

New perspectives in QCD with jet substructure

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GDR QCD, December 4 2017

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- ubiquitous in collider physics
- around since 40 years
- used in at least 60% of LHC analyses

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You could live a happy life by just knowing a few things

Concepts:

- Jets are proxies to hard partons produced in collisions
- infrared-and-collinear safe
- capture collimated parton cascades from hard scale Q to $\mathcal{O}(1 \text{ GeV})$

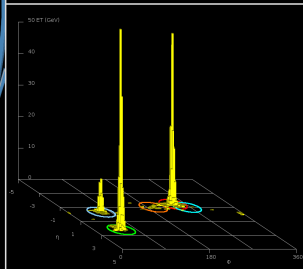
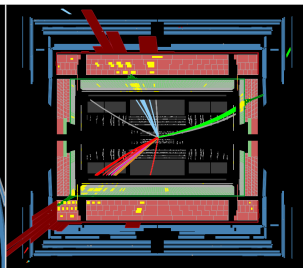
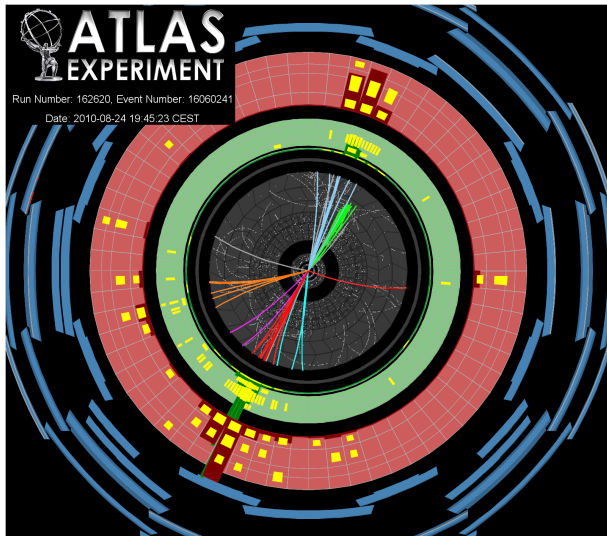
Practically:

- obtained by running a clustering algorithm
- the LHC uses the anti- k_t algorithm
- FastJet covers covers all your numerical needs for clustering



Run Number: 162620, Event Number: 16060241

Date: 2010-08-24 19:45:23 CEST



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(as opposed to consider jets as monolithic objects)

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- boosted jet tagging (now a common search tool)
- entered the field of Heavy-Ion collisions
- rich QCD phenomenology
- precision calculations at the LHC
- many conceptual ideas

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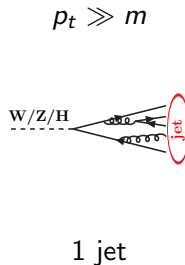
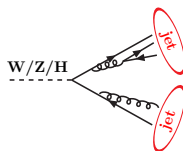
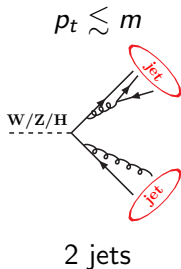
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This talk: give you a hint of all these aspects

Boosted objects and searches

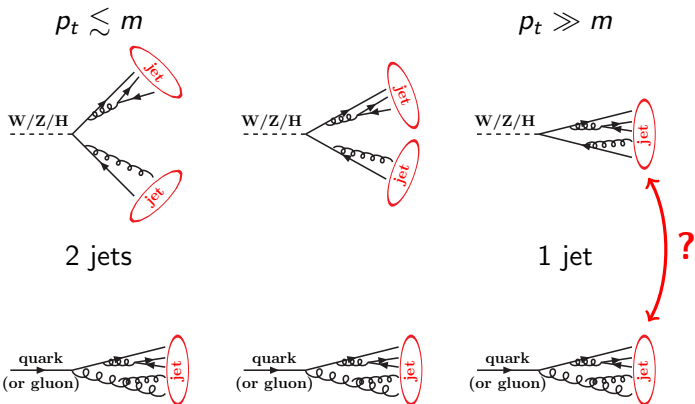
Boosted objects



(massive) objects produced boosted (energy $\gg$ mass) are seen as 1 jet:

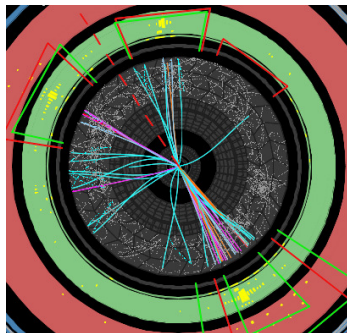
$$\theta_{q\bar{q}} \sim \frac{m}{p_t}$$

Boosted objects



use substructure to separate from QCD jets

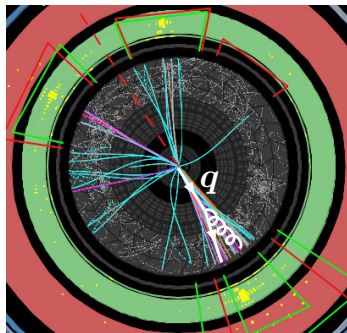
What jet do we have here?



