

Jet finding at the LHC era

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in collaboration with G. Salam, M. Cacciari and J. Rojo arXiv:0704:0292, arXiv:0802:1188, arXiv:0802:1189, arXiv:0803.0678 + works in preparation

Plan

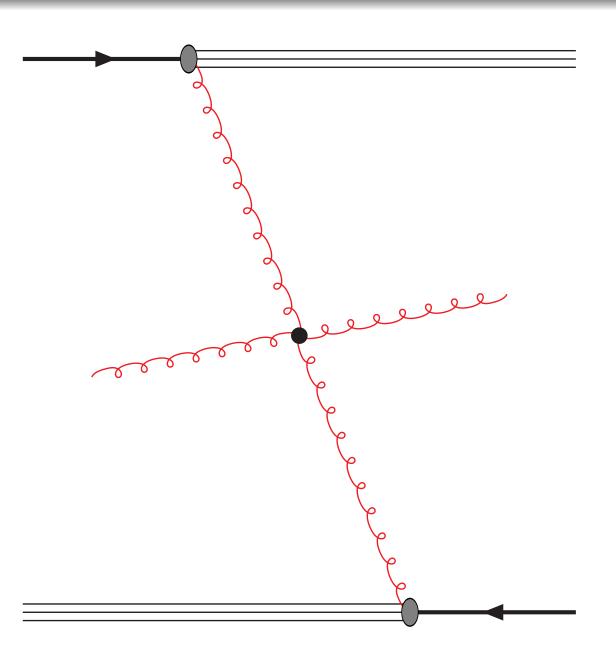


- Foreword: why jets? what are they? introducing the basic concepts
- Part 1: recent progresses in building a solid toolkit jet definitions meeting the fundamental requirements
- Part 2: jets in pp collisions
 - Choosing the adapted jet definition which jet algorithm is best suited?
 - Subtracting pileup background using jet areas
 - defining areas
 - analytic control
 - using them for pileup subtraction



Foreword: why jets? what are they?



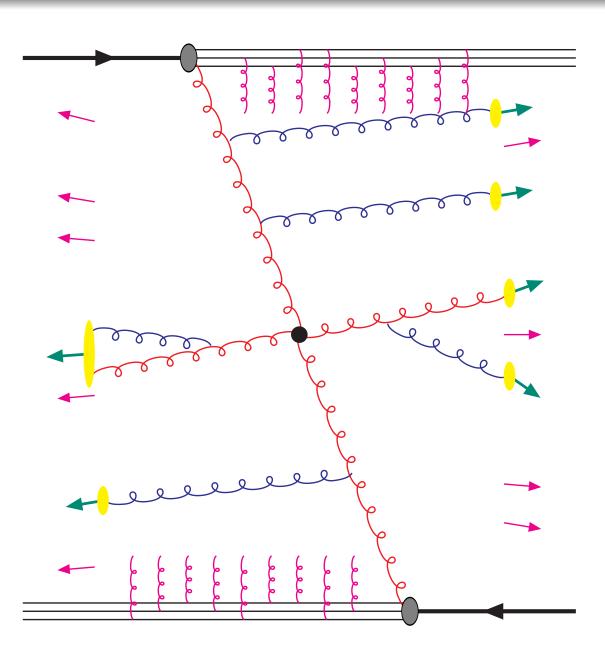


Hard scattering $(2 \rightarrow n)$

computed exactly at $\mathcal{O}(\alpha_s^p)$

$$egin{align} gg
ightarrow gg, gg
ightarrow ggg, \ gg
ightarrow gggg, \ gg
ightarrow H
ightarrow bar{b}, \ gg
ightarrow tar{t}
ightarrow \mu
u_{\mu}bar{b}qar{q}, \ gg
ightarrow Z'
ightarrow qar{q}, \ldots \ \end{array}$$





Hard scattering $(2 \rightarrow n)$

Parton level

 \approx resummed collinear div.

$$\sum_i \alpha_s^i \log^i(p_t^2/\mu^2)$$

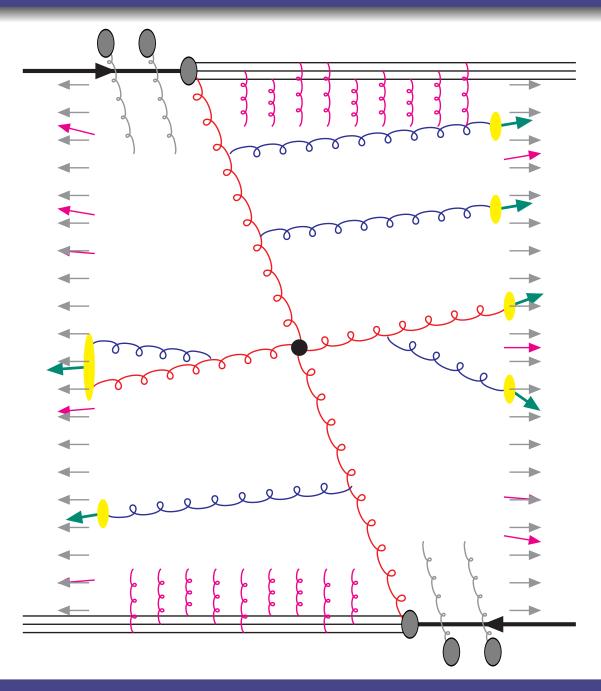
Hadron level: hadronisation

Underlying event

beam remnants interactions

⇒ soft background





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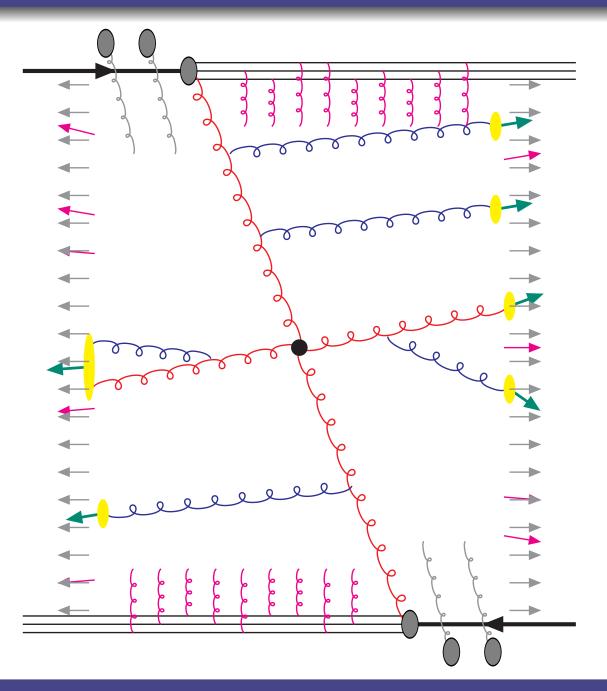
beam remnants interactions

⇒ soft background

Pileup

≈ uniform soft background





Hard scattering $(2 \rightarrow n)$

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Underlying event

beam remnants interactions

⇒ soft background

Pileup

pprox uniform soft background

"Jets" ≡ hard partons

Parton ambiguous

⇒ multiple jet definitions

Two classes of algorithms



Class 1: recombination	Cass 2: cone
Successive recombinations of the	find directions of energy flow
"closest" $^{(a)}$ pair of particle	\equiv stable cones $^{(b)}$
Nice perturbative behaviour	Small sensitivity to soft radiation (UE,PU)
Often used in $e^{\pm}e^{\pm}$, $e^{\pm}p$	Often used in pp

(a) <u>Distance</u>: (stop when $d_{\min} > R$)

$$k_t$$
: $d_{i,j} = \min(k_{t,i}^2, k_{t,j}^2)(\Delta \phi_{i,j}^2 + \Delta y_{i,j}^2)$

Aachen/Cam.:
$$d_{i,j} = \Delta \phi_{i,j}^2 + \Delta y_{i,j}^2$$

 $^{(b)}$ stable cones (radius R) such that: the total momentum of its contents points in the direction of its centre

How the cone works...



