

# A brief look inside jet substructure

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Getting to grips with QCD, April 4-6 2018

## Jets are routine QCD objects

- ubiquitous in collider physics
- around since 40 years
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You could live a happy life by just knowing a few things

Concepts:

- Jets are proxies to hard partons produced in collisions
- infrared-and-collinear safe
- capture collimated parton cascades from hard scale  $Q$  to  $\mathcal{O}(1 \text{ GeV})$

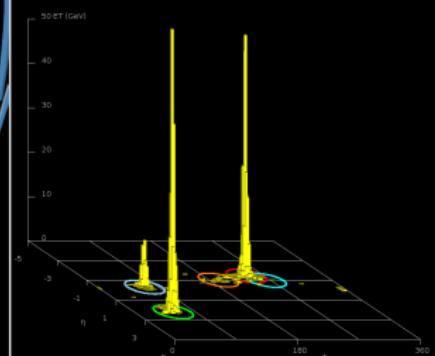
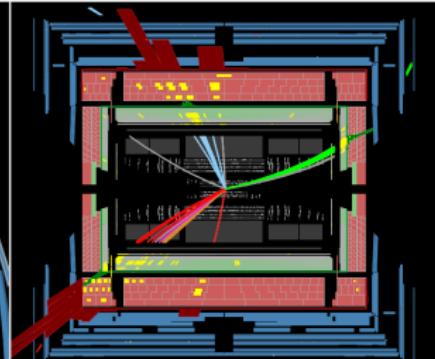
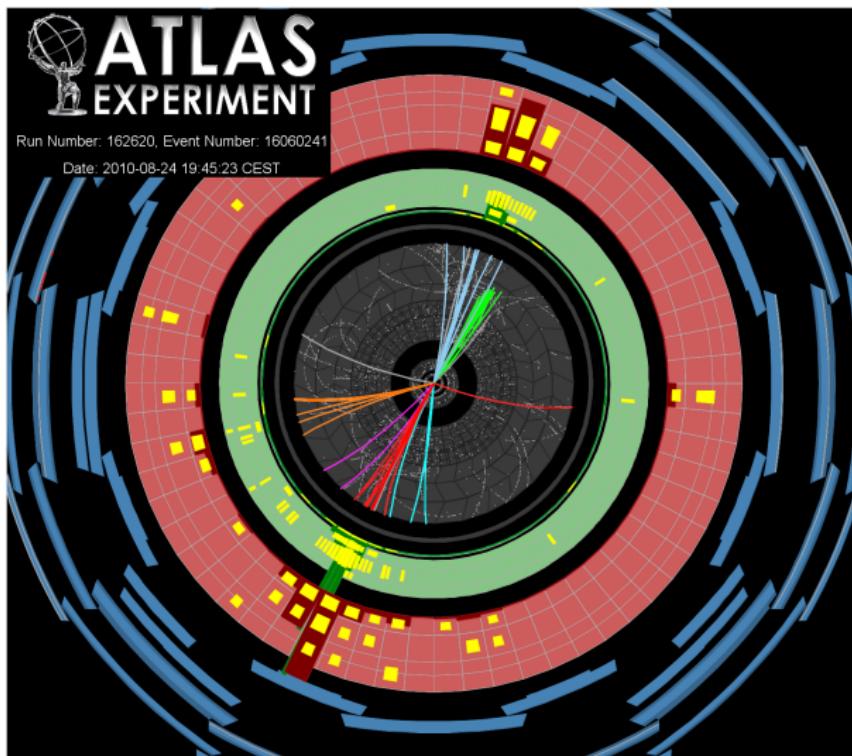
Practically:

- obtained by running a clustering algorithm
- the LHC uses the anti- $k_t$  algorithm
- FastJet covers all your numerical needs for clustering

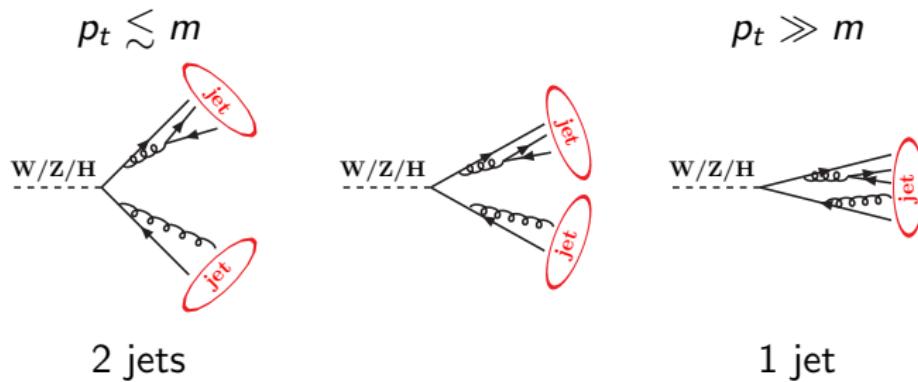


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Date: 2010-08-24 19:45:23 CEST



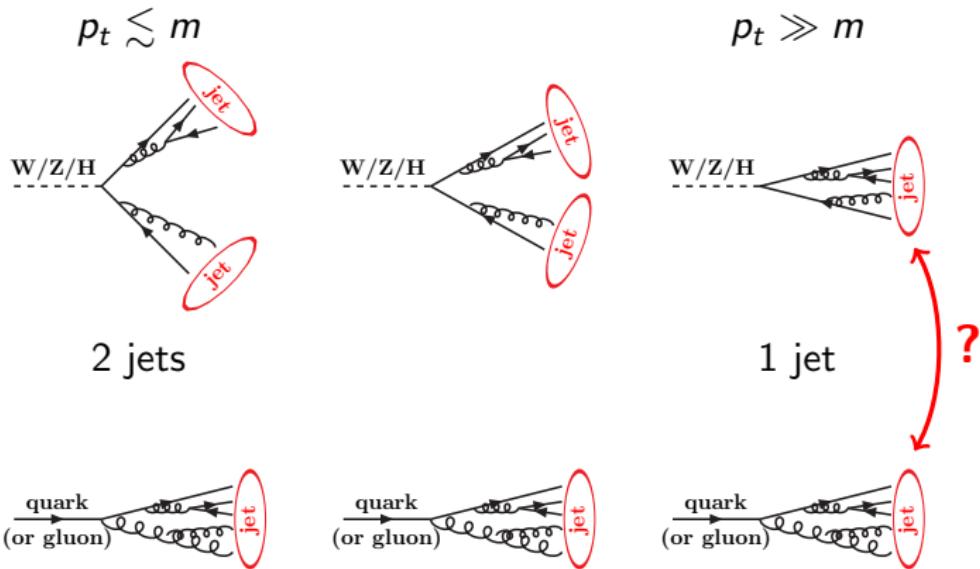
# Boosted objects



(massive) objects produced boosted (energy  $\gg$  mass) are seen as 1 jet:

$$\theta_{q\bar{q}} \sim \frac{m}{p_t}$$

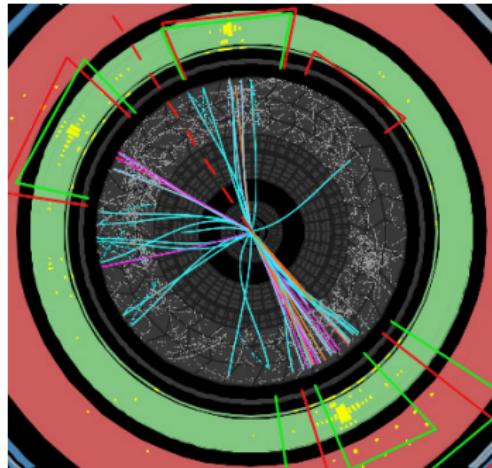
# Boosted objects



use substructure to separate from QCD jets

# Other examples

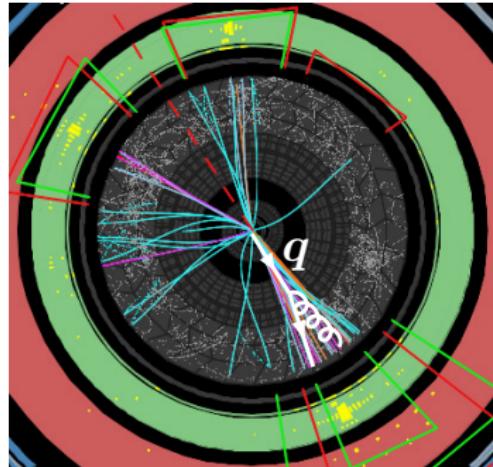
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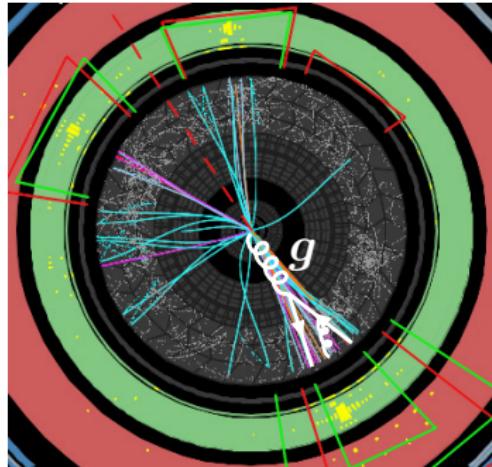
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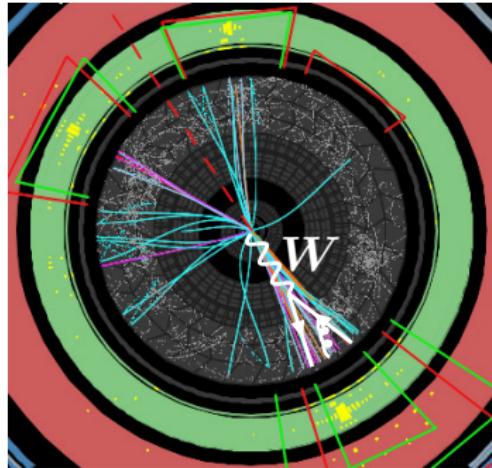
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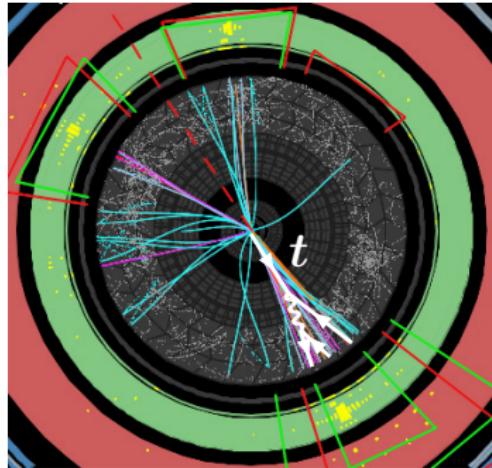
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- a  $W/Z$  (or a Higgs)?



# Other examples

What jet do we have here?

- a quark?
- a gluon?
- a  $W/Z$  (or a Higgs)?
- a top quark?

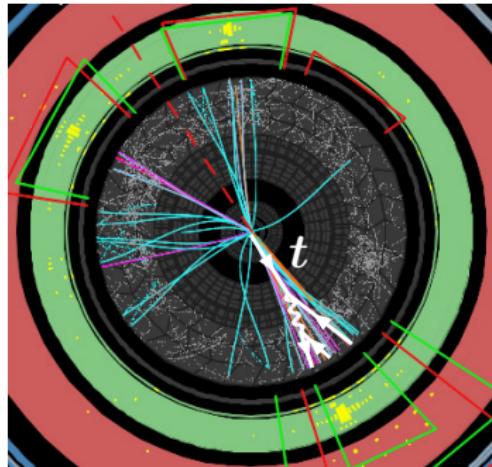


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Source: ATLAS boosted top candidate

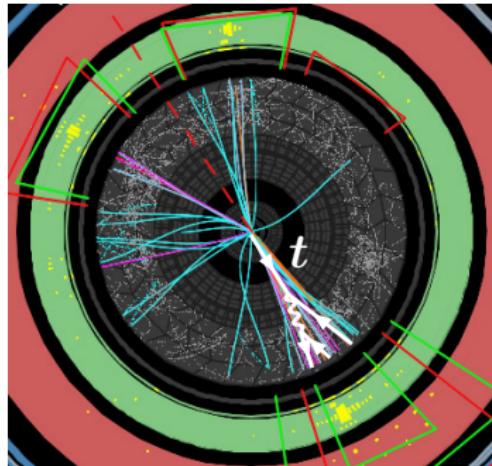


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Substructure means looking at the internal dynamics of jets  
(as opposed to consider jets as monolithic objects)

## Main concepts:

- Compared to standard jets, substructure uses a **large toolkit**

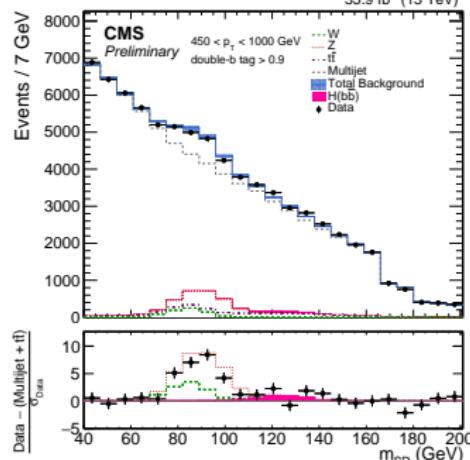
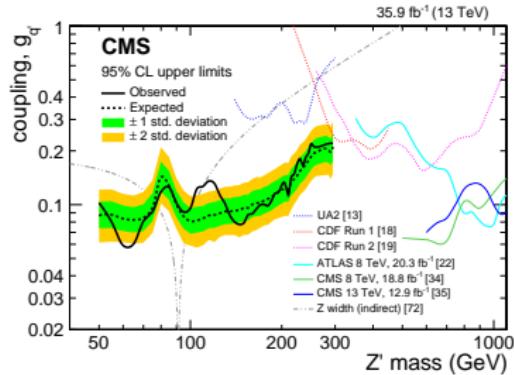
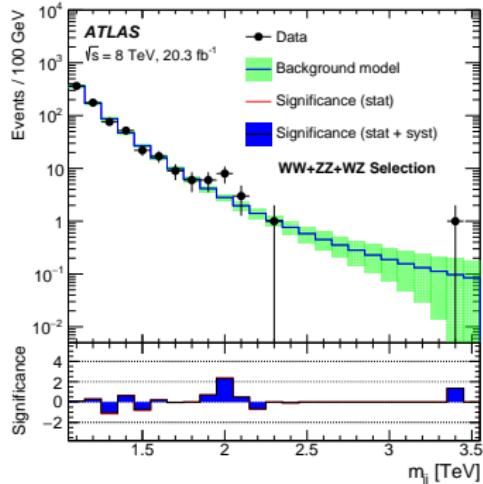
## Main concepts:

- Compared to standard jets, substructure uses a **large toolkit**
- Basic tools are organised around **2<sub>(3)</sub> major concepts**:
  - “peak/prong finders”:
    - $W/Z/H/t$  decay into hard partons  $\Rightarrow$  jets with multiple hard cores
    - QCD ( $q/g$ ) jets dominated by soft radiation  $\Rightarrow$  single cores
  - Tools search for multiple hard cores
  - **Radiation patterns**:
    - colourless  $W/Z/H$  has less radiation than  $q/g$  jets
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  - (also grooming to remove soft contamination from fat jets)
- **Increasing range of applications**
  - Searches and measurements at the LHC
  - Precision QCD calculations
  - Measurements in heavy-ion collisions
  - Machine Learning

# Searches and measurements



↑ (now-gone) di-boson excess (end of Run-I)