Other examples

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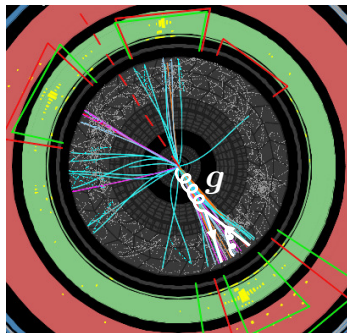
- a quark?



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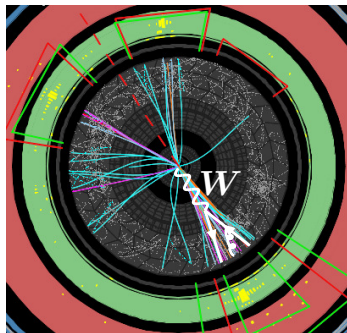
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Other examples

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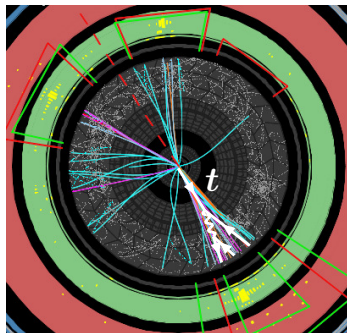
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- a W/Z (or a Higgs)?



Other examples

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- a gluon?
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- a top quark?

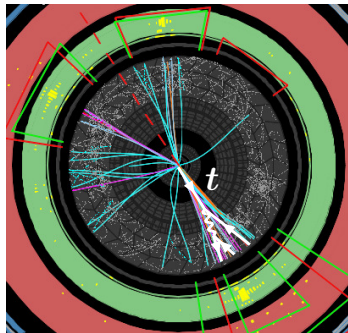


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Source: ATLAS boosted top candidate

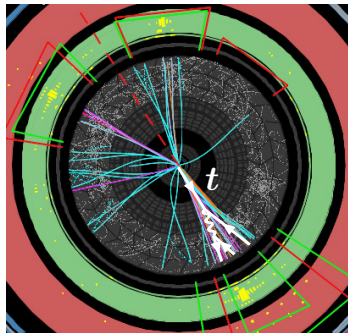


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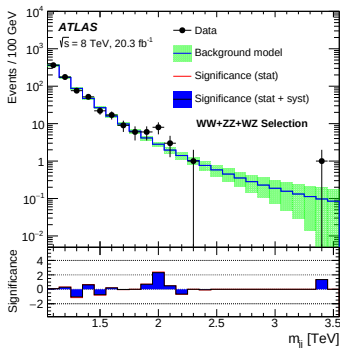
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Many applications, all relevant to new physics searches:

- 2-pronged decay: $W/Z \rightarrow q\bar{q}$, $H \rightarrow b\bar{b}$
- 3-pronged decay: $t \rightarrow qq\bar{b}$, $\tilde{\chi} \rightarrow qq\bar{q}$
- quark-gluon discrimination
- more exotic signatures

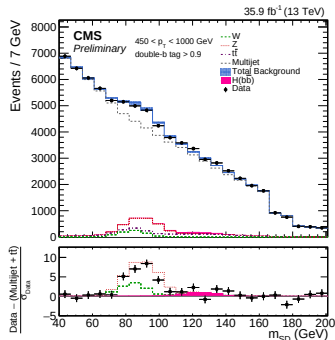
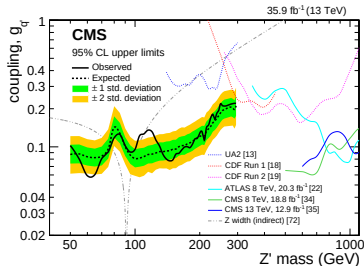
Searches and measurements



↑ (now-gone) di-boson excess (end of Run-I)

↗ Search for $X \rightarrow q\bar{q}$
 Region inaccessible otherwise

→ Clear Z peak, hint of a H peak



Conceptual ideas

Like a kid in a candy store

Compared to standard jets, substructure uses a **large toolkit**

- all kinds of jet algorithms

anti- k_t , Cambridge/Aachen (ang-ordered), k_t , generalised k_t , winner-takes-all recomb., ...