- Seeded (iterative) approaches: iterate from an initial position until stable
 - seed = initial particle
 - seed = midpoint between stable cones found at first step
- One has to deal with overlapping stable cones: 2 subclasses

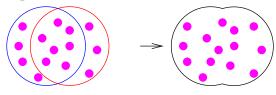
How the cone works...



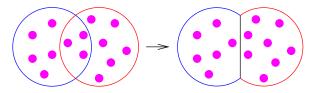
- Seeded (iterative) approaches: iterate from an initial position until stable
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Class 2(a): cone with split-merge (ex.: JetClu, Atlas, MidPoint):

$$\tilde{p}_{t, \mathrm{shared}} > f \tilde{p}_{t, \mathrm{min}}$$



$$\tilde{p}_{t, \mathrm{shared}} \leq f \tilde{p}_{t, \mathrm{min}}$$



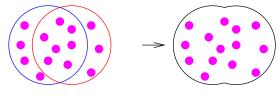
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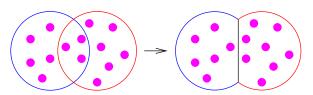
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$$\tilde{p}_{t, \text{shared}} \leq f \tilde{p}_{t, \text{min}}$$



Class 2(b): cone with progressive removal (ex.: Iterative Cone)

- iterate from the hardest seed
- remove the stable cone as a jet and start again

Idea: "regular/circular" jets

20th century jet finders



Recombination:

- k_t algorithm
- Cambridge/Aachen alg.

Cone:

- CDF JetClu
- CDF MidPoint
- D0 (run II) Cone
- PxCone
- ATLAS Cone
- CMS Iterative Cone
- PyCell/CellJet
- GetJet



Part 1 21st century: towards a solid toolkit

1990: fixing the rules



SNOWMASS accords, Tevatron 1990 (i.e. old!):

Several important properties that should be met by a jet definition are [3]:

- 1. Simple to implement in an experimental analysis;
- Simple to implement in the theoretical calculation;
- 3. Defined at any order of perturbation theory;
- 4. Yields finite cross section at any order of perturbation theory;
- 5. Yields a cross section that is relatively insensitive to hadronization.

i.e. usable by theoreticians (*e.g.* finite perturbative results) and experimentalists (*e.g.* fast enough, not much UE sensitivity)

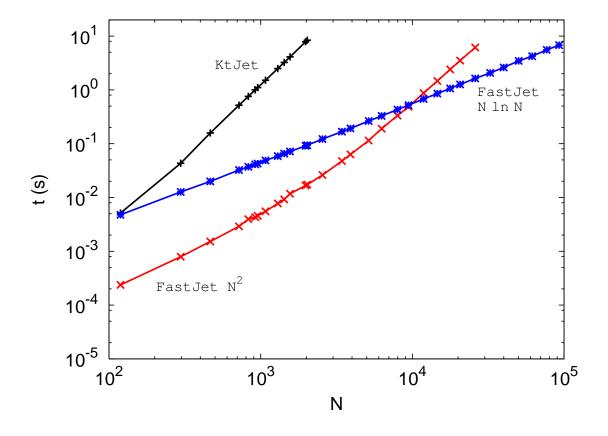
Speed improvement



[M. Cacciari, G. Salam, 06]

Speeding up the k_t and Cam/Aachen algorithms

- **●** using computational-geometry techniques: $\mathcal{O}\left(N^3\right) \to \mathcal{O}\left(N \log N\right)$
- C++ implementation in FastJet



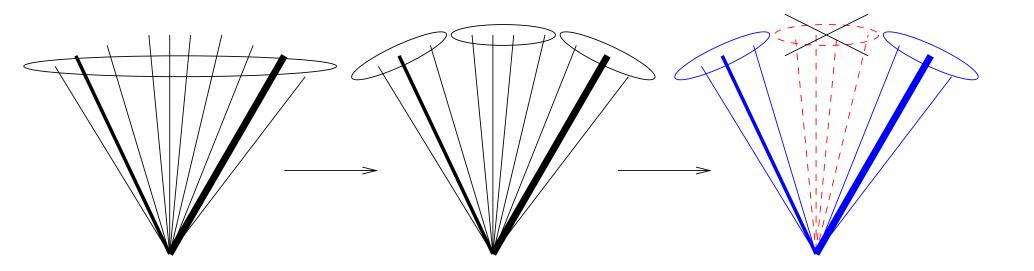
Filtering using jet substructure



More refined clustering ("2nd generation of algorithms")

Cambridge+Filtering algorithm:

- Cluster with Aachen/Cambridge and radius R
- For each jet, recluster it with Aachen/Cambridge and radius $R_{\rm sub}$ keep only $n_{\rm sub}$ hardest sub-jets of the initial jet



Filtering using jet substructure



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Aim: remove the soft background

Properties:

ullet Proven to improve jet reconstruction, in H o bar b

[J.Butterworth, A.Davison, M.Rubin, G.Salam, 08]

- Additional parameters that deserve appropriate studies
- We will use the simplest choice: $R_{\rm sub}=R/2$, $n_{\rm sub}=2$

QCD divergences



QCD probability for gluon bremsstrahlung at angle θ and \perp -mom. k_t :

$$dP \propto \alpha_s \, \frac{d\theta}{\theta} \, \frac{dk_t}{k_t}$$

Two divergences:



Collinear

$$p_t \longrightarrow k_t \ll p_t$$

Soft

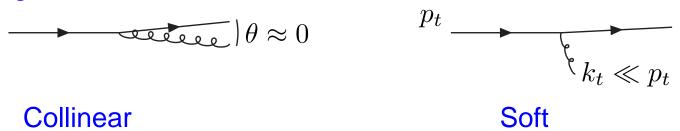
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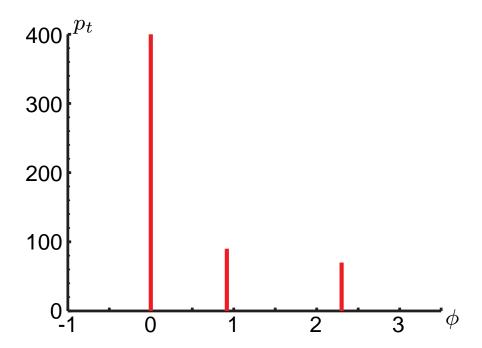
Two divergences:



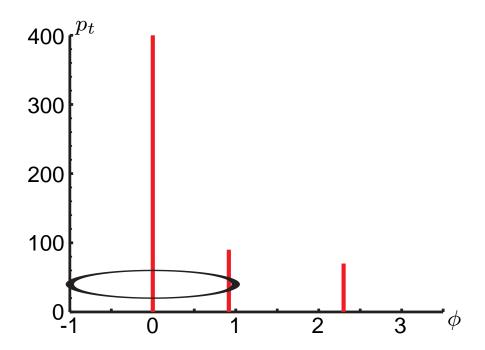
For pQCD to make sense, the (hard) jets should not change when

- one has a collinear splitting i.e. replaces one parton by two at the same place (η, ϕ)
- one has a soft emission i.e. adds a very soft gluon