→ Search for  $X \rightarrow q\bar{q}$   
Region inaccessible otherwise

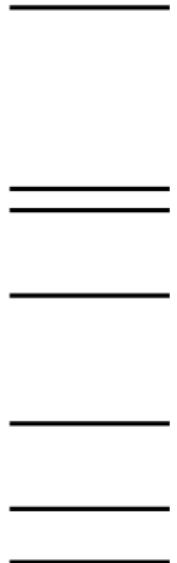
→ Clear Z peak, hint of a H peak

Give an overview of these aspects

Articulated around a work in progress  
with Frederic Dreyer and Gavin Salam

# Pre-requisite number 1: Cambridge/Aachen (de-)clustering

Cambridge/Aachen: iteratively recombine the closest pair



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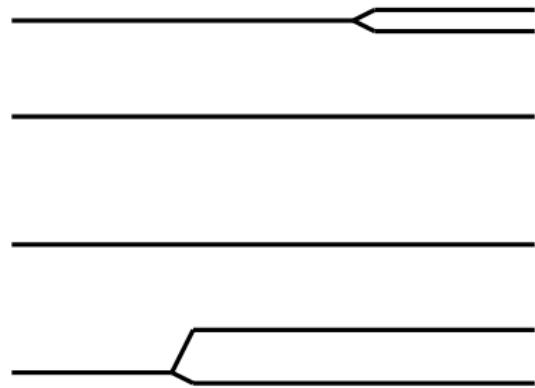
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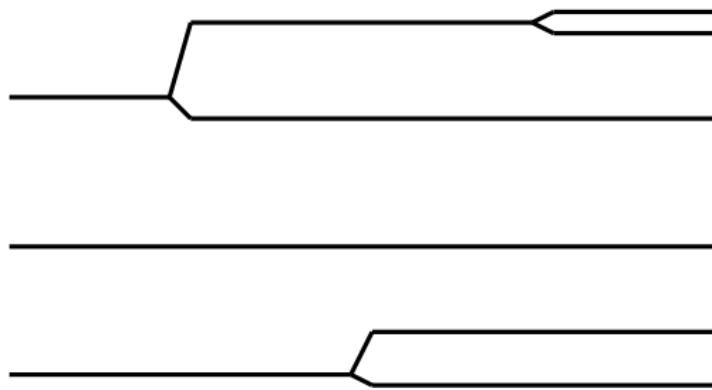
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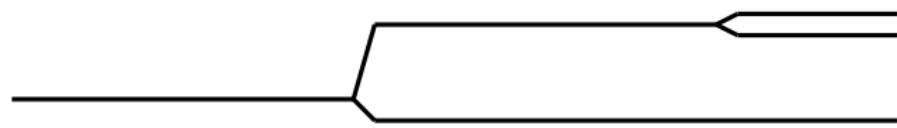
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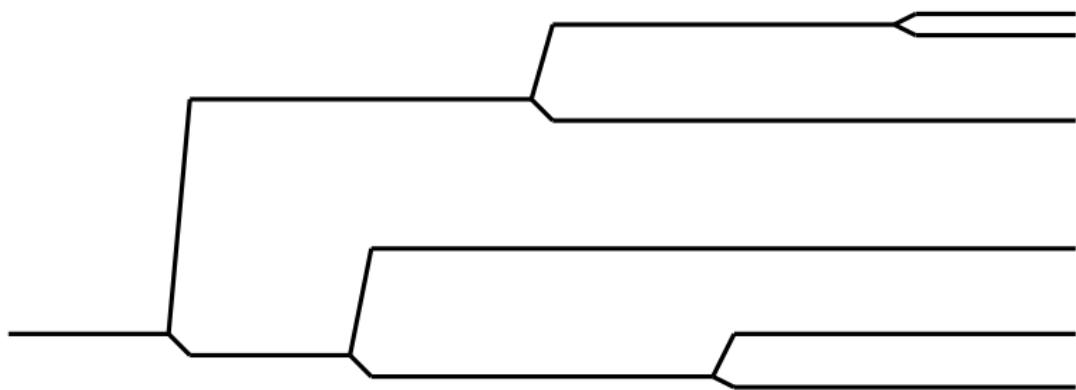
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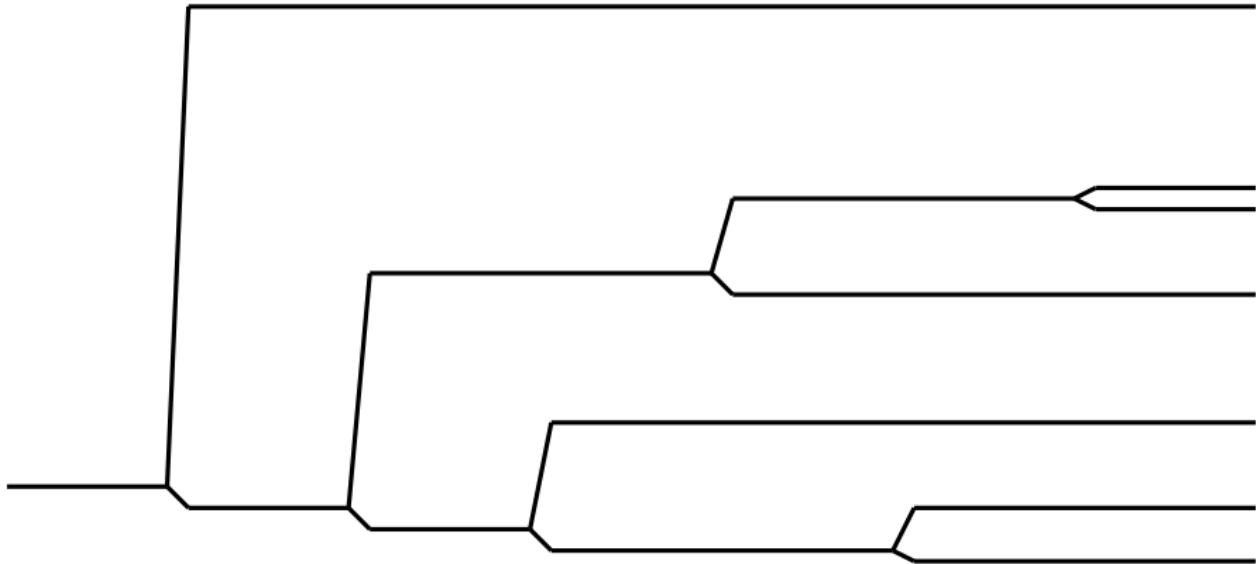
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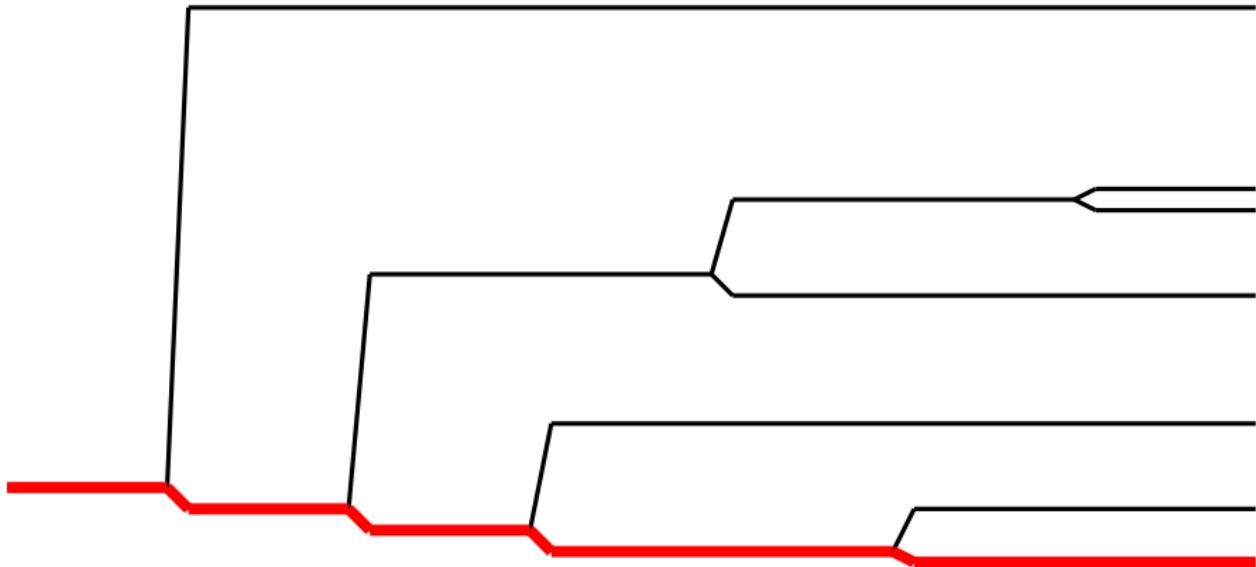
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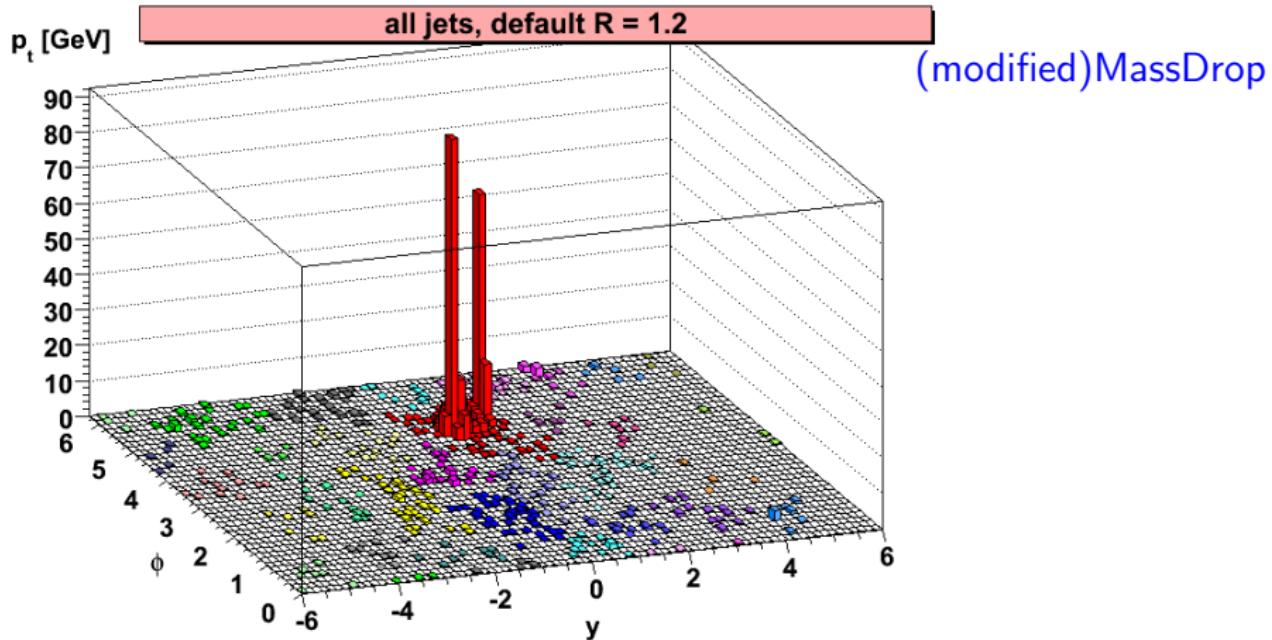