- tools to find peaks in jets

(modified) mass-drop, soft-drop, trimming, JHTopTagger, ...

- tools to quantify radiation patterns in jets

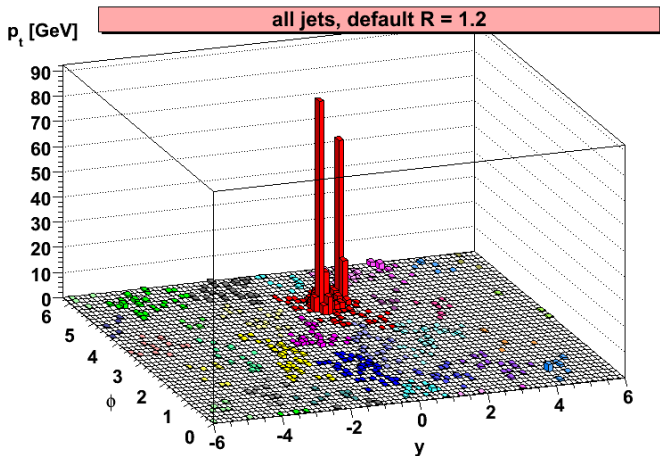
N -subjettiness, energy-correlation functions, planar flow, ...

Active field for developing/studying new tools , combining them,...

Requires both some creativity and some control over the underlying physics

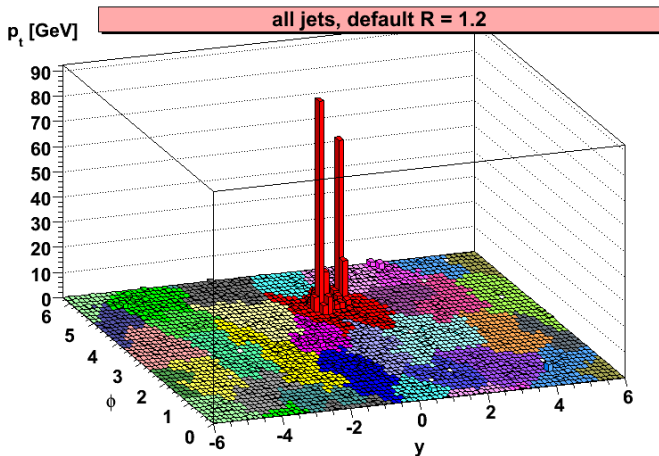
Search hard components: mMDT/SD

[J.Butterworth,A.Davison,M.Rubin,G.Salam,08]

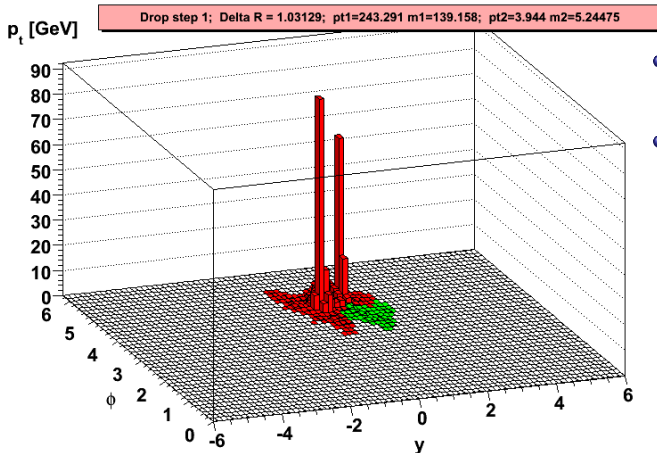


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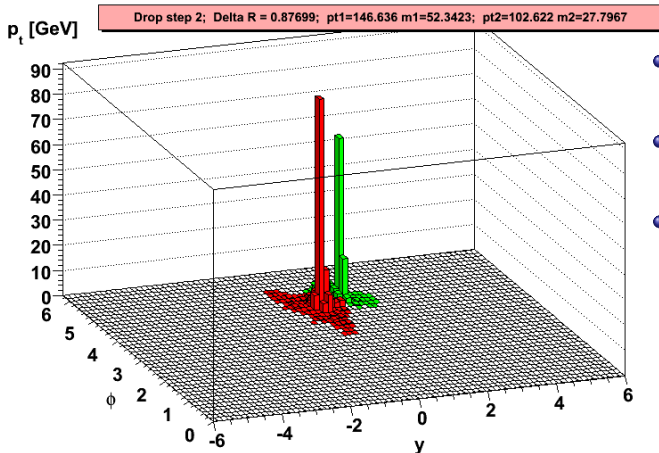
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MassDrop