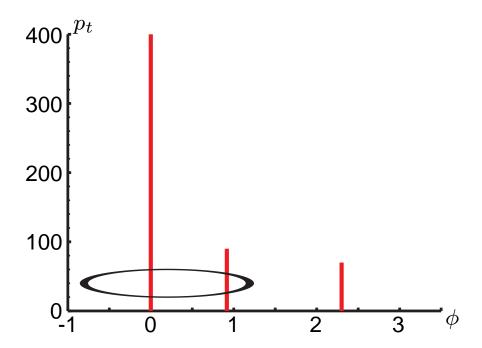




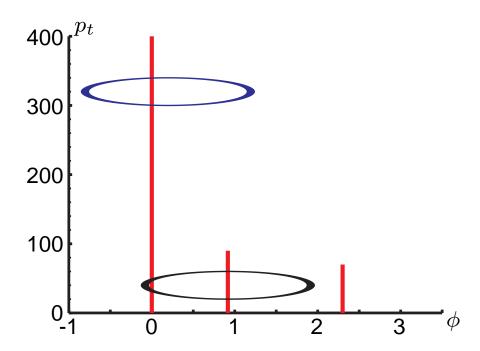




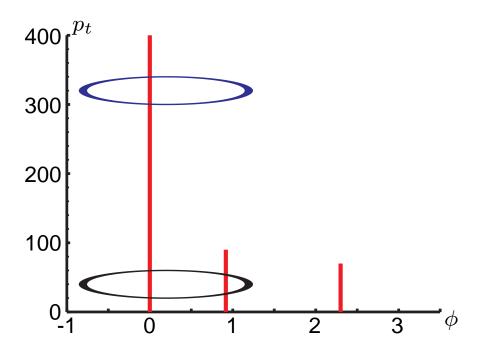




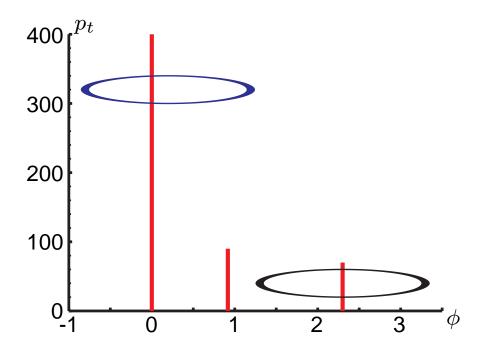




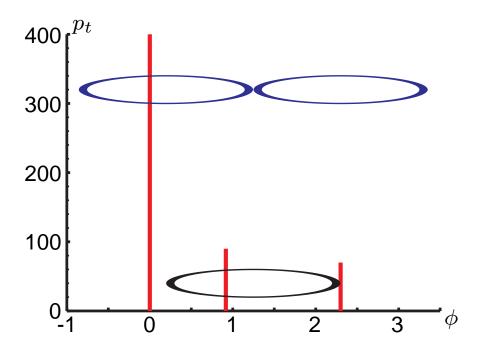




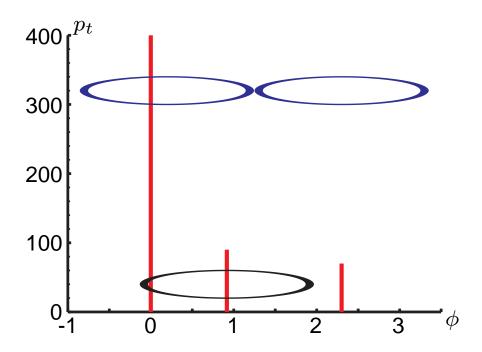




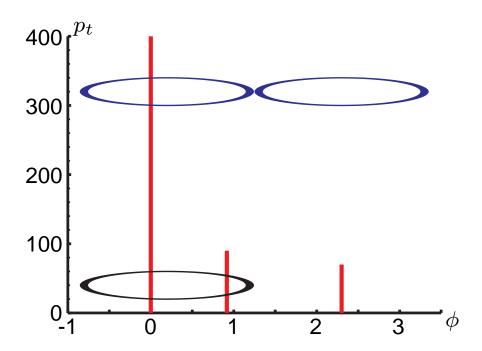




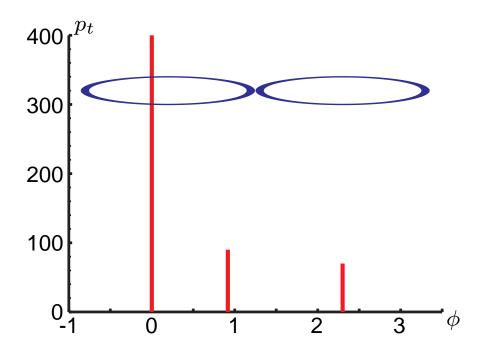


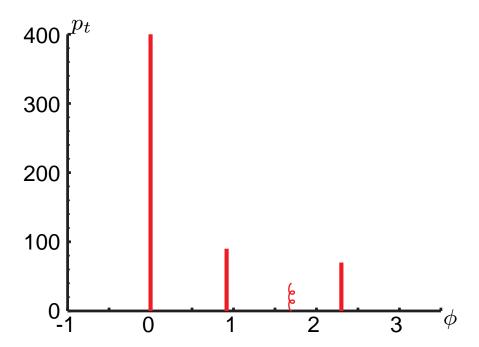




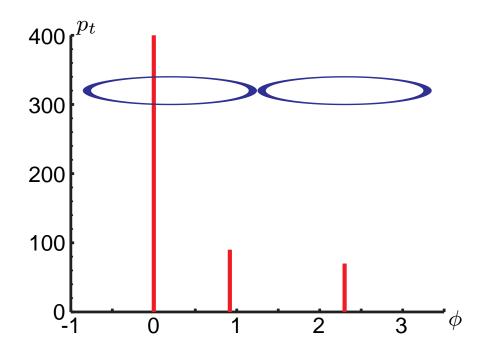


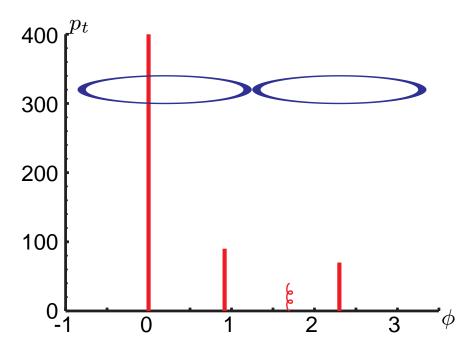




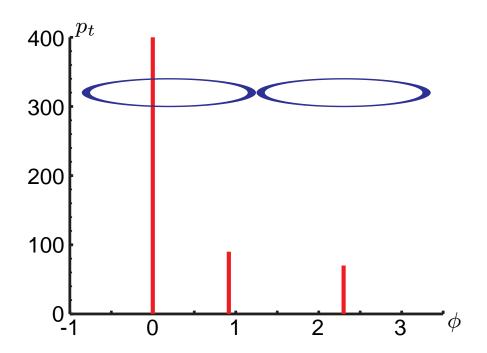


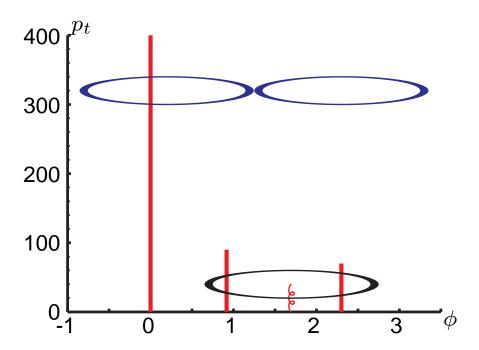




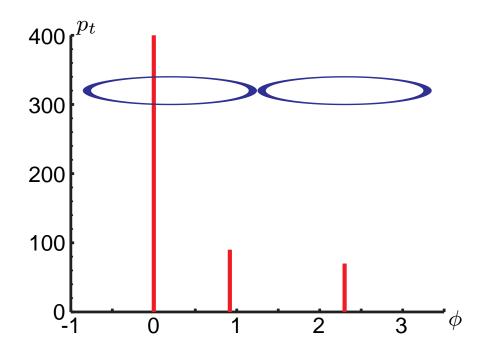


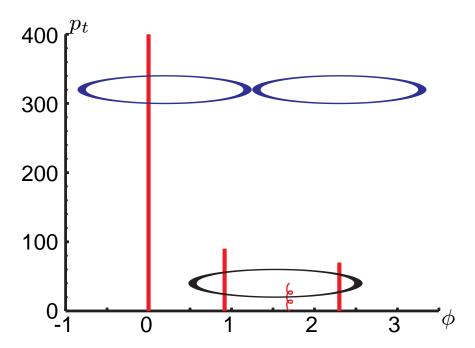




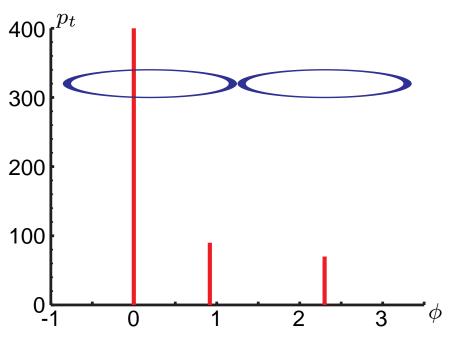


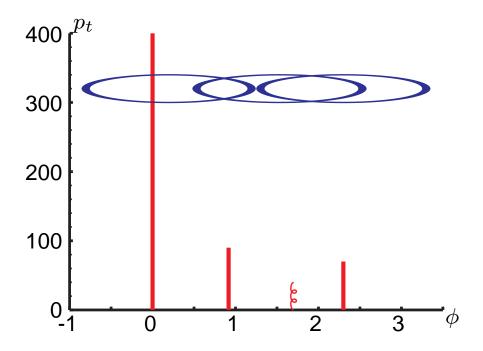












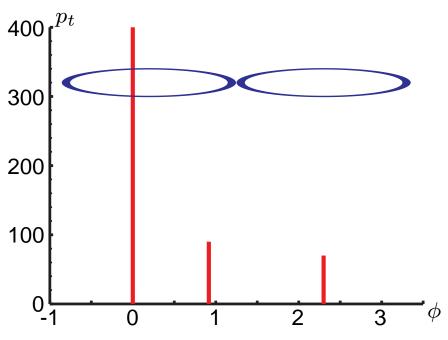
Stable cones:

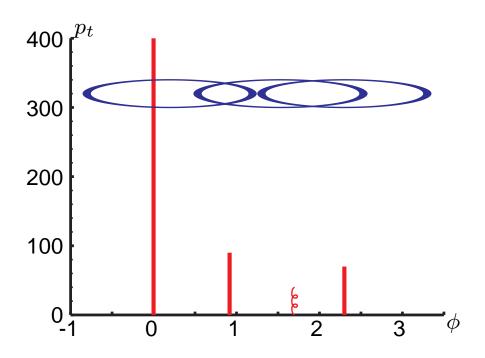
Midpoint:

{1,2} & {3}

{1,2} & {3} & {2,3}







Stable cones:

Midpoint:

{1,2} & {3}

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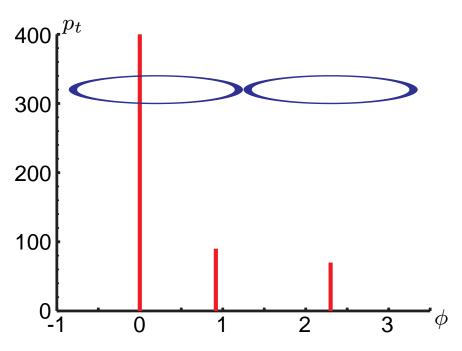
Jets: (f = 0.5)

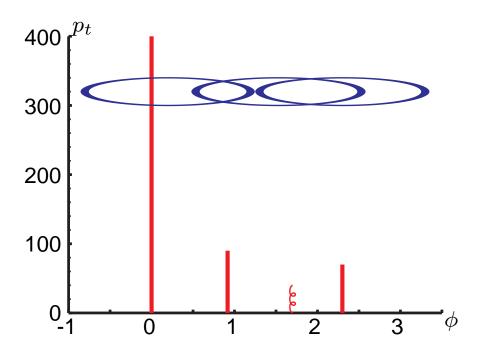
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{1,2,3}







Stable cones:

Midpoint:

Seedless:

Jets: (f = 0.5)

Midpoint:

Seedless:

{1,2} & {3}

{1,2,3}

{1,2,3}

{1,2,3}

Stable cone missed — IR unsafety of the midpoint algorithm

Solution: SISCone



- Solution: use a seedless approach, find ALL stable cones
- Naive approach: check stability of each subset of particle

Solution: SISCone



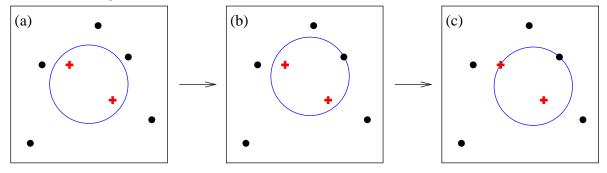
