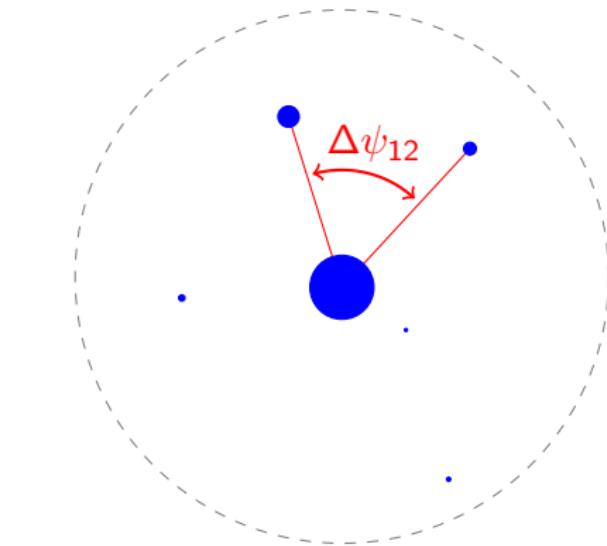


PanLocal( $0 < \beta < 1$ ) and PanGlobal( $0 \leq \beta < 1$ ) get expected NLL (i.e. 0)

(green: OK at NLL; orange: issues at fixed order; red issues at fixed and all orders)

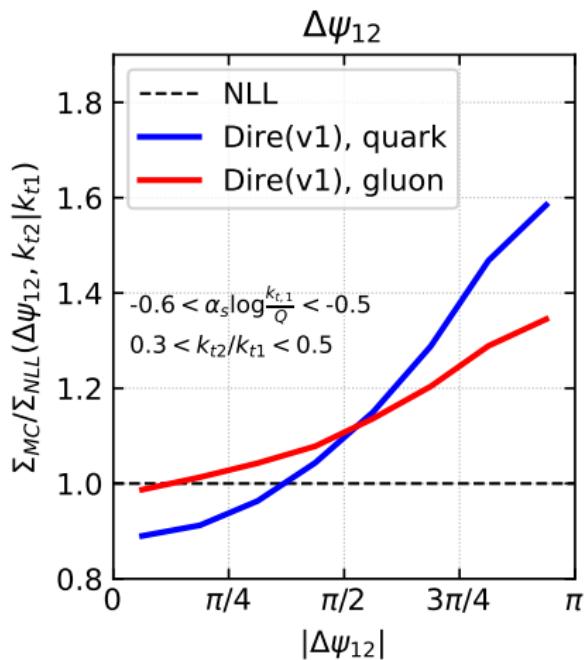
# A last example

- ▶ Look at angle  $\Delta\psi_{12}$  between two hardest “emissions” in jet  
(defined through Lund declusterings)



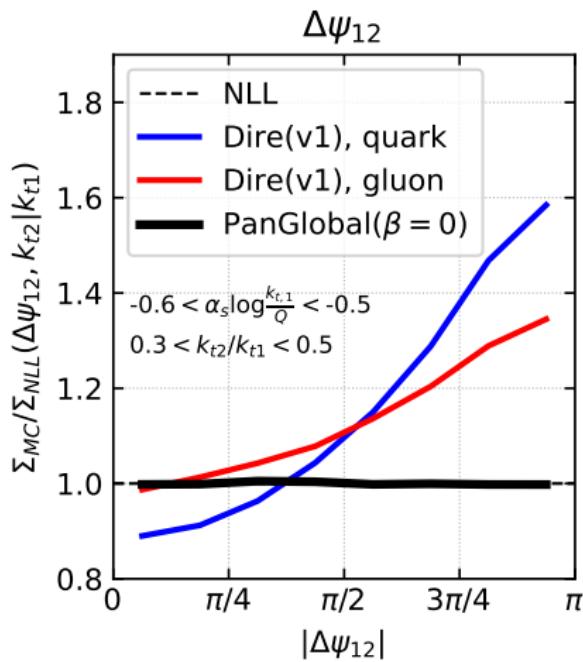
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- ▶ quite large NLL deviations in current dipole showers
- ▶ differences between quark and gluon jets



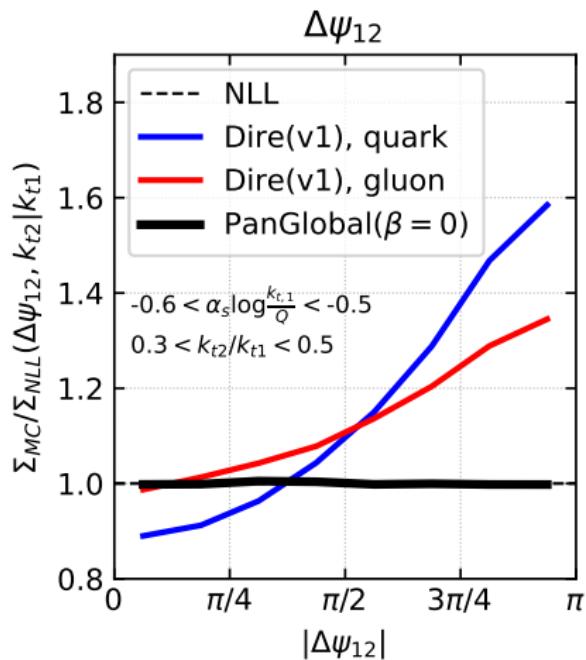
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- ▶ quite large NLL deviations in current dipole showers
- ▶ differences between quark and gluon jets
- ▶ PanGlobal gets correct NLL
- ▶ ML could “wrongly/correctly” learn this



# The quest for precision across scales

What is your name?

## PanScales

E.Slade, R.Medves; F.Dreyer, B.El-Menoufi, A.Karlberg, L.Scyzboz, R.Verheyen;  
M.Dasgupta, K.Hamilton, P.Monni, G.Salam, GS

What is your quest?

Deepen the understanding & improve parton showers (core at colliders)  
1st step presented here: accuracy assessment + first (towards) NLL  $e^+e^-$  shower

What is your favourite colour?

- still at large  $N_C$ , in  $e^+e^-$  and without spin correlations
- Next (obvious) steps:  
*beyond large- $N_c$ , extend to  $pp$ , include spin correlations*
- Longer run: *investigate phenomenology, go public, explore NNLL*