**Usage:** iteratively undo the clustering to study internal jet dynamics

**Typically:** follow the hardest branch (largest  $p_t$  or  $z$ )

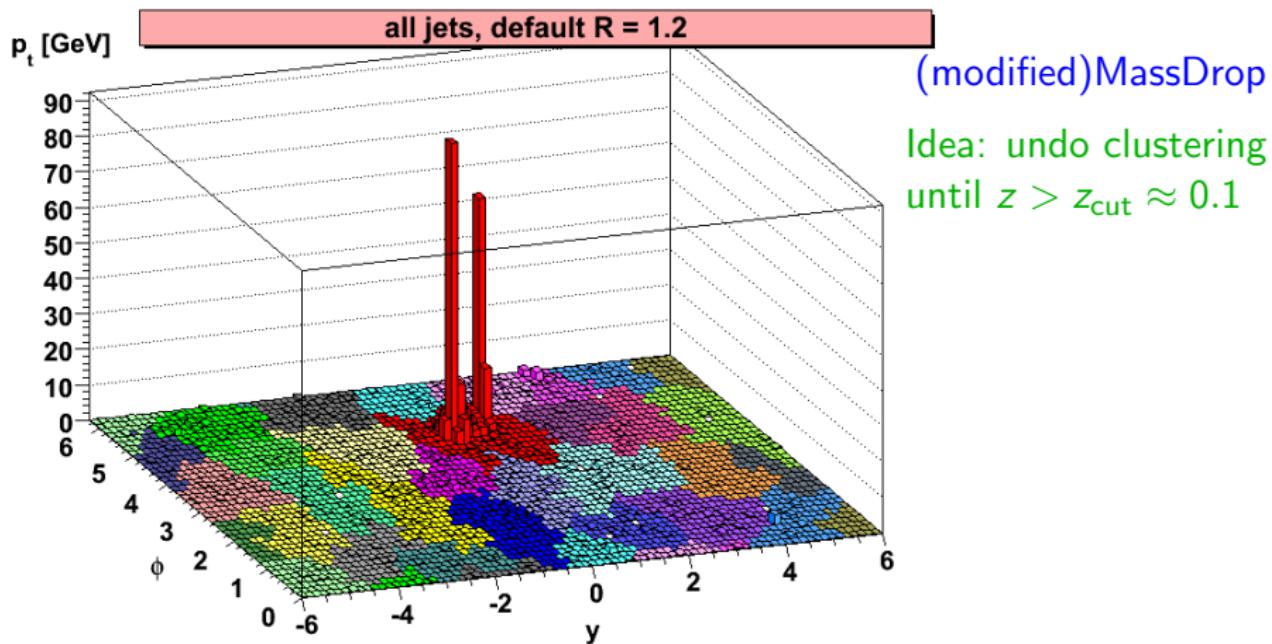
# Example: mMDT/SD prong finder

[J.Butterworth,A.Davison,M.Rubin,G.Salam,08]



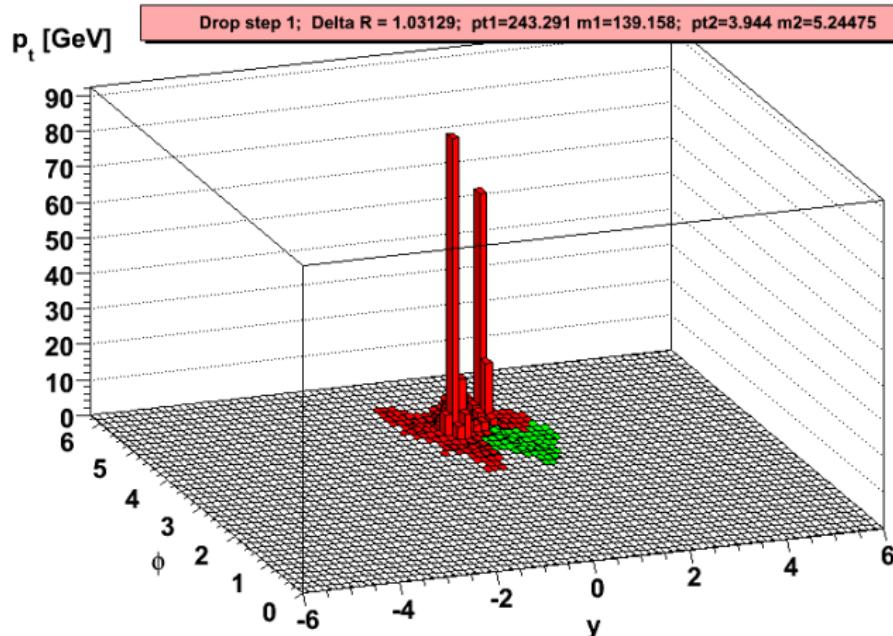
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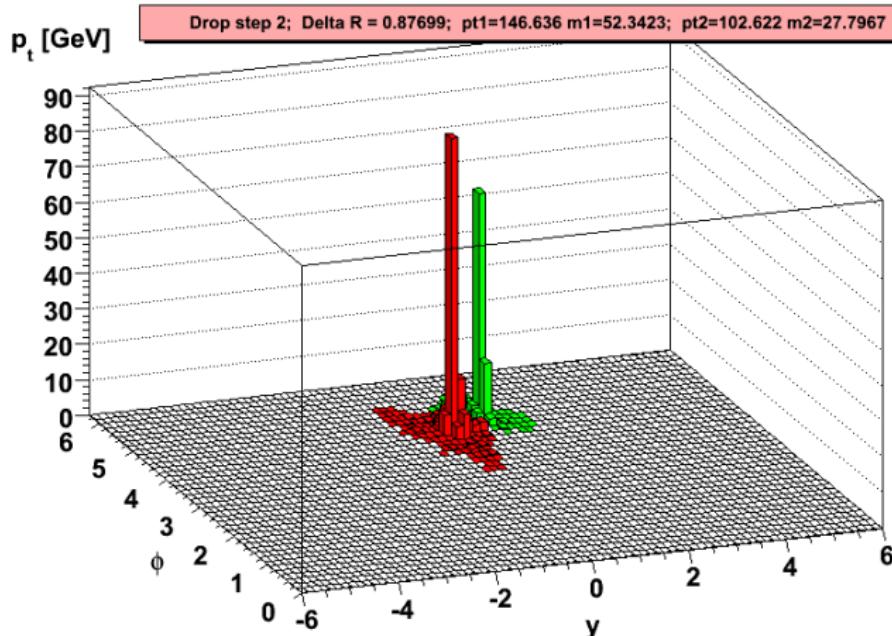
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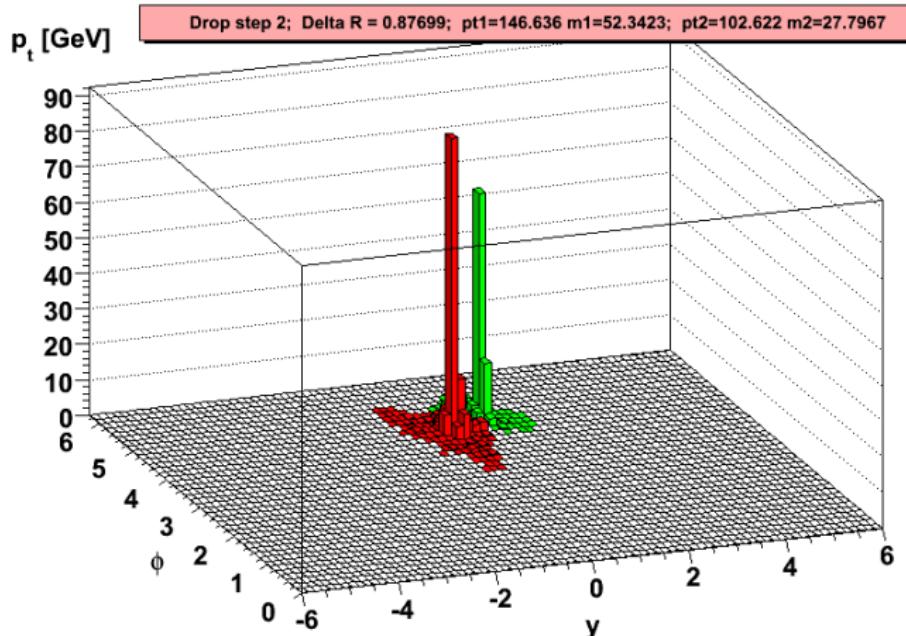
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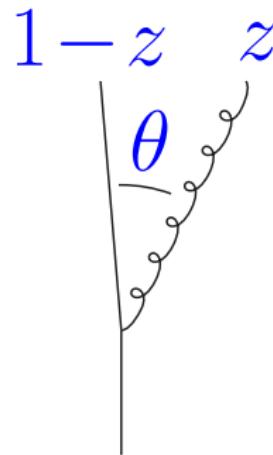
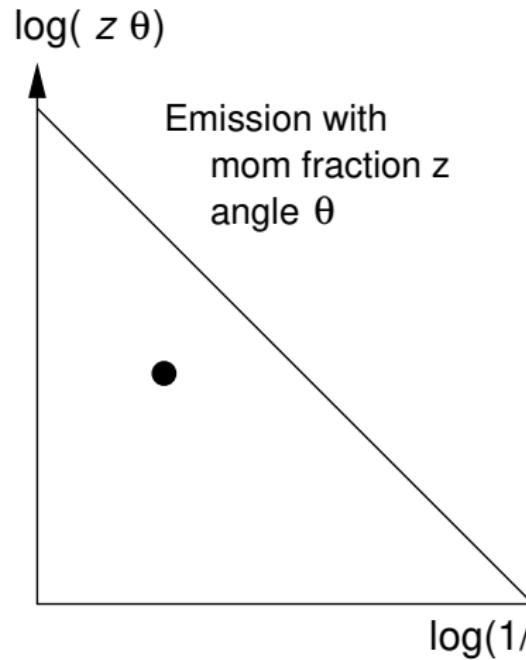
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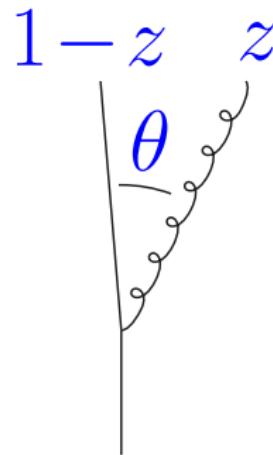
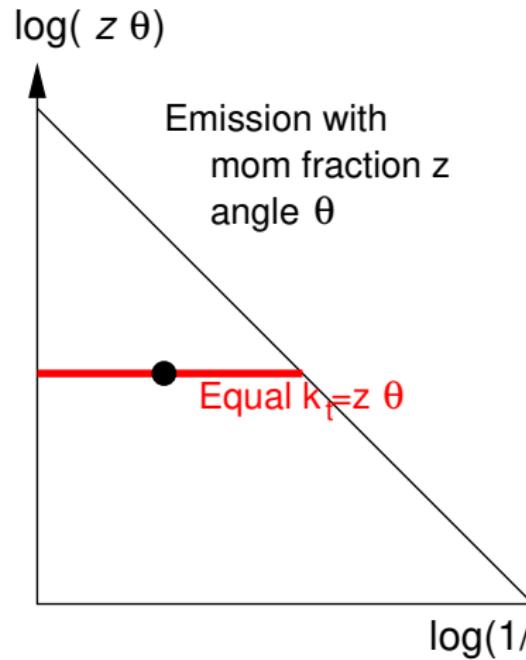
Variant: **SoftDrop**: impose  $z > z_{\text{cut}} e^{-\beta}$