- Solution: use a seedless approach, find ALL stable cones
- Naive approach: check stability of each subset of particle Complexity is $\mathcal{O}\left(N2^N\right)$
 - \Rightarrow definitely unrealistic: 10^{17} years for N=100
- Midpoint complexity: $\mathcal{O}\left(N^3\right)$

Solution: SISCone



- Solution: use a seedless approach, find ALL stable cones
- Midpoint complexity: $\mathcal{O}\left(N^3\right)$

<u>Idea</u>: use geometric arguments



- Each enclosure can be moved (in any direction) until it touches a point
- ... then rotated until it touches a second one
- ⇒ Enumerate all pairs of particles with 2 circle orientations and 4 possible inclusion/exclusion
- → find all enclosures

Solution: SISCone



- Solution: use a seedless approach, find ALL stable cones
- Midpoint complexity: $\mathcal{O}\left(N^3\right)$

Idea: use geometric arguments

- ⇒ Enumerate all pairs of particles with 2 circle orientations and 4 possible inclusion/exclusion
- → find all enclosures
- Complexity: $\mathcal{O}\left(N^3\right)$, with improvements: $\mathcal{O}\left(N^2\log(N)\right)$

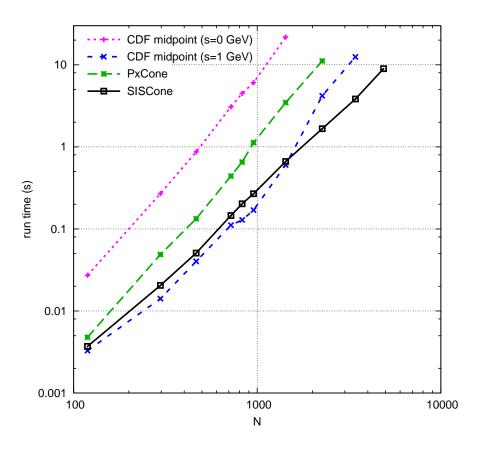
→ C++ implementation: Seedless Infrared-Safe Cone algorithm (SISCone) G.Salam, G.S., JHEP 04 (2007) 086; http://projects.hepforge.org/siscone

NB.: also available from FastJet [M.Cacciari, G.Salam, G.S.]; http://www.fastjet.fr

Physical impact



Execution timings:

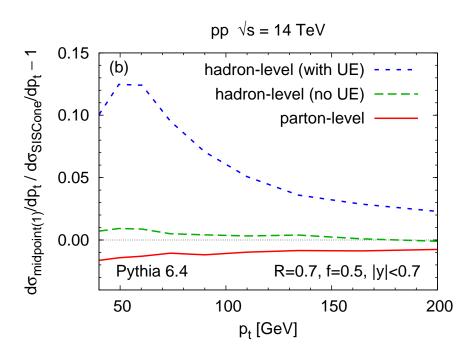


- faster than midpoint without seed threshold
- at least as fast as as midpoint with seed threshols