- undo the last clustering step
- $z = 0.016 < 0.1$
carry on

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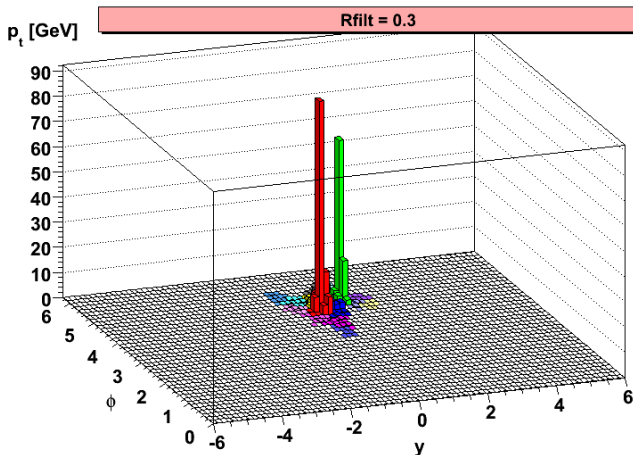


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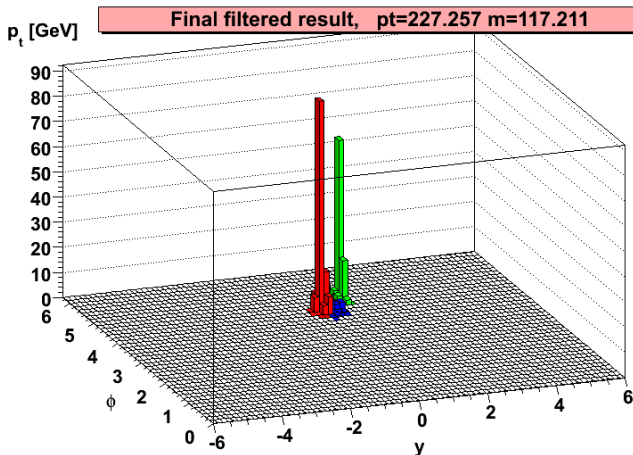
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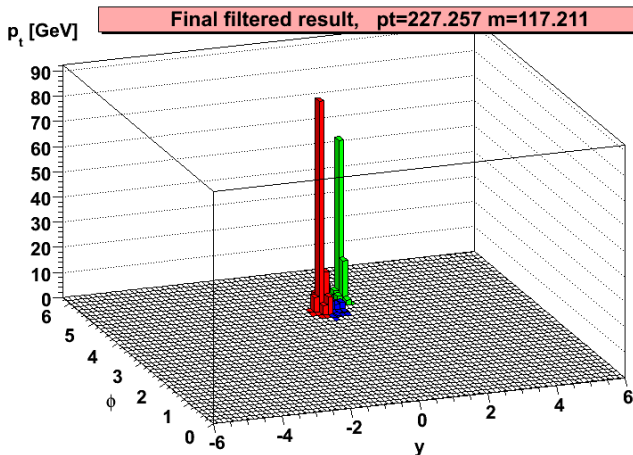
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Variant: **SoftDrop**: impose $z > z_{\text{cut}} \theta^\beta$

[A.Larkoski,S.Marzani,GS,J.Thaler,14]

Study radiation: N -subjettiness

Given N axes/prongs in a jet (axes)

[$\neq$ options, e.g. k_t subjets]

$$\tau_N^{(\beta)} = \frac{1}{p_T R^\beta} \sum_{i \in \text{jet}} p_{t,i} \min(\theta_{i,a_1}^\beta, \dots, \theta_{i,a_n}^\beta)$$

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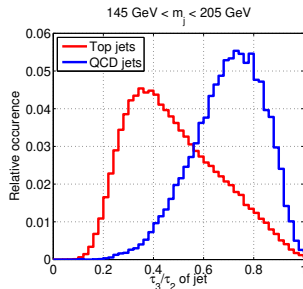
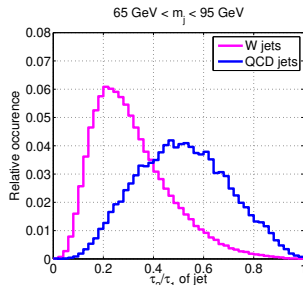
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- Measures the radiation from N prongs
- $\tau_{N,N-1} = \tau_N / \tau_{N-1}$ discriminates N -prong v. QCD
- τ_{21} smaller for W than for QCD
- τ_{32} smaller for top than for QCD