[A.Larkoski,S.Marzani,GS,J.Thaler,14]

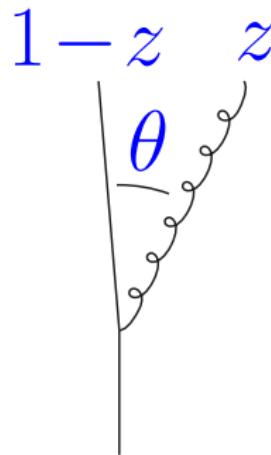
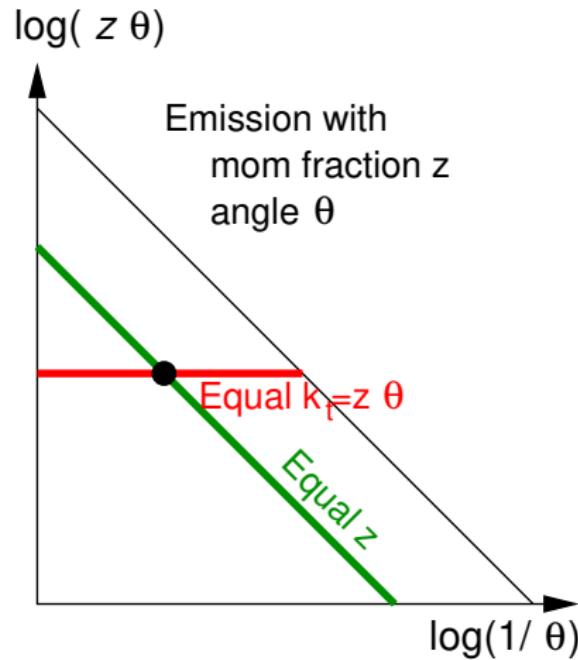
## Pre-requisite number 2: Lund planes



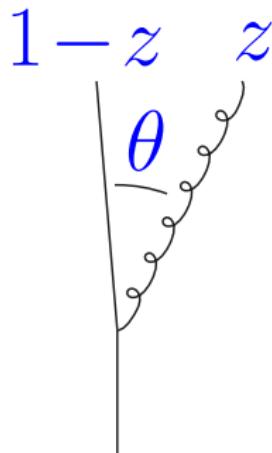
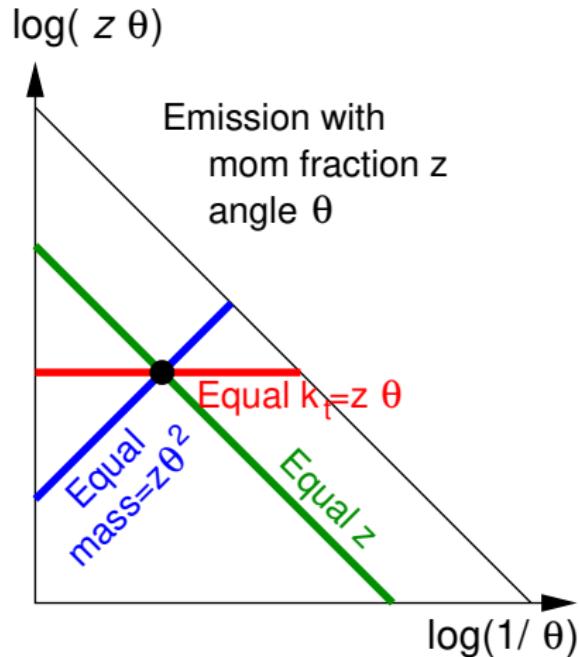
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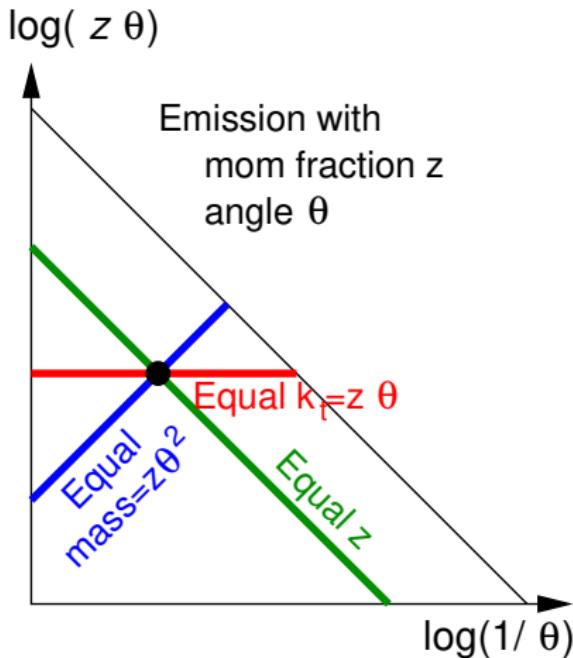
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Observables in the boosted limit

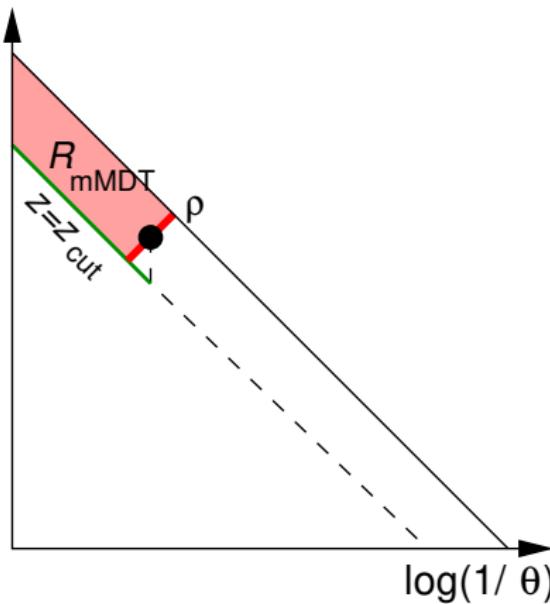
Jet “mass”:  $(z_1\theta_1^2 \gg z_2\theta_2^2 \gg \dots)$

$$\rho \equiv \frac{m^2}{p_t^2 R^2} = \sum_{i \in \text{jet}} z_i \theta_i^2 \approx z_1 \theta_1^2$$

## Pre-requisite number 2: Lund planes

(mMDT) jet mass spectrum at LL

$\log(z\theta)$



$$\frac{\rho}{\sigma} \frac{d\sigma}{d\rho} = R'_{\text{mMDT}} \exp(-R_{\text{mMDT}})$$