Physical impact (2)



(Midpoint-SISCone)/SISCone



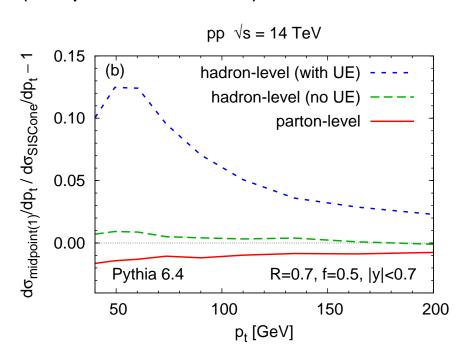
Inclusive cross-section:

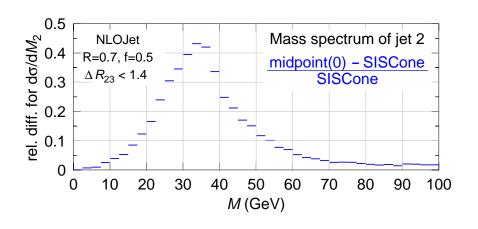
- effect of a few %
- less UE sensitivity

Physical impact (2)



(Midpoint-SISCone)/SISCone





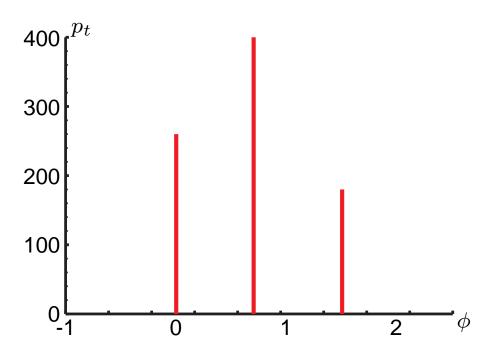
Inclusive cross-section:

- effect of a few %
- less UE sensitivity

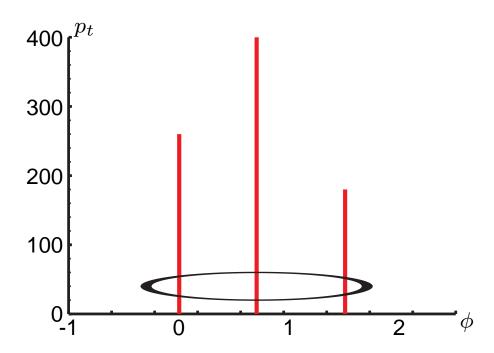
Masses in 3-jet events:

- effects $\sim 45\%$
- Important for LHC!

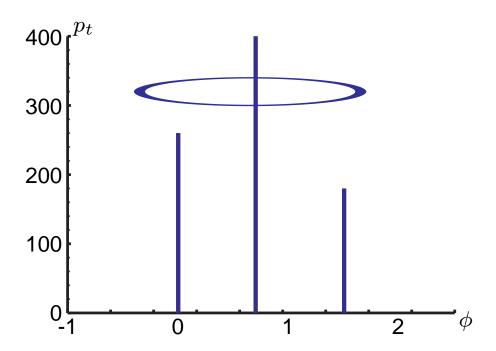




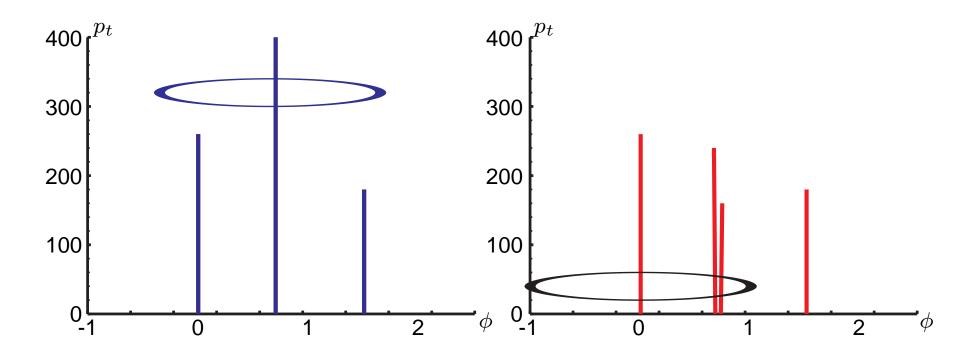




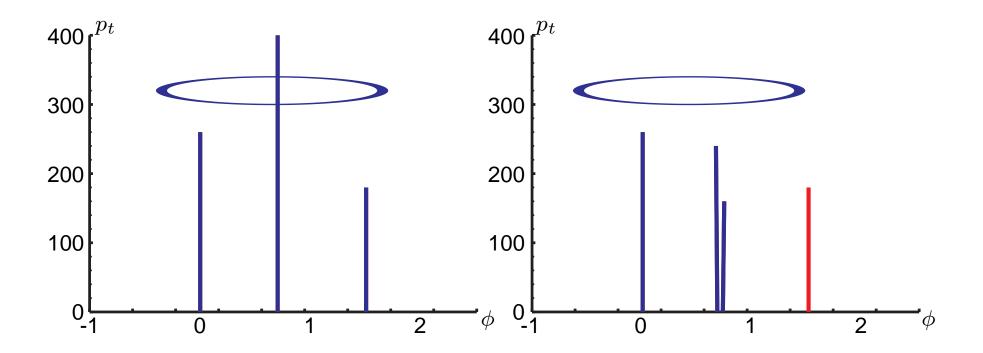




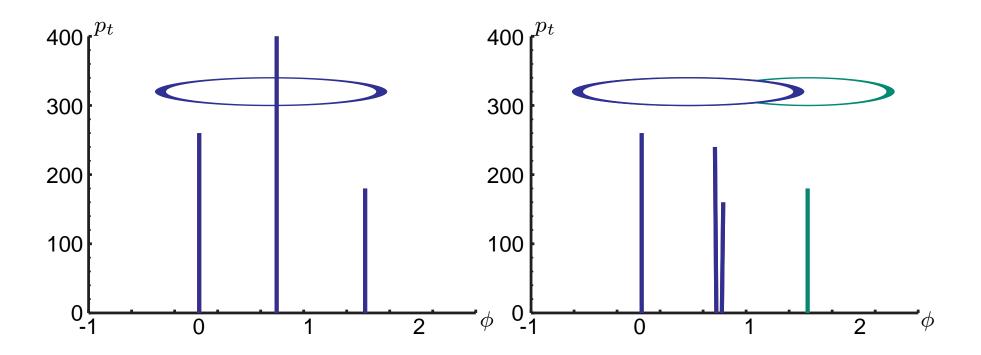




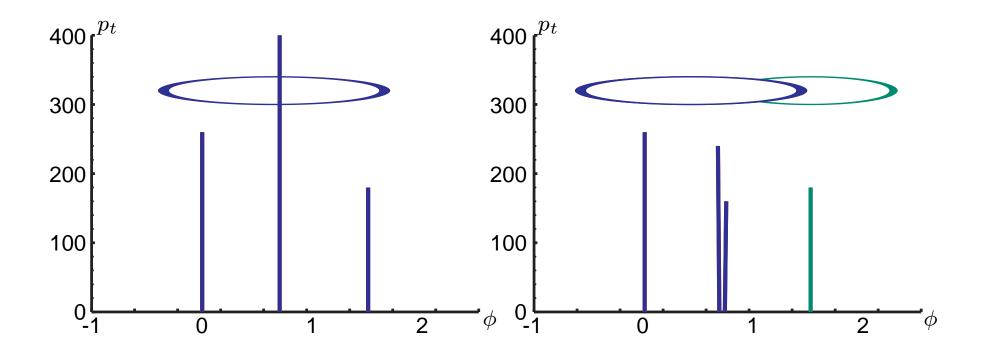












- Before collinear spliting: 1 jet
- After collinear spliting: 2 jets





Come back to recombination-type algorithms:

$$d_{ij} = \min(k_{t,i}^{2p}, k_{t,j}^{2p}) \left(\Delta \phi_{ij}^2 + \Delta \eta_{ij}^2\right)$$