Several alternatives similar to τ_N



Machine Learning has become a major player

- Many architectures:

 - ANN Artificial Neural Network

 - DNN Dense Neural Network

 - CNN Convolutional Neural Network

 - GANN Generative Adversarial Neural Network

 - LSTM Long Short-Term Memory Neural Network

- Many approaches:

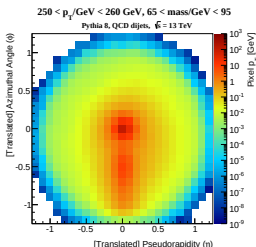
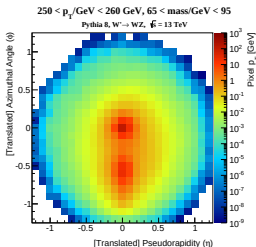
Feed jet variables, jet constituents, jet images, ...

- Many applications:

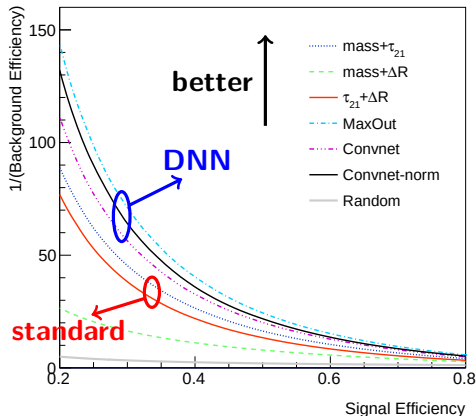
q/g , b , W , H , t tagging, pileup-mitigation, detector sim, ...

Latest playground: deep learning

Example 1: jet image for W vs. QCD jets using Convolutional/Dense NN



$250 < p_T/\text{GeV} < 300 \text{ GeV}$, $65 < \text{mass}/\text{GeV} < 95$
 $\sqrt{s} = 13 \text{ TeV}$, Pythia 8



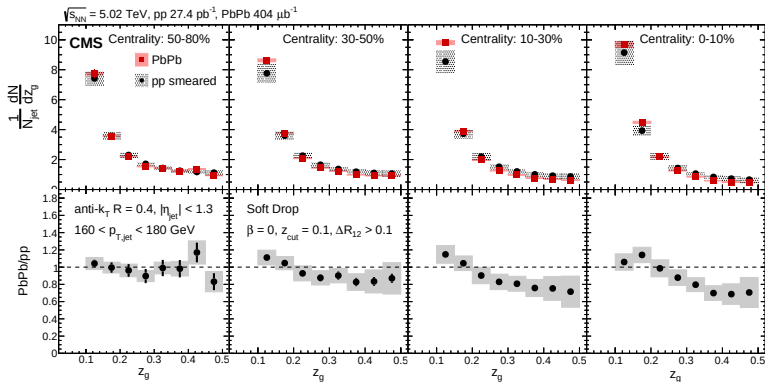
Improvement compared to standard approach

Heavy-Ion collisions

Measuring the splitting function

- Take a jet with large p_t
- apply mMDT $\rightarrow$ hard splitting
- $z_g \equiv$ mom fraction of that splitting

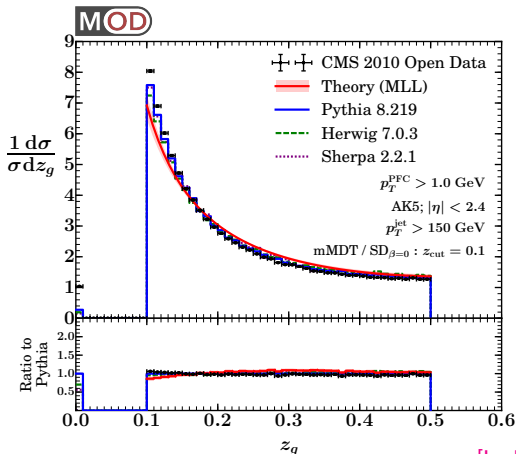
Measurement in *PbPb* shows quenching effects



Expect more to come in the (near) future...