- ① emission of given mass

$$R'_{\text{mMDT}} \sim \frac{\alpha_s C_R}{\pi} \log(1/z_{\text{cut}})$$

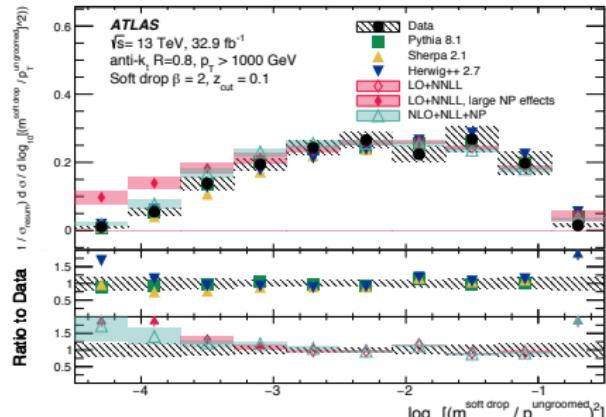
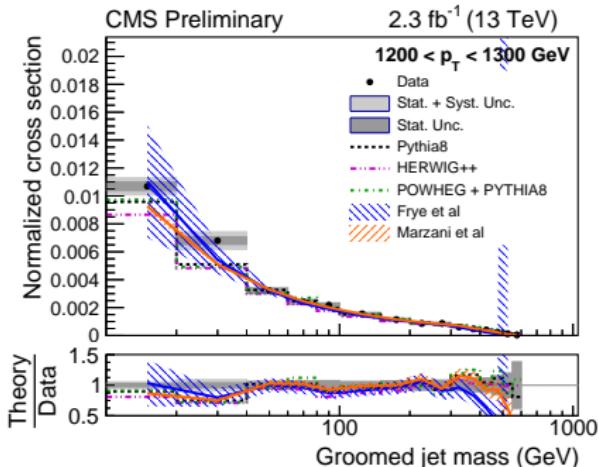
- ② veto on larger-mass (Sudakov)

$$R_{\text{mMDT}} \sim \frac{\alpha_s C_R}{\pi} \log(1/\rho) \log(1/z_{\text{cut}})$$

[M.Dasgupta, A.Fregoso, S.Marzani, G.Salam]

# Precision physics at the LHC

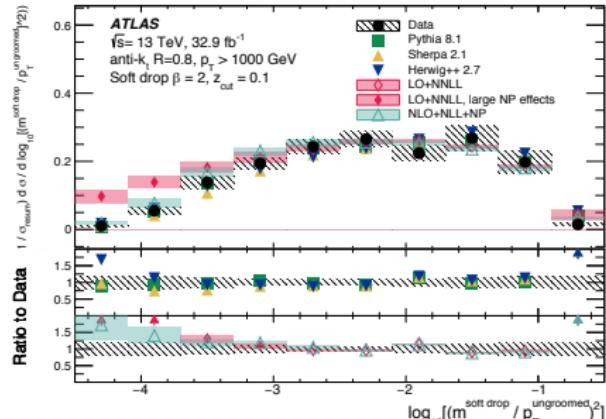
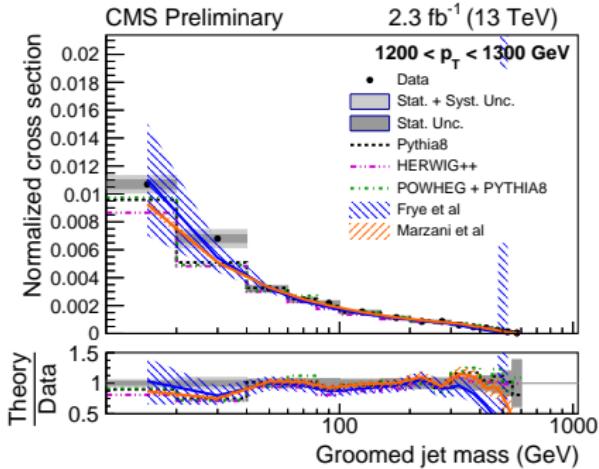
- ▶ LHC Measurements (CMS-PAS-SMP-16-010, ATLAS CERN-EP-2017-231)
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good overall agreement with the data

Precise observable with limited sensitivity to NP effects

⇒ possibility to extract  $\alpha_s$  (on-going study)

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Based on

- ① Cambridge/Aachen de-clusterings
- ② Lund-plane variables

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We can

- ▶ learn about jet dynamics
- ▶ constrain Monte-Carlo generators  
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- ▶ perform analytic studies
- ▶ learn about the quark-gluon plasma
- ▶ Tag boosted objects
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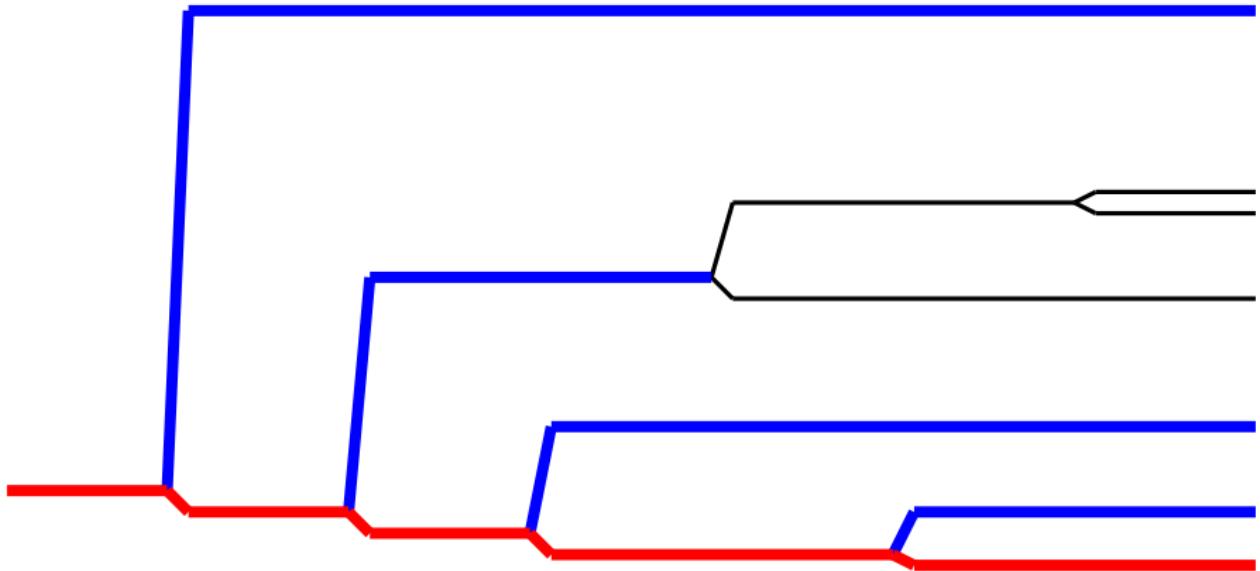
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I will illustrate this in the next slides

# Lund plane density

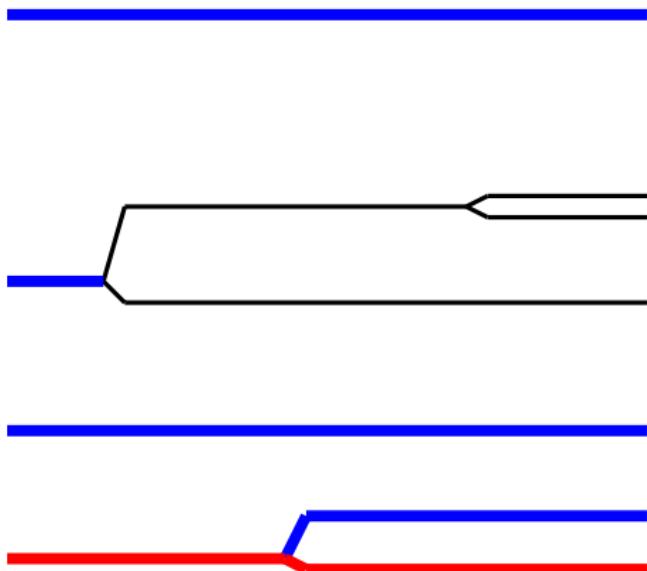
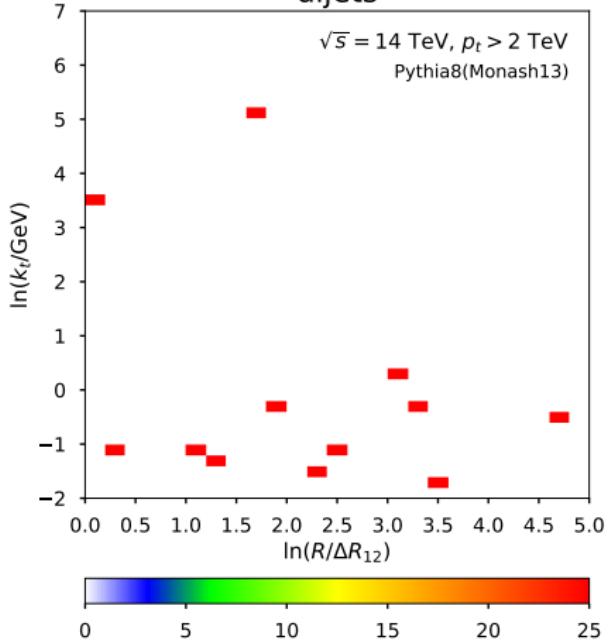