- p=1: k_t algorithm
- p = 0: Aachen/Cambridge algorithm





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- p = 0: Aachen/Cambridge algorithm
- p = -1: anti- k_t algorithm [M.Cacciari, G.Salam, G.S.,JHEP 04 (08) 063]





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- p=-1: anti- k_t algorithm [M.Cacciari, G.Salam, G.S.,JHEP 04 (08) 063]

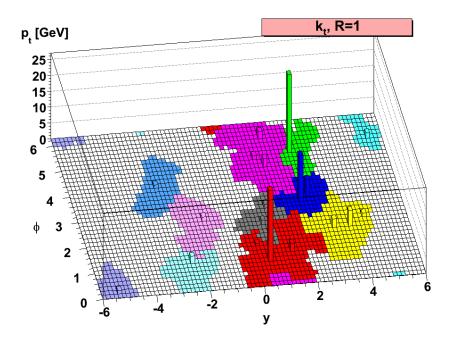
Why should that be related to the iterative cone?!?

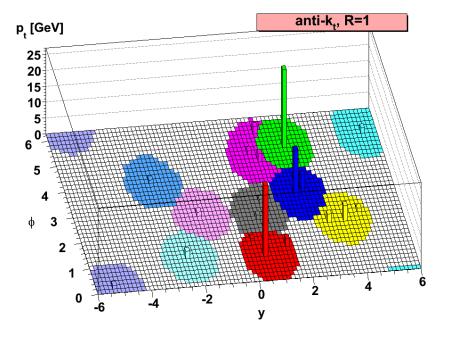
- "large $k_t \Rightarrow$ small distance" i.e. hard partons "eat" everything up to a distance Ri.e. circular/regular jets, jet borders unmodified by soft radiation
- infrared and collinear safe





Hard event + homogeneous soft background





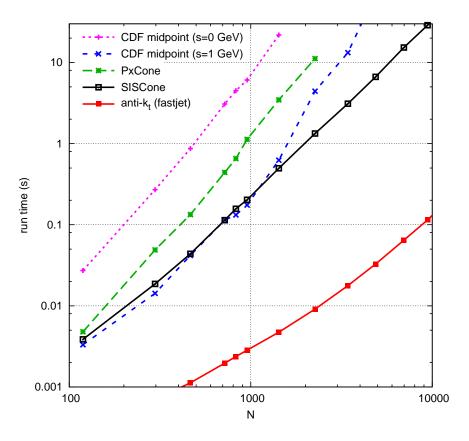
anti- k_t is soft-resilient

more later in this talk...





Execution timings:



As fast as the (fast) k_t ([M. Cacciari, G. Salam, 06])

21st century jet finders



Recombination:

- k_t algorithm
- Cambridge/Aachen alg.
- ullet anti- k_t algorithm -

4 available safe algorithms

All part of FastJet

[M.Cacciari, G.Salam, G.S.]

Cone:

- CDF JetClu
- CDF MidPoint
- D0 (run II) Cone
- PxCone
- ATLAS Cone
- CMS Iterative Cone
- ➤ PyCell/CellJet
- **GetJet**
- SISCone



Part 2 Jets in pp collisions Choosing the adapted jet definition

[M.Cacciari, J.Rojo, G.Salam. G.S., to appear]

Sample processes to study



We analyse 3 processes:

- $Z' \rightarrow q\bar{q} \rightarrow 2$ jets and $H \rightarrow gg \rightarrow 2$ jets:
 - simple environment: identify 2 jets and reconstruct $M_{Z',H}$ source of monochromatic quark/gluon jets scale dependence: mass of the Z'/H varied between 100 GeV and 4 TeV ficticious narrow Z',H
- $t\bar{t} \to W^+bW^-\bar{b} \to q\bar{q}bq\bar{q}\bar{b} \to 6$ jets:

complex environment: identify 6 jets and reconstruct 2 top balance between reconstruction efficiency and identification

with

- the 5 IRC-safe algorithms: k_t , Cambridge, anti- k_t , SISCone, Cam+filtering
- jet radius varied between 0.1 and 1.5

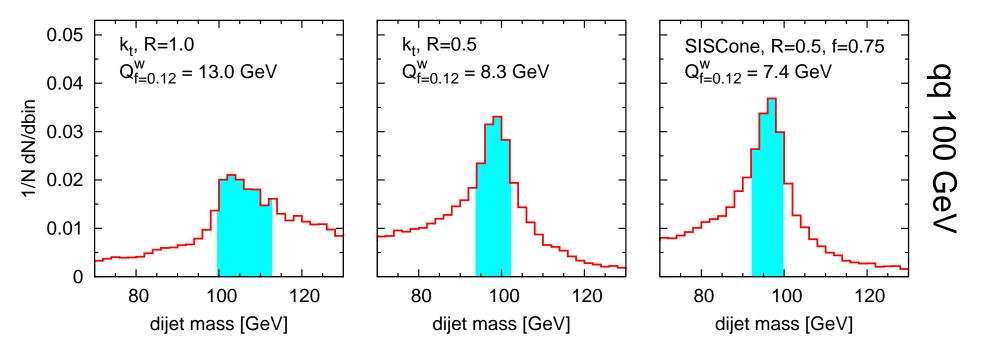


Measure of the jet reconstruction efficiency

- Forget about measures related to parton-jet matching,
 - use the reconstructed mass peak
- Forget about fits depending on the shape of the peak
- \Rightarrow maximise the signal over background ratio (S/\sqrt{B}) :



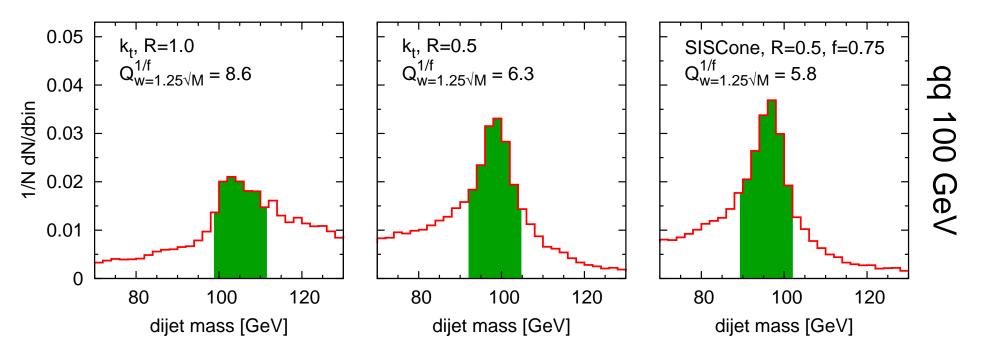
 $Q_{f=z}^w(JA,R)=$ minimal width of a window containing a fraction f=z of the events



Fixed signal, minimal width(background)



 $Q_f^{w=x\sqrt{M}}(JA,R) = \mbox{(1/) maximal number of events}$ in a window of width $x\sqrt{M}$



Maximal signal, fixed width(background)