Measuring the splitting function

First “analysis” using CMS Open Data



- Open data is a heated debate
- many interesting possibilities (incl. substructure)

[Larkoski,Marzani,Thaler,Thipathee,Xue,17]

Rich QCD phenomenology

Substructure from first principles (1/2)

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Main benefits of a first-principles understanding:

- ▶ understanding the dynamics at play in jet kinematics (example later)
- ▶ understand similarities and differences between methods
e.g. trimming, pruning, mMDT similar at large mass, differ at low mass
- ▶ adjust substructure tools for better performance (e.g. *modified* MDT)
- ▶ understand parametric dependence, e.g. p_t (without generators)
- ▶ highlight a trade-off between performance and model-independence

Substructure from first principles (2/2)

- Several interesting directions (all overviewed below)
 - ▶ Understanding how the methods work
 - ▶ Building improved tools
 - ▶ Precision QCD at the LHC
 - ▶ Funny structures in pQCD

Substructure from first principles (2/2)

- Several interesting directions (all overviewed below)

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- Substantial progress in understanding substructure, e.g.:

	peak finder	radiation
$W/Z/H$	mMDT, trimming, pruning Dasgupta,Fregoso,Marzani,Salam,13 SoftDrop Larkoski,Marzani,GS,Thaler,14	$\tau_{21}^{(\beta=2)}, \mu^2, D_2^{(\beta=2)}$ Dasgupta,Schunk,GS,15 $D_2^{(\beta)}$ Larkoski,Moult,Neill,15-16
top	CMSTopTagger, Y-splitter Dasgupta,Guzzi,Rawling,GS,soon	next task Cacciari,Napoletano,GS,Stagnitto,18-20

- Main idea:

Boosted jet $\Rightarrow p_t \gg m$

$$\Rightarrow \rho \equiv \frac{m^2}{p_t^2 R^2} \ll 1$$

$\Rightarrow$ expect $\log \rho$ coming with α_s

$\Rightarrow$ need for all-order resummation

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Boosted jet $\Rightarrow p_t \gg m$

$$\Rightarrow \rho \equiv \frac{m^2}{p_t^2 R^2} \ll 1$$

$\Rightarrow$ expect $\log \rho$ coming with α_s

$\Rightarrow$ need for all-order resummation

- Example: jet mass with one (soft-and-collinear) gluon emission

$$\begin{aligned} \text{Prob}_1(> \rho) &\simeq \int_0^1 \frac{d\theta^2}{\theta^2} \frac{dz}{z} \frac{\alpha_s C_R}{\pi} \Theta(z\theta^2 > \rho) \\ &\simeq \frac{\alpha_s C_R}{2\pi} \log^2(1/\rho) \end{aligned}$$



Resummation's kingdom

- (plain) jet mass again:

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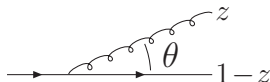
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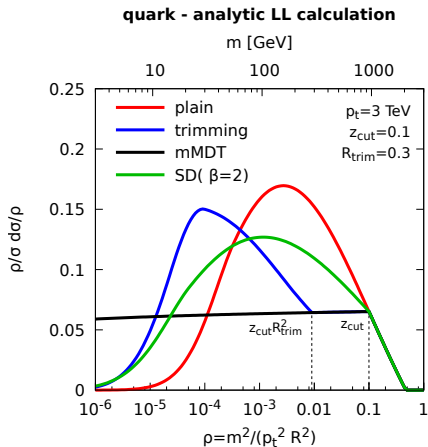
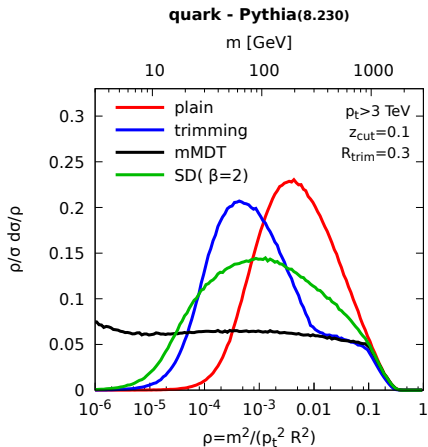
- all-order result (Leading-Log):

$$\text{Prob}_{\text{LL}}(< \rho) = \exp[-\text{Prob}_1(< \rho)]$$

Understanding substructure tools

[M.Dasgupta, A.Fregoso S.Marzani, G.Salam, 13]

[A.Larkoski, S.Marzani, GS, J.Thaler, 14]