Consider all the emissions from the hardest branch

# Lund plane density

One jet

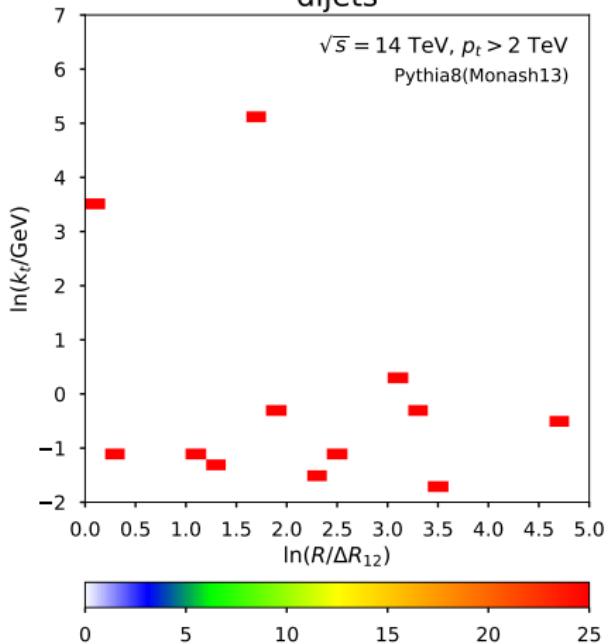
dijets



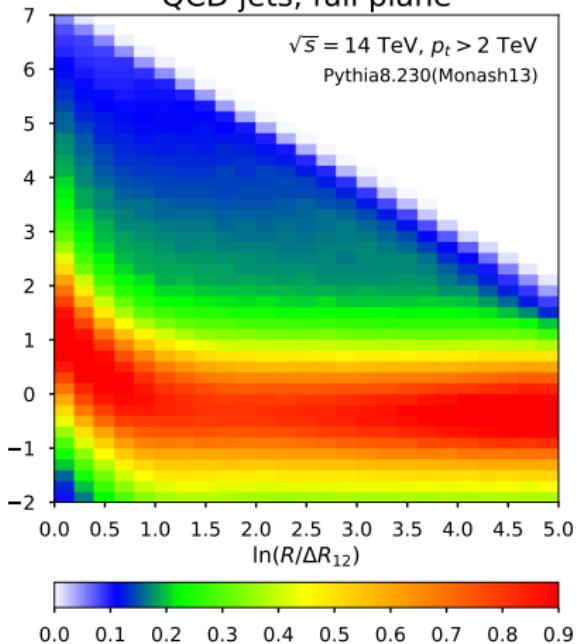
Consider all the emissions from the hardest branch  
Put them in the Lund plane

# Lund plane density

One jet  
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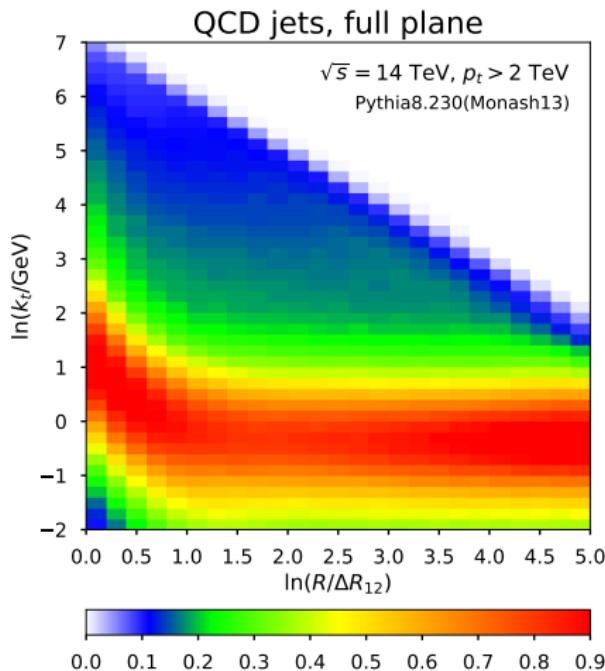


Average over jets  
QCD jets, full plane

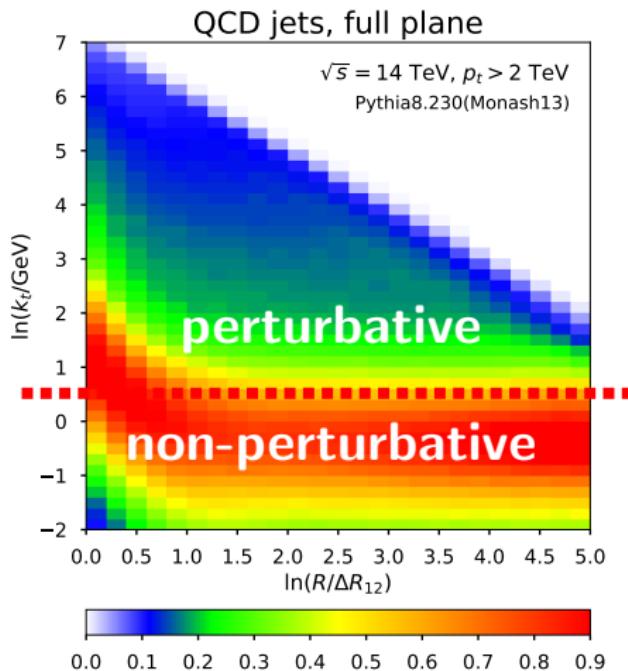


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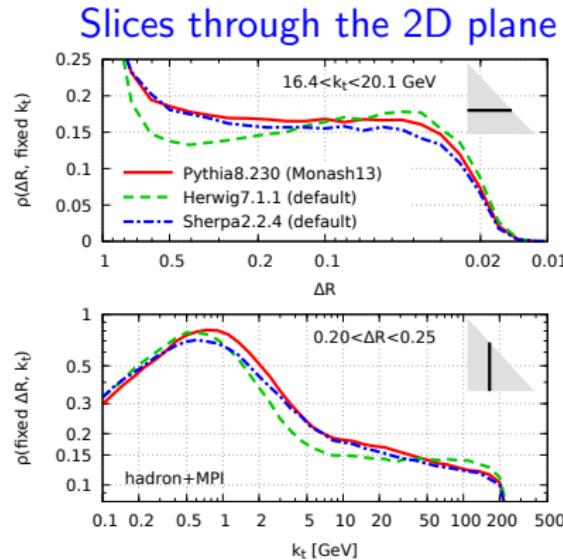
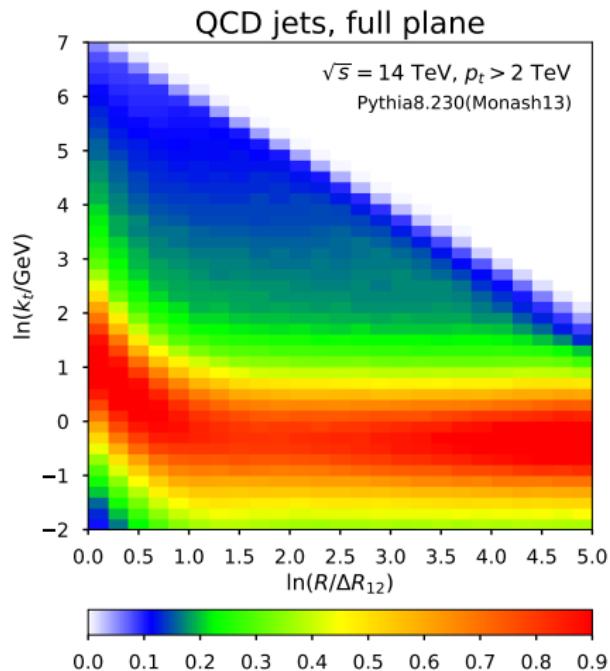
# Lund plane and Monte-Carlo generators



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# Lund plane and Monte-Carlo generators



- Flat at small angles (until ISR)
- $\alpha_s(k_t)$  then non-pert bump
- Differences between MCs
- calls for measurement

# Lund plane and QCD analytic calculations

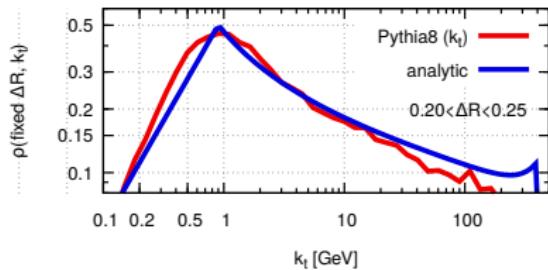
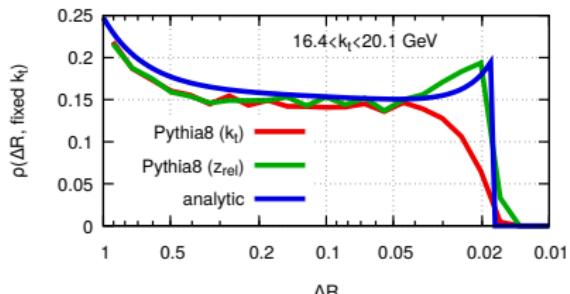
Roughly:

$$\rho(\Delta R, k_t) = \frac{\alpha_s(k_t) C_R}{\pi} z p(z)$$

Additional effects:

- ISR (included here)
- clustering effects
- flavour changes
- energy conservation
- ...