- it intuitively does what it should
- relates to a signal significance (assuming constant background)

$$\frac{\Sigma(\mathrm{JD_1})}{\Sigma(\mathrm{JD_2})} = \left[\frac{N_{\mathrm{signal}}}{\sqrt{N_{\mathrm{bkg}}}}\right]_{\mathrm{JD}} = \sqrt{\frac{Q_{f=z}^w(\mathrm{JD_2})}{Q_{f=z}^w(\mathrm{JD_1})}} = \frac{Q_f^{w=x\sqrt{M}}(\mathrm{JD_2})}{Q_f^{w=x\sqrt{M}}(\mathrm{JD_1})}$$

minmimal $Q \equiv$ better signal-to-background ratio

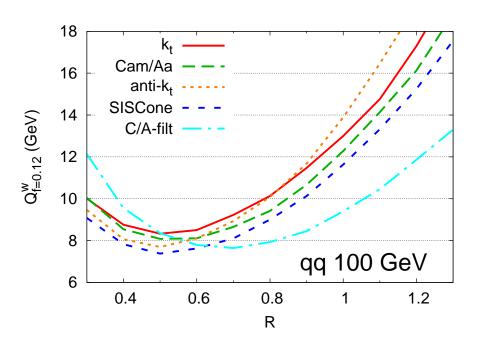
we can associate an effective luminosity ratio

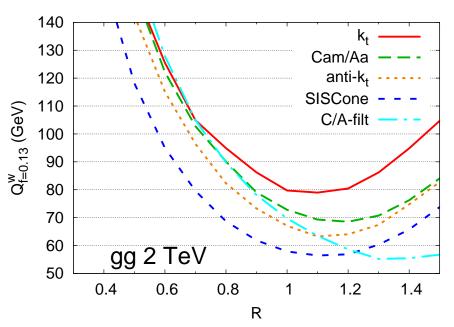
$$\rho_{\mathcal{L}} = \frac{\mathcal{L}_1}{\mathcal{L}_2} = \left[\frac{\Sigma(\mathrm{JD}_1)}{\Sigma(\mathrm{JD}_2)}\right]^2$$

e.g. if JD_1 has half the significance of JD_2 , it will require 4 times the integrated luminosity to achieve the same discriminative power.

Examples: best quality measures





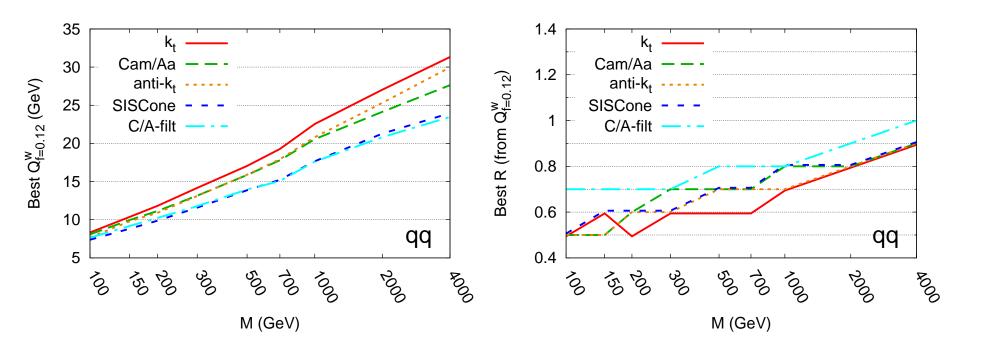


Allows to

- extract the best radius R_{best}
- compare the different algorithm

Best choices

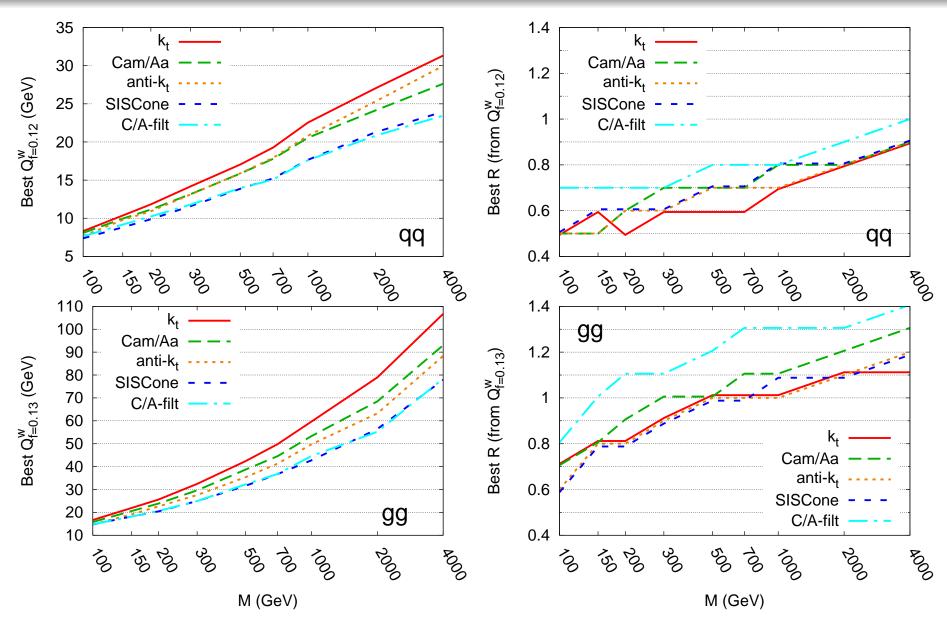




- SISCone and Cam+filtering perform better
- R_{best} strongly depends on the mass

Quarks vs. gluons

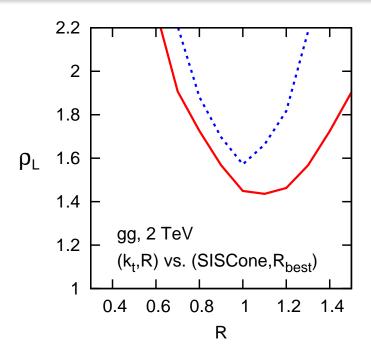




Same conclusions for gluon jets with slightly larger R

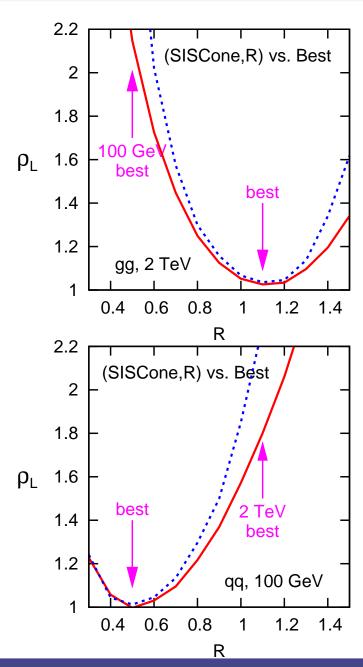
Luminosity ratios





Mandatory at the LHC: Not choosing the best alg. AND R can be very costly for new discoveries

Note: typical choice, $R \sim 0.5$



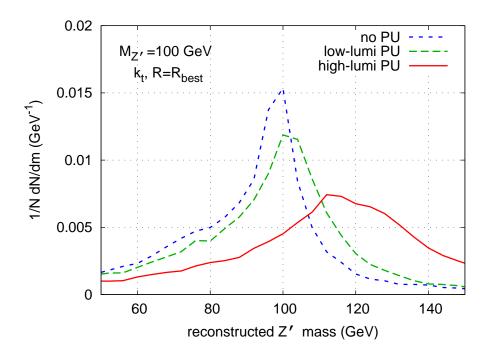


Part 1 Jets in pp collisions Subtracting pileup background using jet areas

Need for subtraction



Pileup \approx uniform soft background that shifts jets to higher p_t



... that needs to be subtracted!

⇒ Using jet areas!