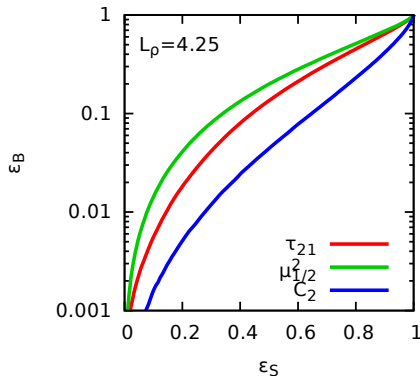


qualitative features reproduced and understood

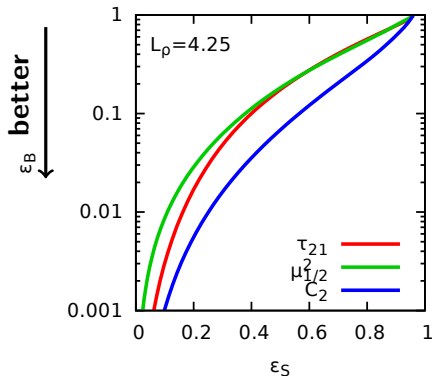
Understanding substructure tools (cont'd)

[M.Dasgupta, L.Schunk, GS, 15]

Pythia8(FSR)



analytic



qualitative features reproduced and understood

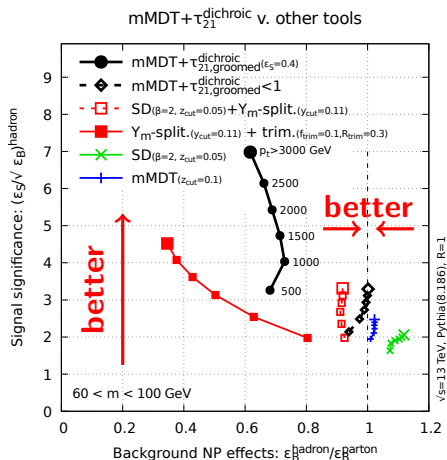
Improving substructure tools

More recently: **use acquired understanding to develop improved tools**

Examples:

- **Y -splitter+grooming**
Dasgupta,Powling,Schunk,GS,16
- **New angles on ECFs**
Moult,Necib,Thaler,16
- **Dichroic N -subjettiness**
Salam,Schunk,GS,16

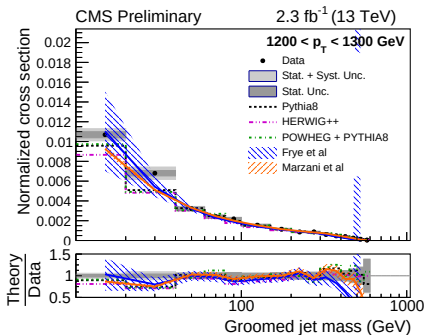
Certainly more of these in the future!



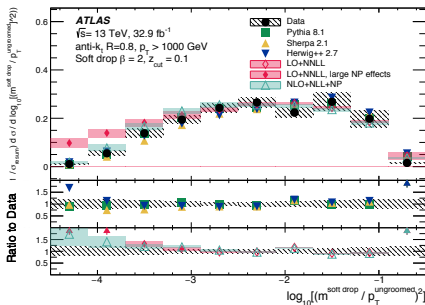
- tools like mMDT and Soft Drop cut soft radiation at large angles
 - ⇒ only sensitive to collinear branchings
 - ⇒ process-independent
 - ⇒ j in jj same as in Wj or Zj , ...
 - ⇒ small non-perturbative corrections
 - ⇒ amenable to precise calculations
- Recent precise calculations of the mMDDT/SD jet mass:
 - ▶ NNLL+LO in SCET (Frye, Larkoski, Schwartz, Yan)
 - ▶ NLL+NLO in “standard QCD” (Marzani, Schunk, GS)

Measurements at the LHC:

CMS-PAS-SMP-16-010



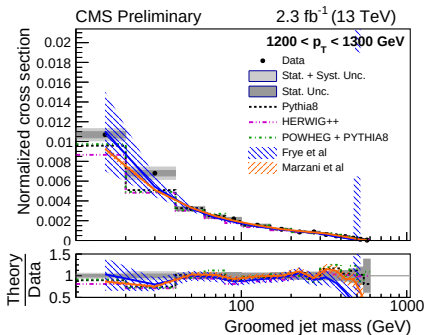
ATLAS(CERN-EP-2017-231)



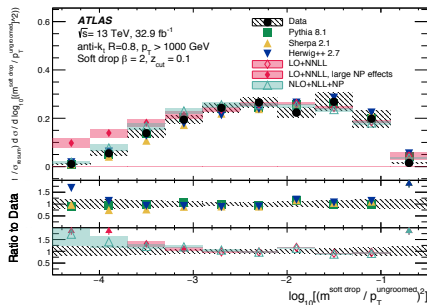
good overall agreement with the data

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Precise observable with limited sensitivity to NP effects