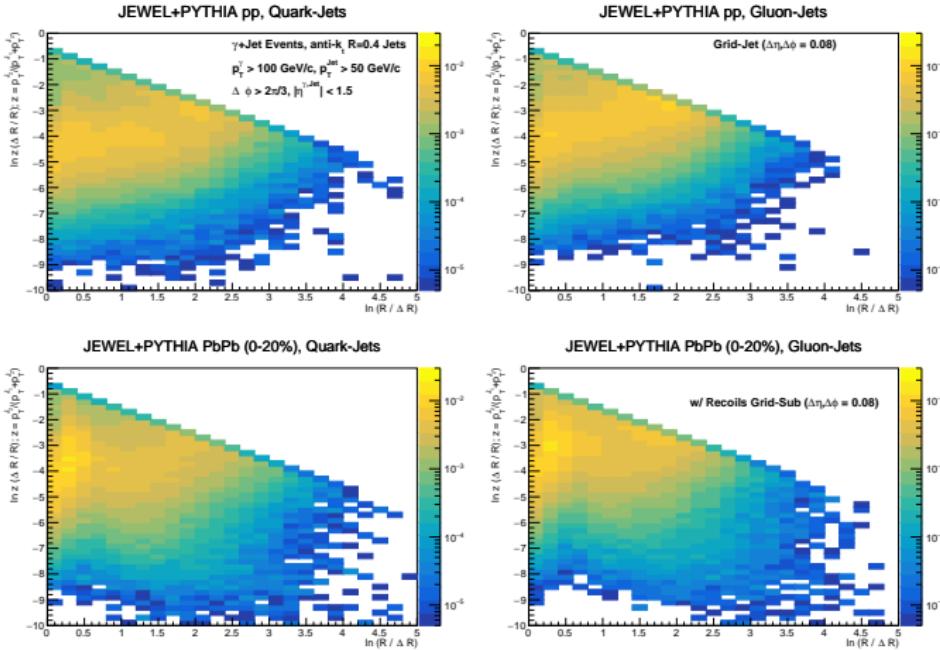
Can be systematically calculated and improved



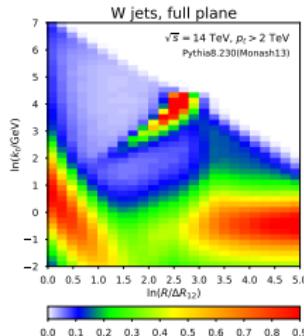
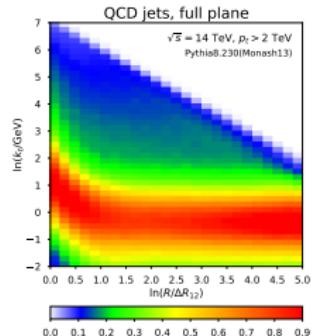
# Lund plane and Heavy-ion collisions

[Y-T. Chien, R. K. Elayavalli]

## Quark v. gluon jets in Heavy-ion collisions

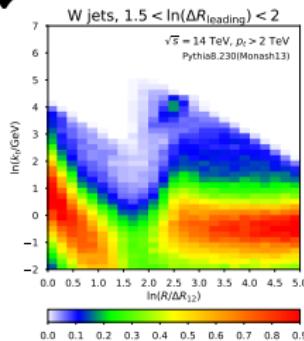
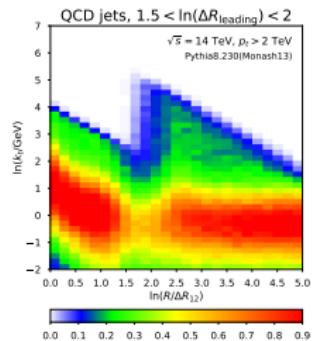


# Lund plane and W tagging

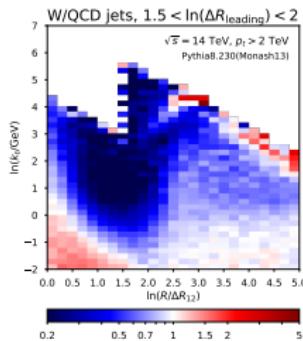


- In practice: split into a “leading” emission and Lund plane for all the others
- Use ratio to build a log-likelihood discriminant

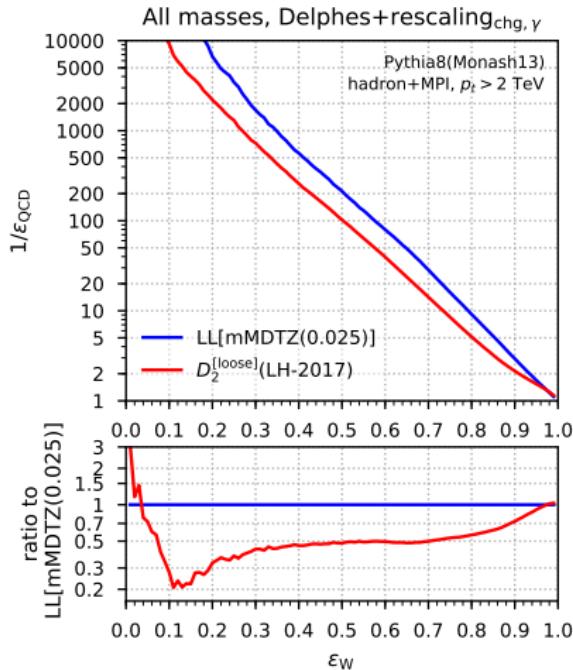
↓  
Lund plane  
after leading removal



ratio →



# Lund plane and W tagging



better than “standard” approach  
(2-prong tagger + cut on shape)

[ $D_2^{\text{[loose]}}$  from Les-Houches PhysTeV 2017]

# Lund plane and Machine learning

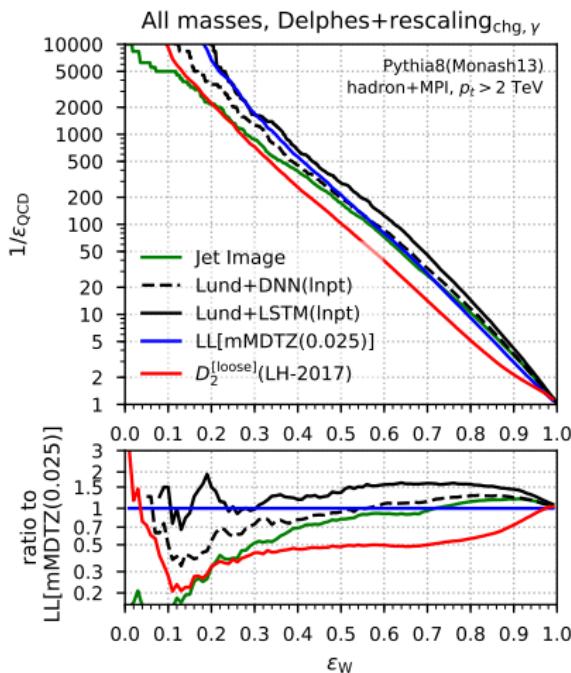
Previous approach can be used as input to Machine Learning:

- “Lund image” fed to a Dense Neural Network
- “Lund coordinates” fed to a Long Short Term Memory network

# Lund plane and Machine learning

Previous approach can be used as input to Machine Learning:

- “Lund image” fed to a Dense Neural Network
- “Lund coordinates” fed to a Long Short Term Memory network



- better than previous ML approaches
- LSTM does even better than Log-Likelihood
- TODO: Log-Likelihood from analytics

[Jet Image: J.Cogan, M.Kagan, E.Strauss, A.Schwarzman, 14; L.de Oliveira, M.Kagan, L.Mackey, B.Nachman and A.Schwarzman, 15]

## Jet substructure has gained a lot of importance in the past decade

- Important tool for LHC physics (searches and measurements)
- exciting pQCD phenomenology
  - ▶ understanding and development of tools
  - ▶ precision pheno at the LHC
  - ▶ interesting QCD structure emerging (not covered here)
- Expansion towards new horizons:
  - ▶ heavy-ion hard probes
  - ▶ machine learning
- Recent work: Lund planes are useful in many aspects

BOOST Annual meeting  
around 100 theorists and experimentalists discussing  
discussing latest progress in substructure

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**July 16-20: BOOST 2018 in Paris**  
<https://indico.cern.ch/e/boost2018>