Pileup subtraction



Basic idea: [M.Cacciari, G.Salam, 08]

$$p_{t, \text{subtracted}} = p_{t, \text{jet}} - \rho_{\text{pileup}} \times \text{Area}_{\text{jet}}$$

Pileup subtraction



Basic idea: [M.Cacciari, G.Salam, 08]

$$p_{t, \text{subtracted}} = p_{t, \text{jet}} - \rho_{\text{pileup}} \times \text{Area}_{\text{jet}}$$

- Jet area: [M.Cacciari, G.Salam, G.S., 08]
 - region where the jet catches infinitely soft particles
 - tractable analytically in pQCD

$$\langle \mathcal{A}(p_{t,1}, R) \rangle = \mathcal{A}_{1\text{hard}}(R) + \frac{C_{F,A}}{\pi b_0} \log \left(\frac{\alpha_s(Q_0)}{\alpha_s(Rp_t)} \right) \pi R^2 d$$

Pileup subtraction

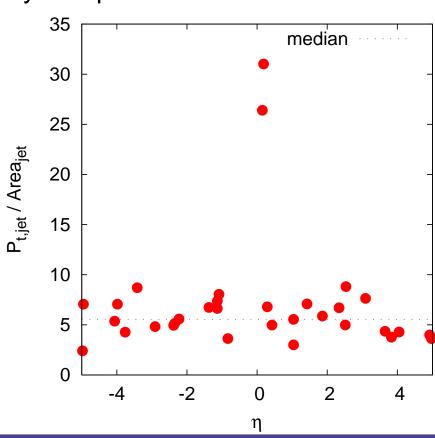


Basic idea: [M.Cacciari, G.Salam, 08]

$$p_{t, \text{subtracted}} = p_{t, \text{jet}} - \rho_{\text{pileup}} \times \text{Area}_{\text{jet}}$$

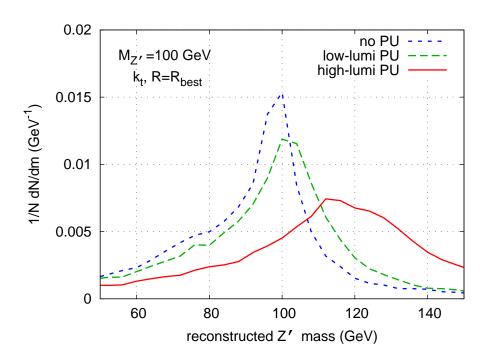
- Jet area: [M.Cacciari, G.Salam, G.S., 08]
 - region where the jet catches infinitely soft particles
 - tractable analytically in pQCD
- Pileup density per unit area: ρ_{pileup} e.g. estimated from the median of $p_{t,\mathrm{jet}}/\mathrm{Area}_{\mathrm{jet}}$

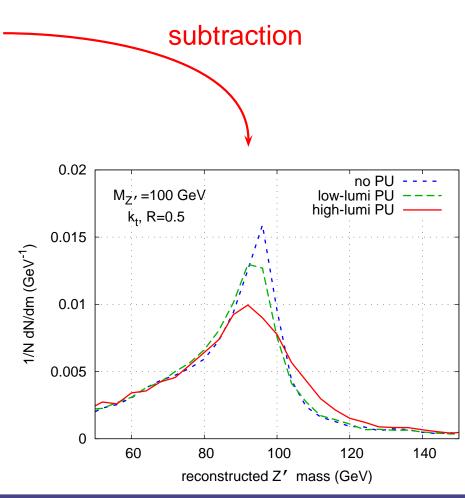
implemented in FastJet on an event-by-event basis



Subtraction at work

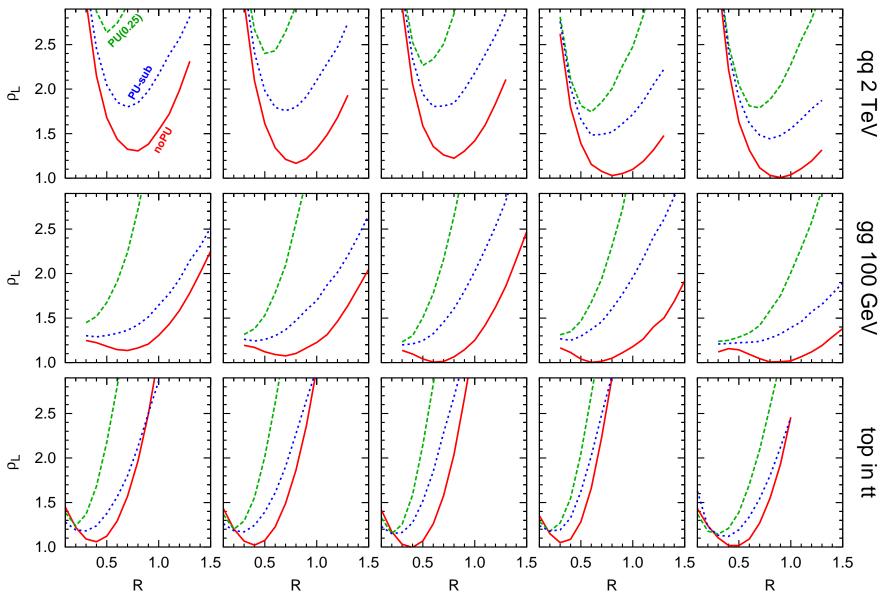






PU effects summary





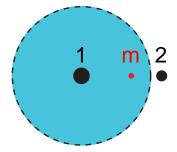
Subtraction \Rightarrow (i) large improvement, (ii) $R_{\text{best}} \sim \text{unchanged}$

Back-reaction

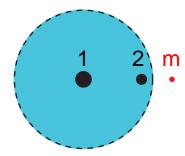


Additional soft background has 2 effects:

- Throw soft particles in the hard jet: dealt with by subtraction
- Modify the hard scattering (back-reaction)
 - can be pointlike or diffuse
 - gain: p_2 gained when adding p_m



• loss: p_2 lost when adding p_m

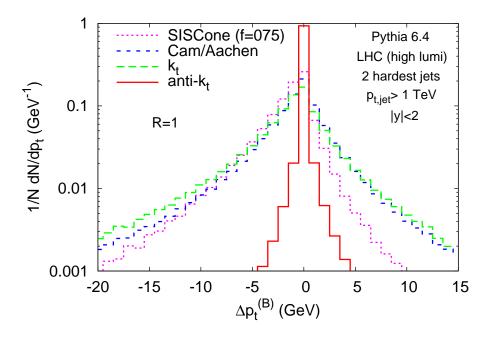


Back-reaction



Additional soft background has 2 effects:

- Throw soft particles in the hard jet: dealt with by subtraction
- Modify the hard scattering (back-reaction)
 - can be pointlike or diffuse
 - tractable analytically (similar to areas)
 - $k_t \gtrsim$ Cambridge > SISCone \gg anti- k_t



Conclusions



Message 1: IRC safety is mandatory

Midpoint and the iterative cone IR or Collinear unsafe (at $\mathcal{O}(\alpha_s^4)$)

Observable	1st miss cones at	Last meaningful order
Inclusive jet cross section	NNLO	NLO
3 jet cross section	NLO	LO (NLO in NLOJet)
W/Z/H + 2 jet cross sect.	NLO	LO (NLO in MCFM)
jet masses in 3 jets	LO	none (LO in NLOJet)

+ We do not want the theoretical efforts to be wasted

- Note: 1 order worse for JetClu of the ATLAS Cone!
- All IRC-safe algorithms available from FastJet (http://www.fastjet.fr)

Conclusions



Message 2: flexibility in jet finding at the LHC

- Optimal jet definition (see also http://quality.fastjet.fr)
 - $m R_{
 m best} \sim 0.5$ at 100 GeV, $R_{
 m best} \sim 1$ at 1 TeV
 - important to choose R_{best} , SISCone and Cam+filt. slightly better
 - ullet same for quark and gluon jets, larger $R_{
 m best}$ for gluons
 - TODO: understand this analytically/ improve clustering (e.g. filtering)
- Pileup subtraction using jet areas
 - Jet areas: clearly defined, analytic control
 - Simple systematic pileup subtraction
 - Same conclusions as without pileup
 - TODO: deal with fluctuating backgroubd (e.g. heavy ions)