⇒ **possibility to extract α_S** (on-going study)

Curiosities (1/2): Sudakov safety

Some observables are ill-defined in fixed-order pQCD:

- z_g not defined at $\mathcal{O}(\alpha_s^0)$ (only 1 particle in the jet)
- many ratios v_2/v_1 (like $\tau_{21} = \tau_2/\tau_1$) have $v_2 = v_1 = 0$ at $\mathcal{O}(\alpha_s^0)$
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but can still be computed perturbatively thanks to resummation

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but can still be computed perturbatively thanks to resummation

Example: $r = e_\alpha/e_\beta$ with $e_\alpha = \sum_{i \in \text{jet}} z_i \theta_{i,\text{jet}}^\alpha$

We can write

$$\frac{dP}{dr} = \int de_\alpha de_\beta \frac{dP}{de_\alpha} \frac{dP}{de_\beta} \delta(r - e_\alpha/e_\beta)$$

Idea: the dangerous case $e_\beta = 0$ is absent because $\frac{dP}{de_\beta} \rightarrow 0$ in that limit (Sudakov exponential)

Curiosities (1/2): Sudakov safety

Some observables are ill-defined in fixed-order pQCD:

- z_g not defined at $\mathcal{O}(\alpha_s^0)$ (only 1 particle in the jet)
- many ratios v_2/v_1 (like $\tau_{21} = \tau_2/\tau_1$) have $v_2 = v_1 = 0$ at $\mathcal{O}(\alpha_s^0)$
- some observables are ill-defined at any fixed order (see next slide)

but can still be computed perturbatively thanks to resummation

Example: $r = e_\alpha/e_\beta$ with $e_\alpha = \sum_{i \in \text{jet}} z_i \theta_{i,\text{jet}}^\alpha$

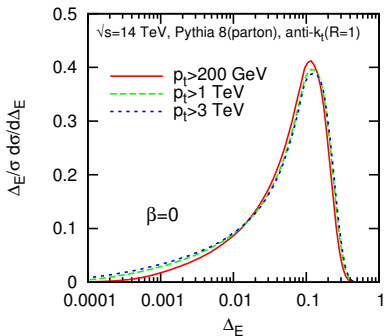
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A series of interesting results
still many unknown to be explored

Curiosities (2/2): α_s independence



LL result: $\text{Prob}(< \Delta) = \frac{\log(z_{\text{cut}}) + \frac{3}{4}}{\log(\Delta) + \frac{3}{4}}$

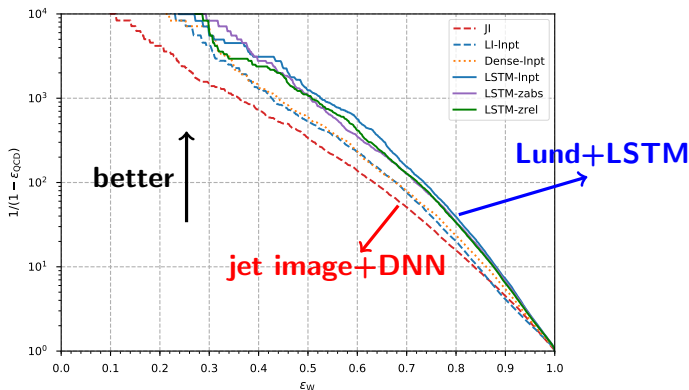
- What are we looking at?

- ▶ jet with momentum $p_{t,\text{jet}}$
- ▶ apply mMDT
- ▶ after, $p_t = p_{t,\text{mMDT}}$
- ▶ measure $\Delta = \frac{p_{t,\text{jet}} - p_{t,\text{mMDT}}}{p_{t,\text{jet}}}$
i.e. the lost p_t fraction

- Result:

at LL and fixed coupling, the Δ distribution is α_s -independent

[F.Dreyer,G.Salam,GS, soon]



QCD-motivated input to LSTM network shows great performance

Jet substructure has gained a lot of importance in the past decade

- Important tool for LHC physics
- exciting pQCD phenomenology
 - ▶ understanding and development of tools
 - ▶ precision pheno at the LHC
 - ▶ interesting structure emerging
- Expansion towards new horizons:
 - ▶ heavy-ion hard probes
 - ▶ machine learning

BOOST Annual meeting
around 100 theorists and experimentalists discussing
discussing latest progress in substructure

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July 16-20: BOOST 2018 in Paris

<https://indico.cern.ch/e/boost2018>

